Use an appropriate second degree function to solve each of the following problems. Show your work neatly organized.

1. A rectangle has two sides on the coordinate axes and one vertex in the first quadrant on the line $2 x+3 y=24$. What are the dimensions of the rectangle if its area is a maximum? What is the maximum area?
2. Mary wants to fence in a rectangular plot of land and to divide it into three equal areas using two lengths of fencing parallel to two opposite sides. If she has a total of 200 feet of fencing to work with, then find the dimensions that will maximize the total area enclosed.
3. A television set manufacturer can sell $\mathbf{4 0 0}$ sets per month for $\mathbf{\$ 3 0 0}$ per set. Marketing research indicates that the company can sell 20 more sets per month for each $\$ 10$ decrease in price. What price per set will give the greatest monthly income? What is the maximum monthly income?

Use an appropriate second degree function to solve each of the following problems. Show your work neatly organized.
4. One number is five less than two times another. The sum of their squares is a minimum. What are the numbers?
5. A long piece of sheet metal 30 inches wide is to be made into a rain gutter with a rectangular cross section by bending up a vertical strip along each side. How many inches should be bent up along each side so that the gutter formed has a maximum cross-sectional area?
6. The summer theater charges $\$ 3$ per ticket and has a full house of 360 people nightly. The manager estimates that the ticket sales would decrease by 60 people for every $\$ 1$ increase in the ticket price. What price per ticket would maximize the total income?

