

Precalculus Algebra Review Worksheet #4 Rational Expressions Selected Solutions

Perform the indicated operations. Express your answers in simplest form.

$$3. \quad \frac{x+4}{3x^2-12} + \frac{x+1}{3x^2+6x} = \frac{2x-1}{3x(x-2)}$$

$$\begin{aligned} \frac{x+4}{3(x^2-4)} + \frac{x+1}{3x(x+2)} &= \frac{x(x+4) + (x-2)(x+1)}{3x(x+2)(x-2)} = \frac{x^2+4x+x^2-x-2}{3x(x+2)(x-2)} \\ &= \frac{2x^2+3x-2}{3x(x+2)(x-2)} = \frac{(2x-1)(x+2)}{3x(x+2)(x-2)} \end{aligned}$$

$$4. \quad \frac{3}{6x^2+x-2} + \frac{2}{4x^2-4x+1} = \frac{12x+1}{(3x+2)(2x-1)^2}$$

$$\frac{3}{(3x+2)(2x-1)} + \frac{2}{(2x-1)(2x-1)} = \frac{3(2x-1) + 2(3x+2)}{(3x+2)(2x-1)^2} = \frac{6x-3+6x+4}{(3x+2)(2x-1)^2}$$

$$7. \quad \frac{x+2}{10x} - \frac{2x-1}{4x} = \frac{-8x+9}{20x}$$

$$\frac{2(x+2) - 5(2x-1)}{20x} = \frac{2x+4-10x+5}{20x} = \frac{-8x+9}{20x}$$

$$9. \quad \frac{x-3}{5x^2+3x} - \frac{x-5}{5x^2-7x-6} = \frac{6}{x(5x+3)(x-2)}$$

$$\begin{aligned} \frac{x-3}{x(5x+3)} - \frac{x-5}{(5x+3)(x-2)} &= \frac{(x-3)(x-2) - x(x-5)}{x(5x+3)(x-2)} = \\ &= \frac{x^2-5x+6-x^2+5x}{x(5x+3)(x-2)} \end{aligned}$$