Use implicit differentiation to find dy/dx for each of the following equations. Show your work neatly organized.

1. 
$$x^2 + y^2 = 16$$
  
2.  $2x^2 + xy - y^2 = 2$ 

3. 
$$4x^2 + 9y^2 = 36$$
  
4.  $x^2 + y^2 + 4x + 2y - 11 = 0$ 

5. 
$$x^2 - 4y^2 = 16$$
  
6.  $9x^2 - 4y^2 + 18x + 16y + 29 = 0$ 

7. 
$$y^2 + 3xy - 4x^2 = 10$$
  
8.  $5y^2 + 8xy - 5x + 5y + 10 = 0$ 

Find the equation of the line that is tangent to the graph of the given equation at the given point. Sketch a graph of the given equation showing the tangent line.

9. 
$$x^2 + y^2 = 25$$
; (3,-4)  
10.  $xy = 12$ ; (-3,-4)

11. 
$$x^2 - y^2 = 16$$
; (5,-3)  
12.  $4x^2 + y^2 + 8x - 4y - 8 = 0$ ; (-3,2)

Find the equation of the line that is normal to the graph of the given equation at the given point. Sketch a graph of the given equation showing the normal line.

13. 
$$x^2 + y^2 = 25$$
; (-3,-4) 14.  $xy = -6$ ; (3,-2)

15. 
$$x^2 - y^2 = 16$$
; (5,-3)  
16.  $x^2 + y^2 - 4x + 2y - 20 = 0$ ; (-1,3)