Find the general solution and the specific solution to each of the following differential equations. Show your work neatly organized.

1.
$$f'(x) = x^2 - 2x + 3$$
; $f(0) = 4$

2.
$$f'(x) = 3x^2 + 4x - 1$$
; $f(2) = 0$

3.
$$f'(x) = (x+2)^2$$
; $f(-3) = 1$

4.
$$f''(x) = 3x - 4$$
; $f(0) = -2$; $f(2) = -2$

5.
$$f''(x) = -6x + 6$$
; $f(1) = 3$; $f(3) = -3$

Write a differential equation and use it to answer the following questions. Show your work neatly organized.

6. The slope, m, of a particular curve at any point (x, y) on the curve is given by the equation m = 4x - 3. Find the equation of the curve if it passes through the point (1, 3).

7. A function is such that its second derivative is f''(x) = -6x. Find its equation if it is tangent to y = x + 3 at the point (3, 4).