Evaluate each of the following determinants. Show your work neatly organized.

$$\begin{vmatrix} 3 & 5 \\ 2 & 4 \end{vmatrix} = \underline{\qquad}$$

$$\begin{vmatrix}
-2 & 3 \\
-3 & 2
\end{vmatrix} = \underline{\qquad}$$

3.
$$\begin{vmatrix} -5 & 4 & -2 \\ 0 & 6 & 2 \\ 0 & 0 & -3 \end{vmatrix} = \underline{\qquad}$$

5.
$$\begin{vmatrix} 4 & 1 & 1 & 2 \\ 3 & -2 & 0 & -1 \\ -1 & 0 & 3 & 0 \\ 2 & 0 & -1 & 3 \end{vmatrix} = \underline{\hspace{1cm}}$$

Use Cramer's rule to solve each of the following systems. Show your work neatly organized.

6.
$$3x + 2y = 0$$

 $x - 3y = -11$

7.
$$3x + y = 2$$

 $5x + 3y = 3$

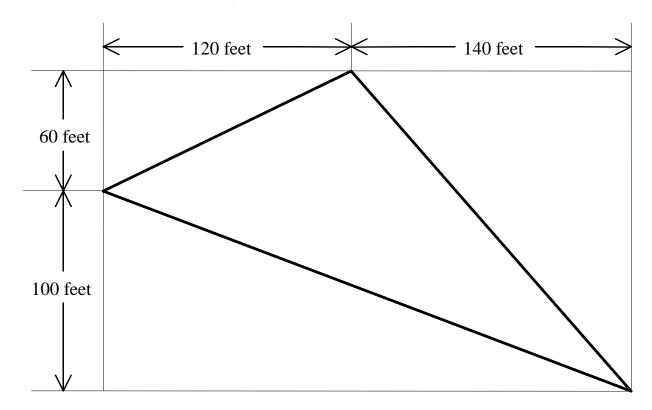
8.
$$x + 3y - z = -4$$

 $2x - 2y + z = 9$
 $-2x + y - 3z = -14$

9.
$$3x + 5y = 2$$

 $2x - 3z = -5$
 $4y + z = 3$

10. Consider the triangular region shown below. Use a determinant to find its area. Show your work neatly organized.



11. For this problem, you must decode a message. The matrix, A, that was used to encode the message is given below. The matrix C represents the coded message. What you must do is find A^{-1} and then multiply it by C. The order is important. If M is the matrix representing the message, then $M = (A^{-1})(C)$.

$$\mathbf{A} = \begin{bmatrix} -2 & 0 & 2 & 1 \\ 2 & -1 & 0 & 4 \\ 1 & -1 & -1 & 2 \\ 0 & -1 & -1 & 1 \end{bmatrix} \qquad \mathbf{C} = \begin{bmatrix} 13 & -33 & -6 & 11 \\ 85 & 60 & 82 & 45 \\ 21 & 21 & 38 & 3 \\ -11 & -9 & 11 & -17 \end{bmatrix}$$