

Calculus Lesson #1 Unit 11

Class Worksheet #1

Solids of Revolution

Disks

Calculus Class Worksheet #1 Unit 11 Solutions

Use “disks” to find the volume generated by rotating the given region about the given line. For each problem, you must

- a) sketch the generating region, showing a typical generating rectangle,
- b) write an expression for the volume generated by this rectangle,
- c) express the exact volume of the solid as a definite integral, and
- d) evaluate the integral.

Sample 1a. The region in the first quadrant bounded by $x + 2y = 10$ and the coordinate axes is rotated about the x-axis.

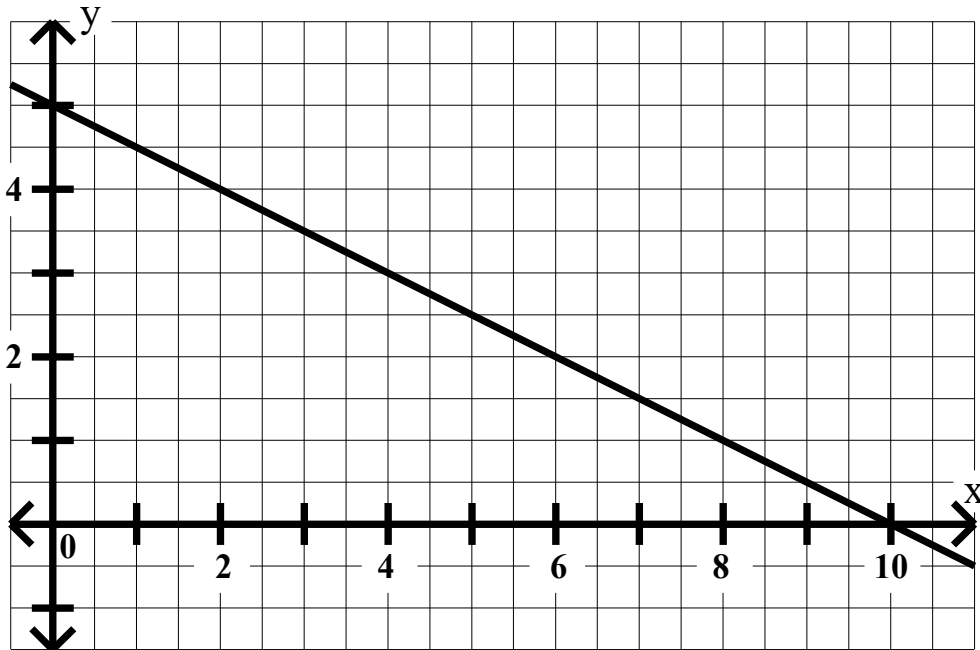
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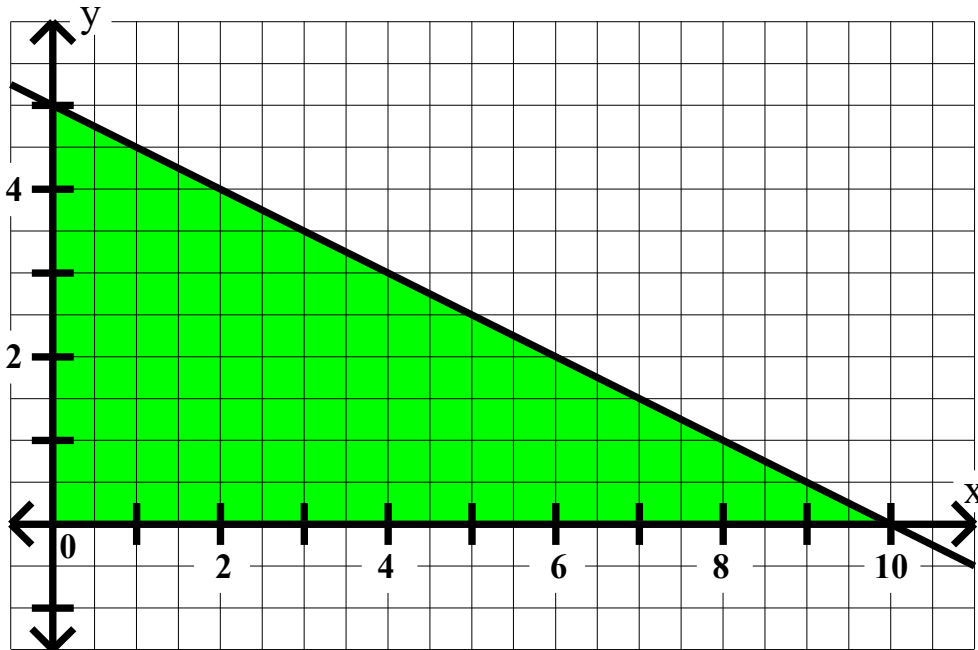
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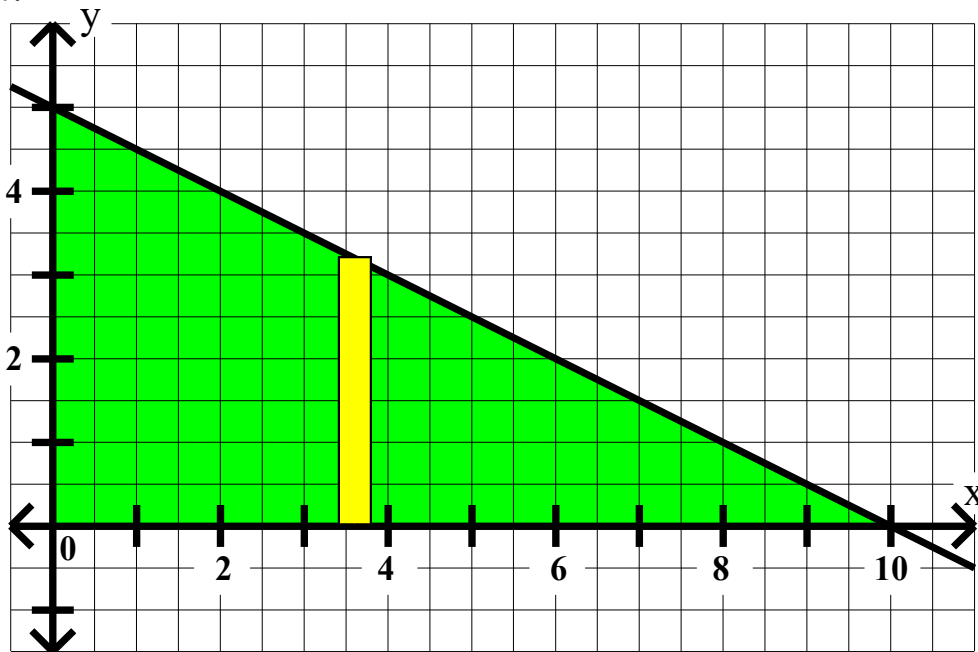
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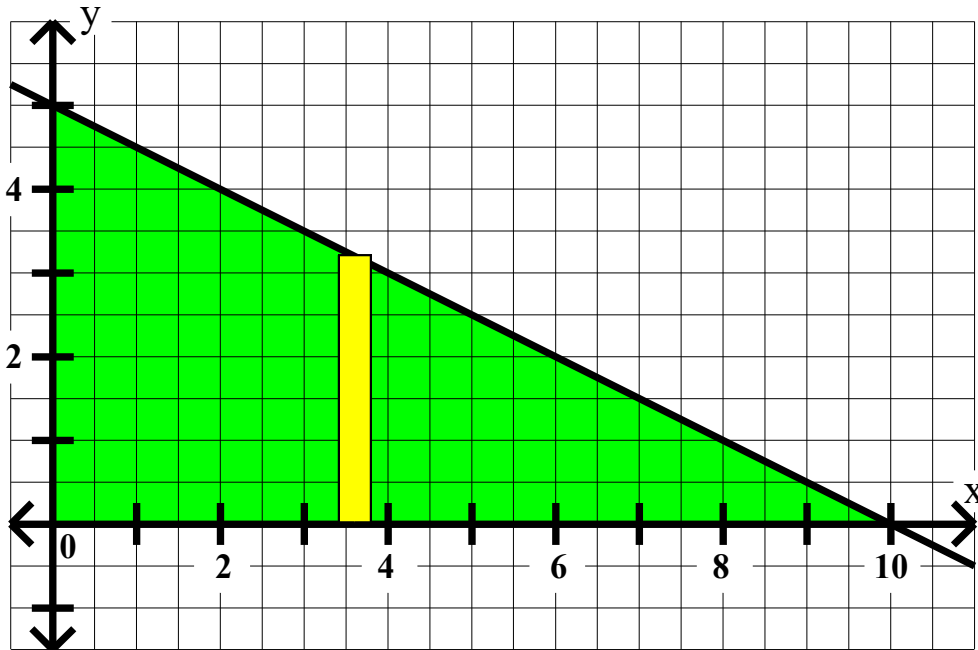
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Disks: $V = \pi r^2 h$

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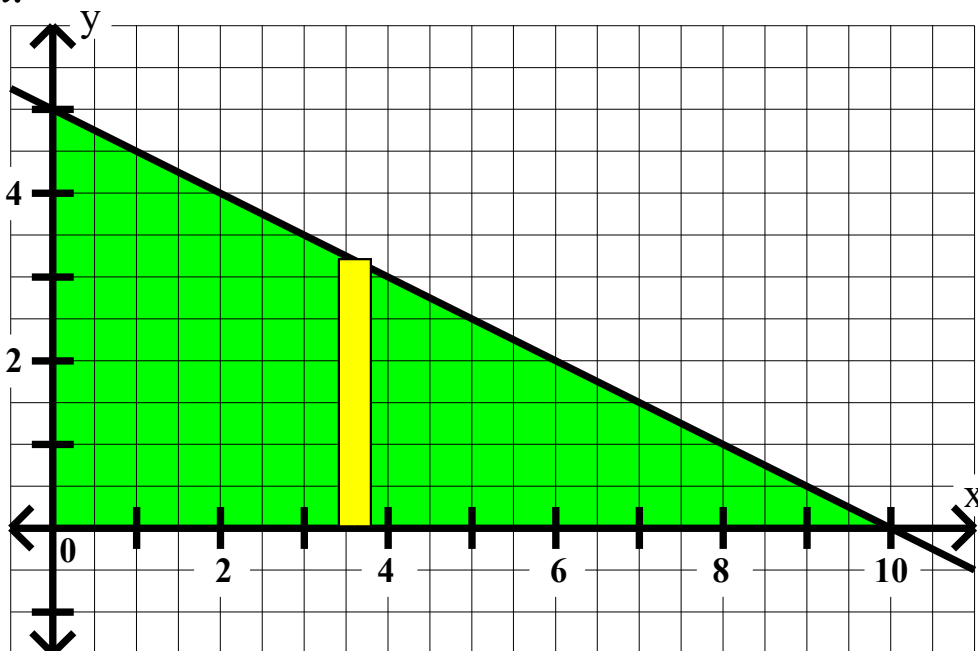
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$h =$

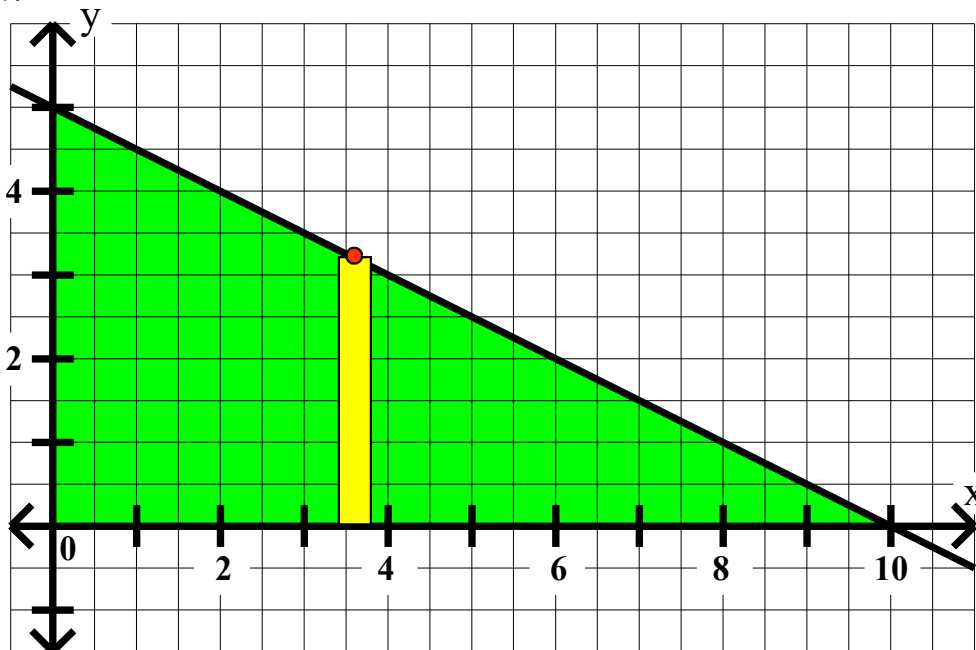
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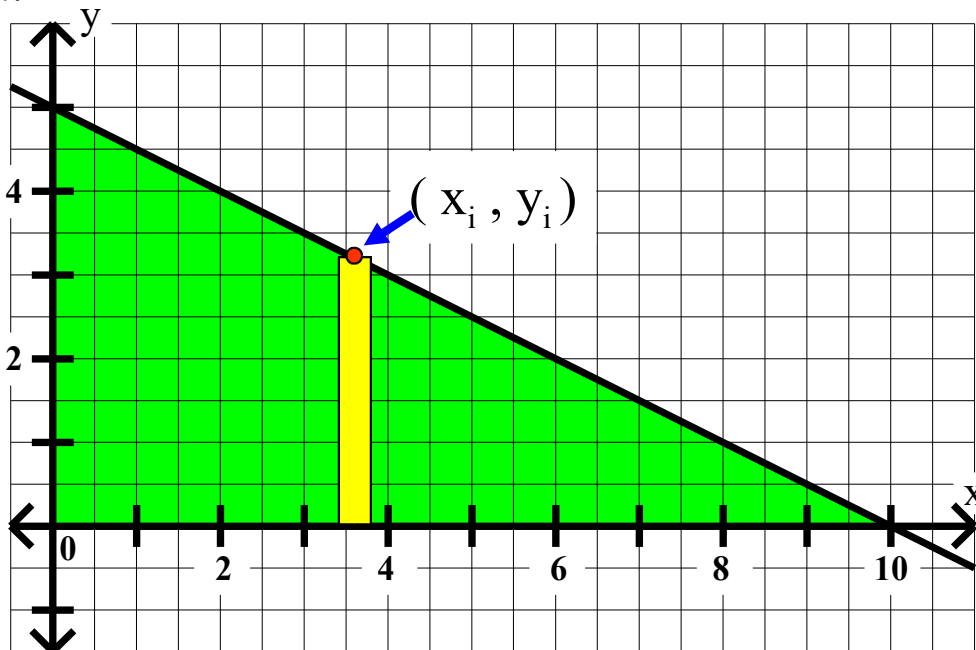
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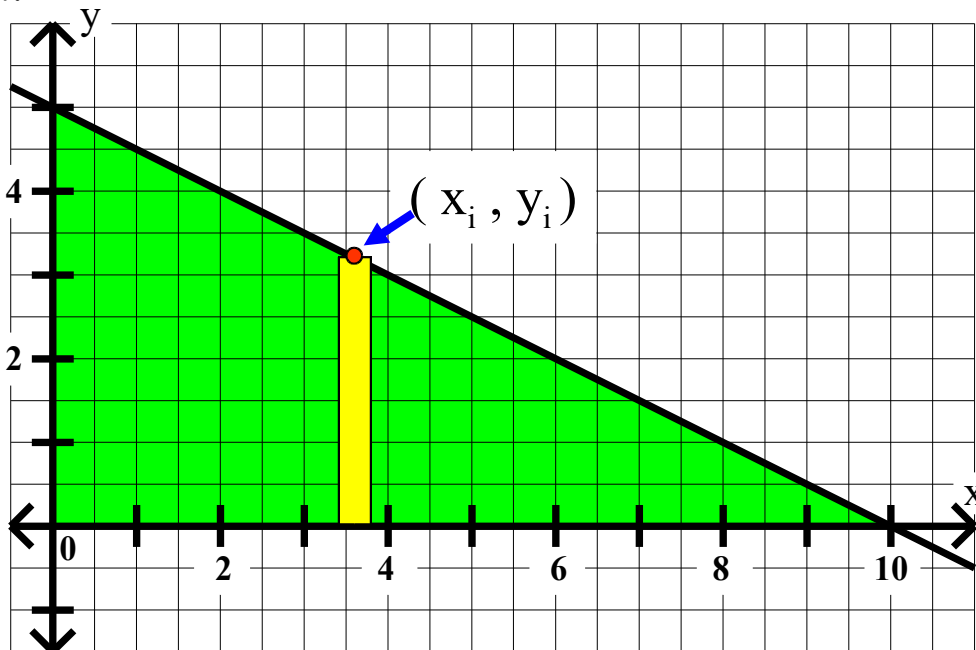
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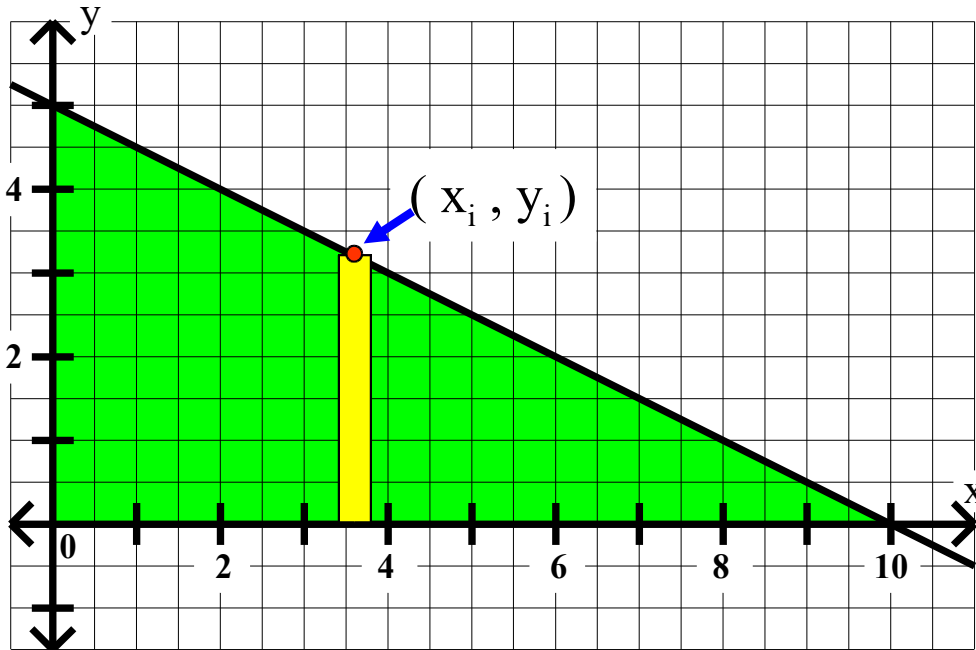
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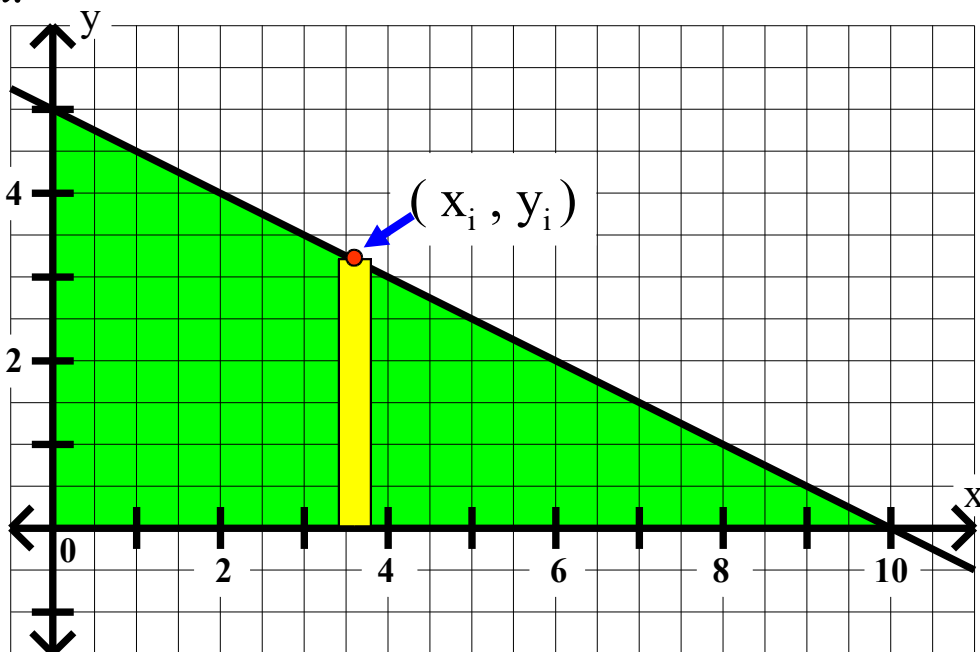
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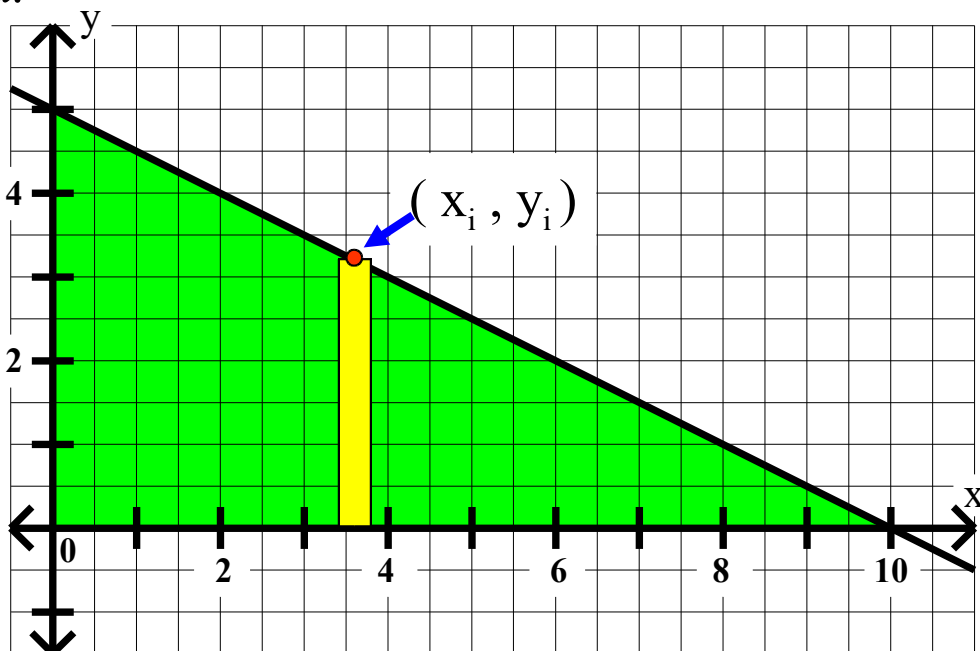
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b. $V_i =$

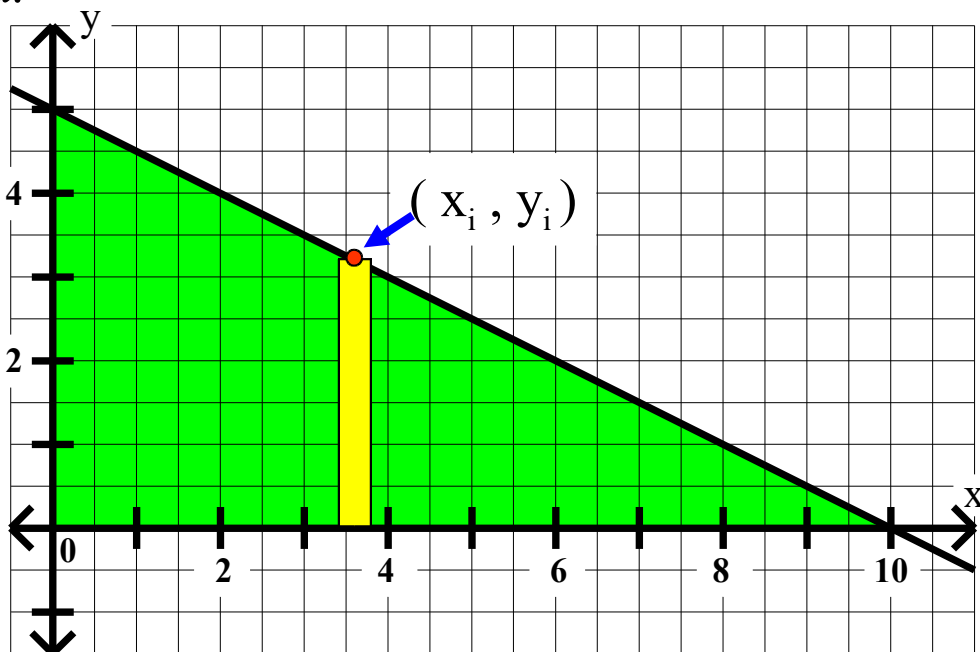
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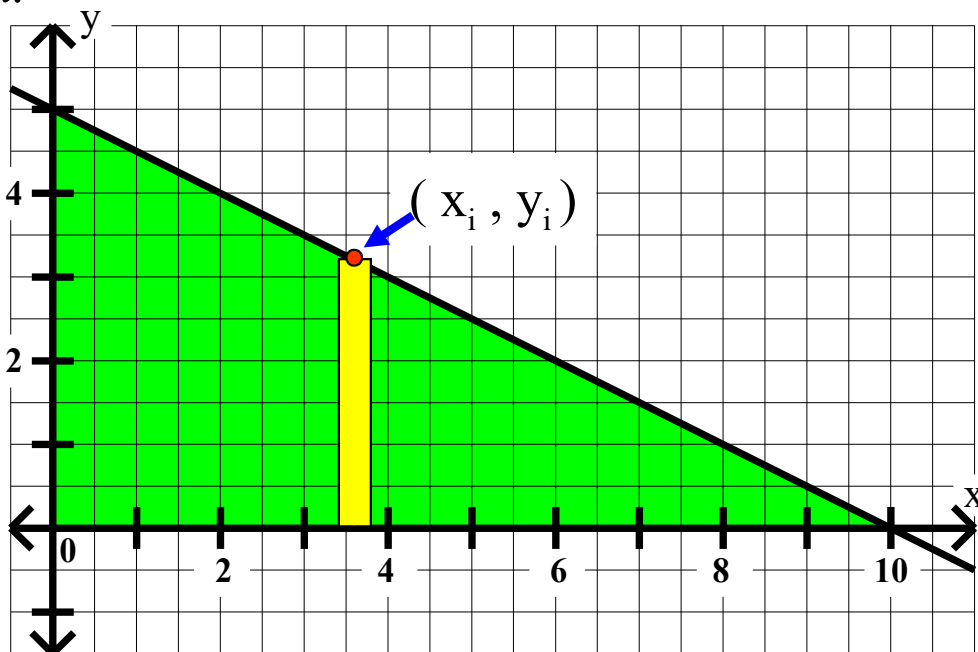
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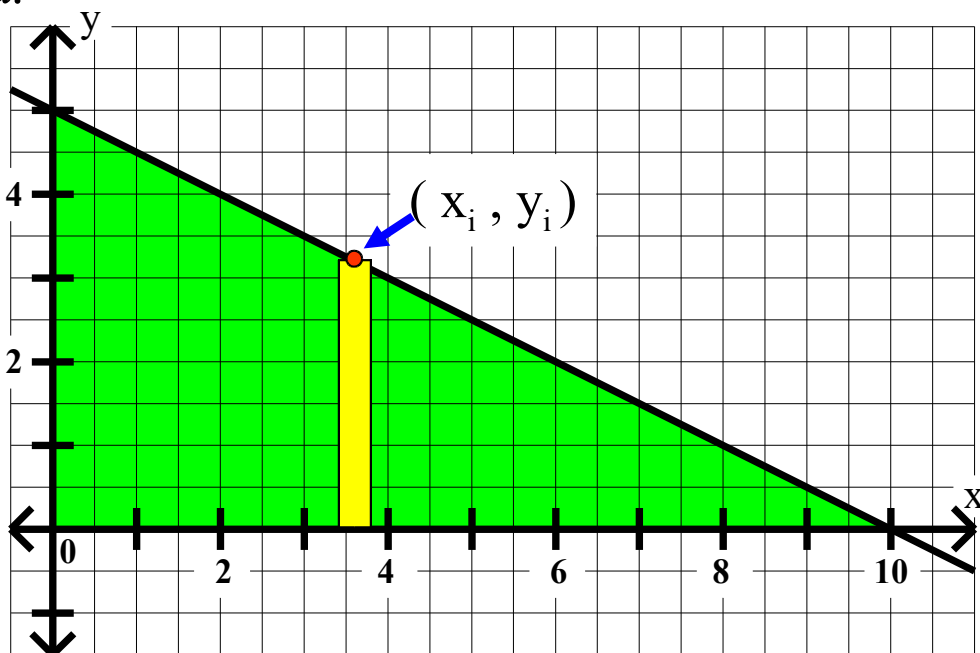
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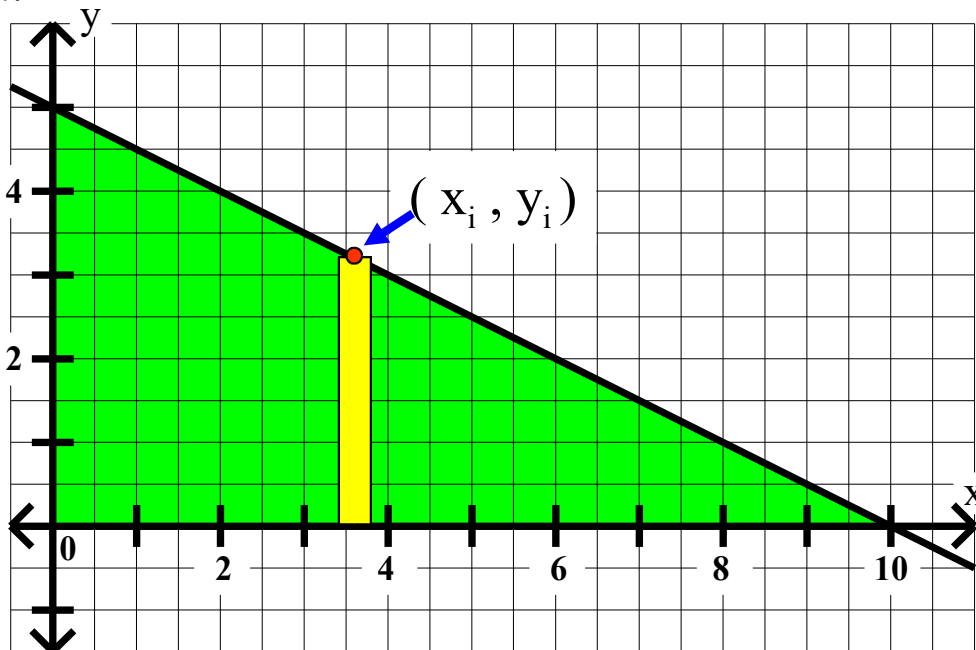
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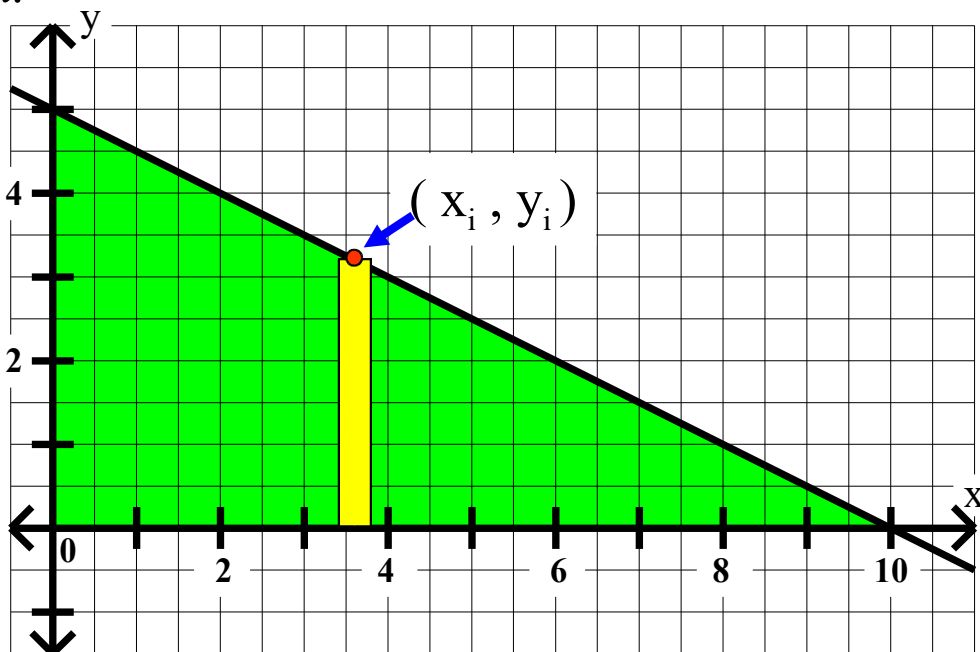
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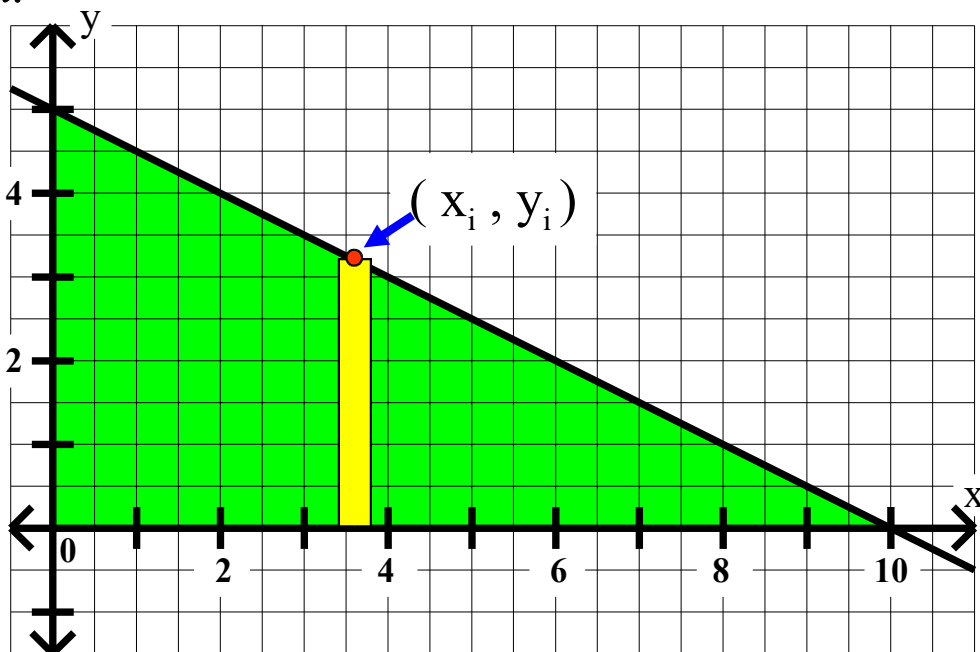
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c. $V =$

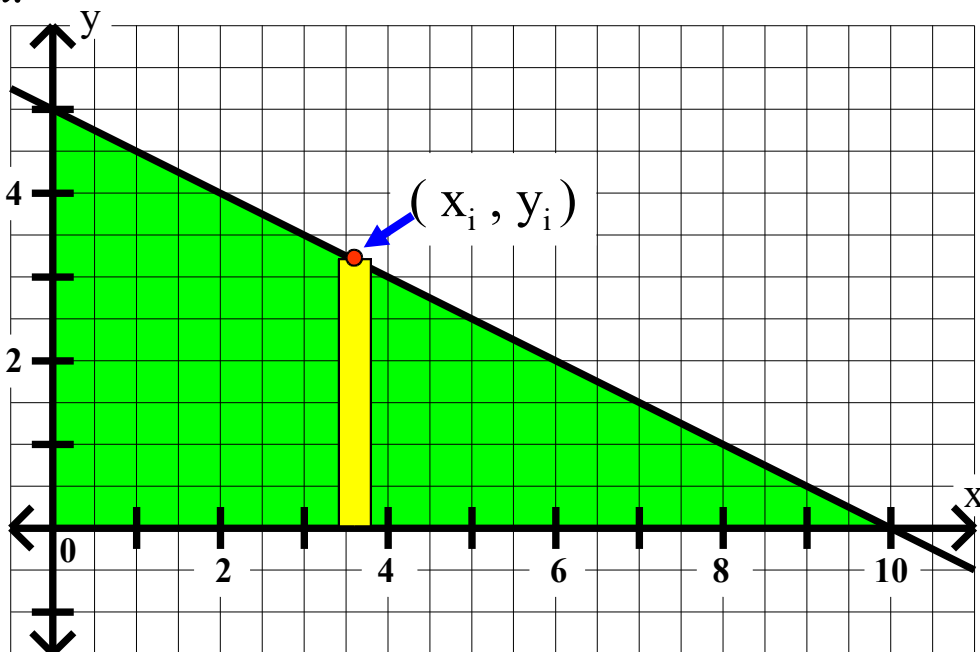
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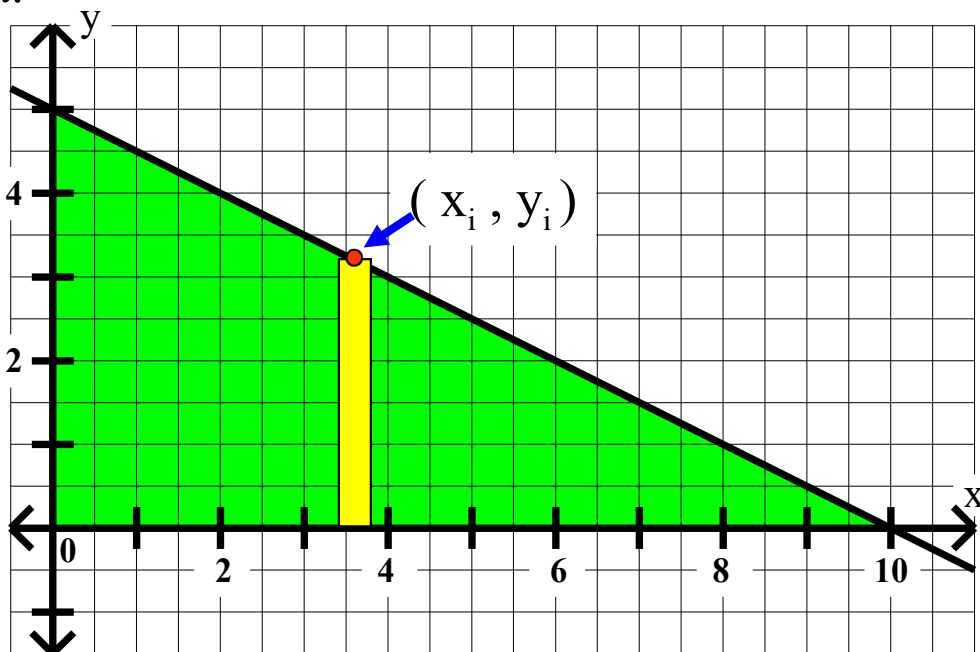
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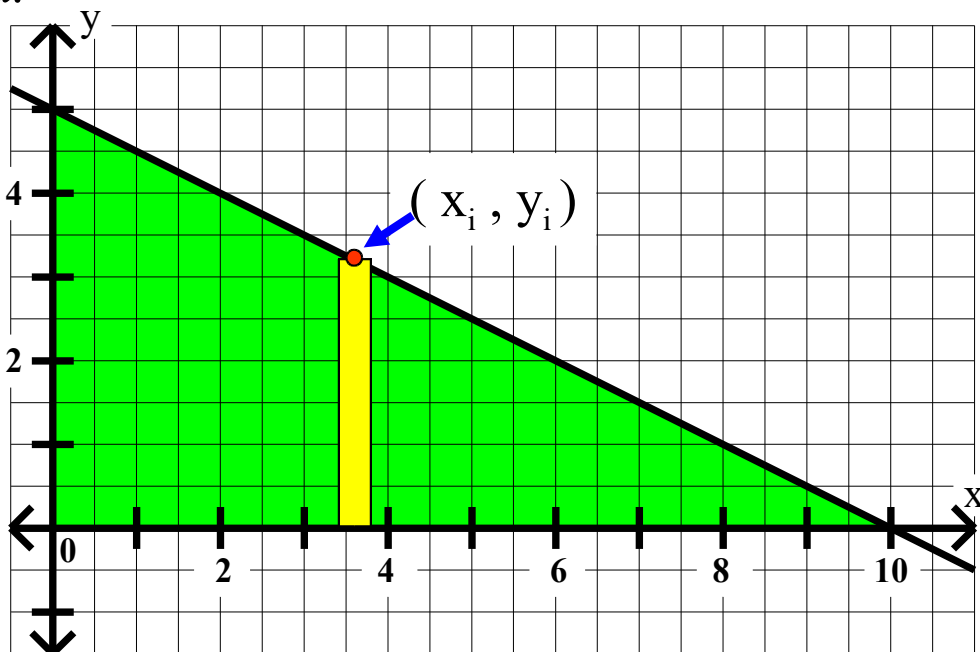
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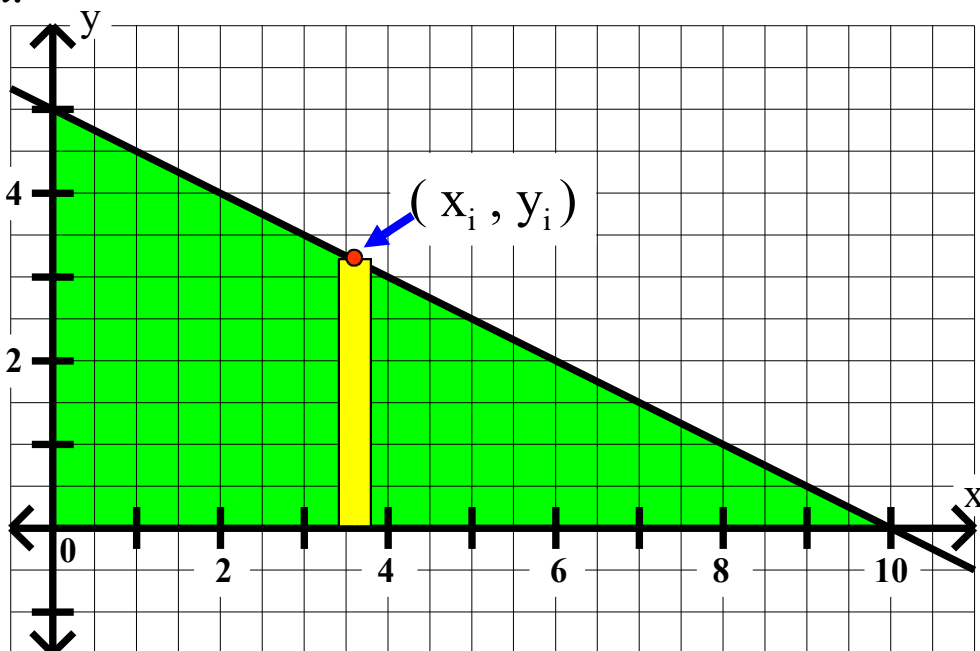
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b. $V_i = \pi \left(\frac{-1}{2}x_i + 5 \right)^2 \Delta x$

c. $V = \pi \int_0^{10} \left(\frac{-1}{2}x + 5 \right)^2 dx$

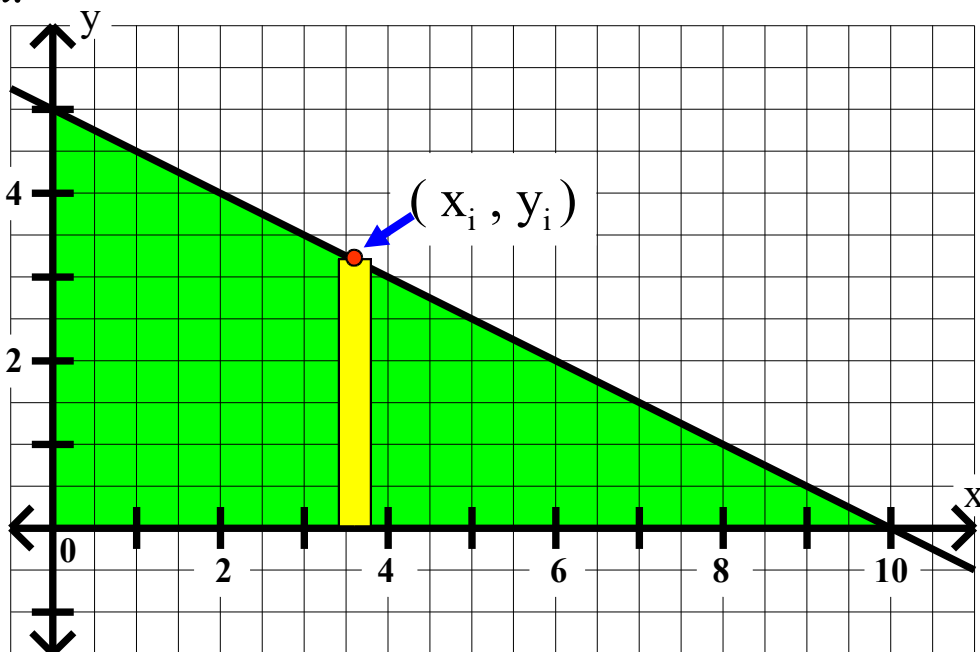
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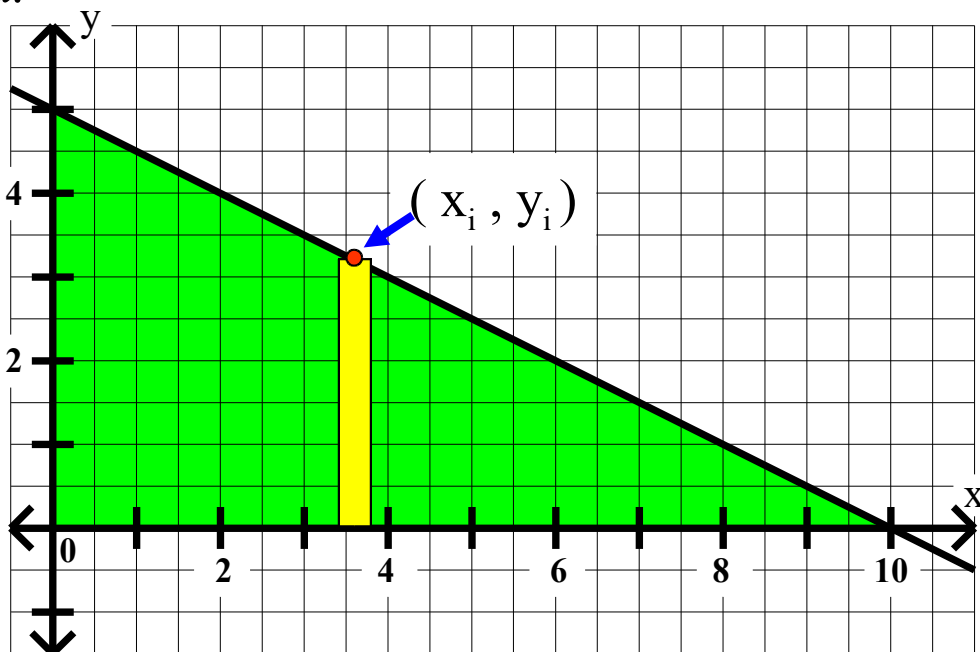
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d. $V \approx$

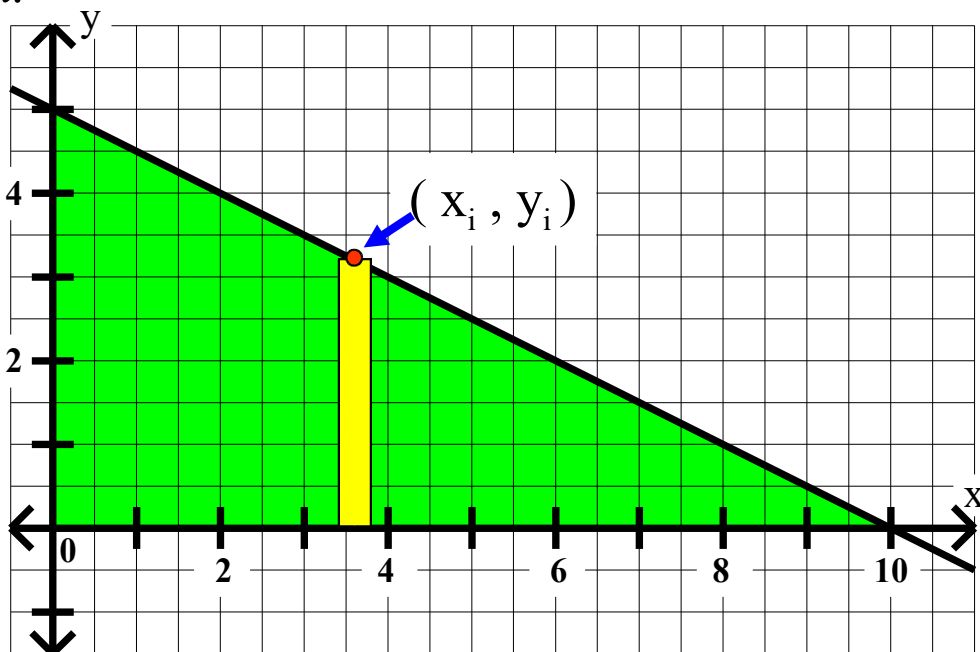
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c. $V = \pi \int_0^{10} \left(\frac{-1}{2}x + 5 \right)^2 dx$

d. $V \approx 262$ cu. units

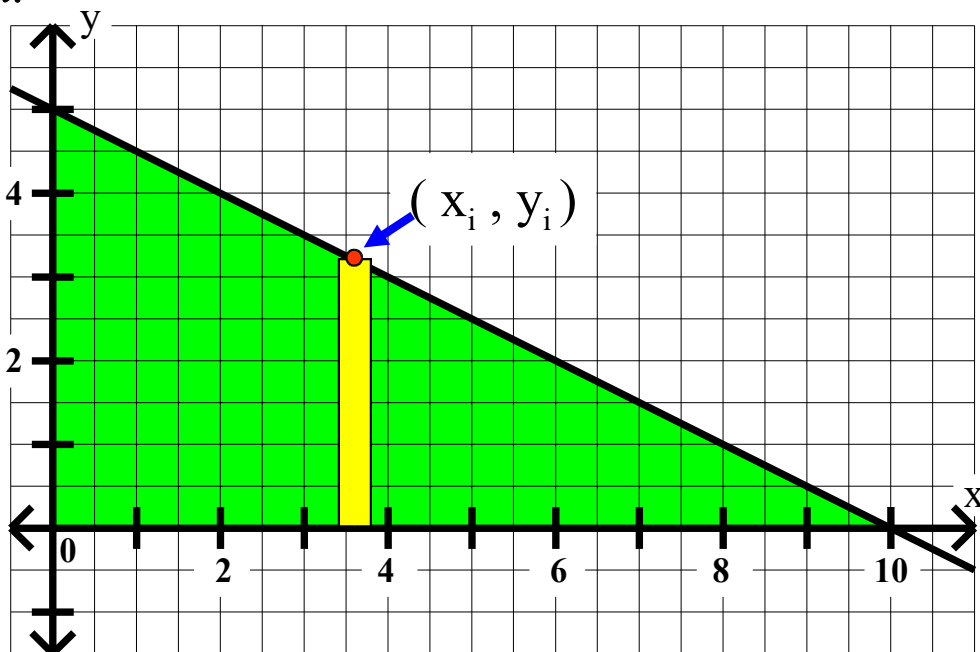
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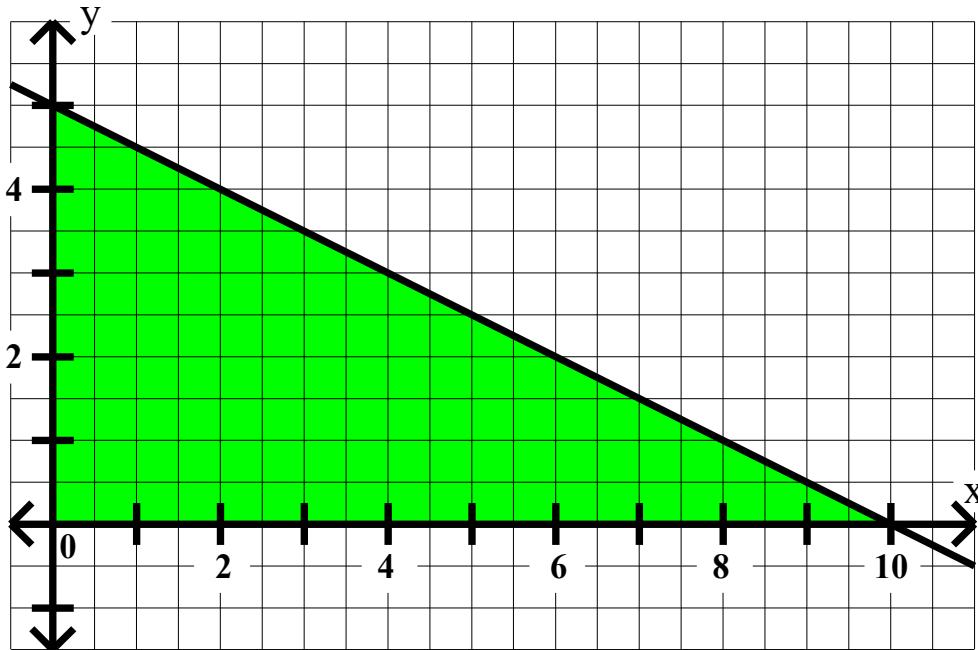
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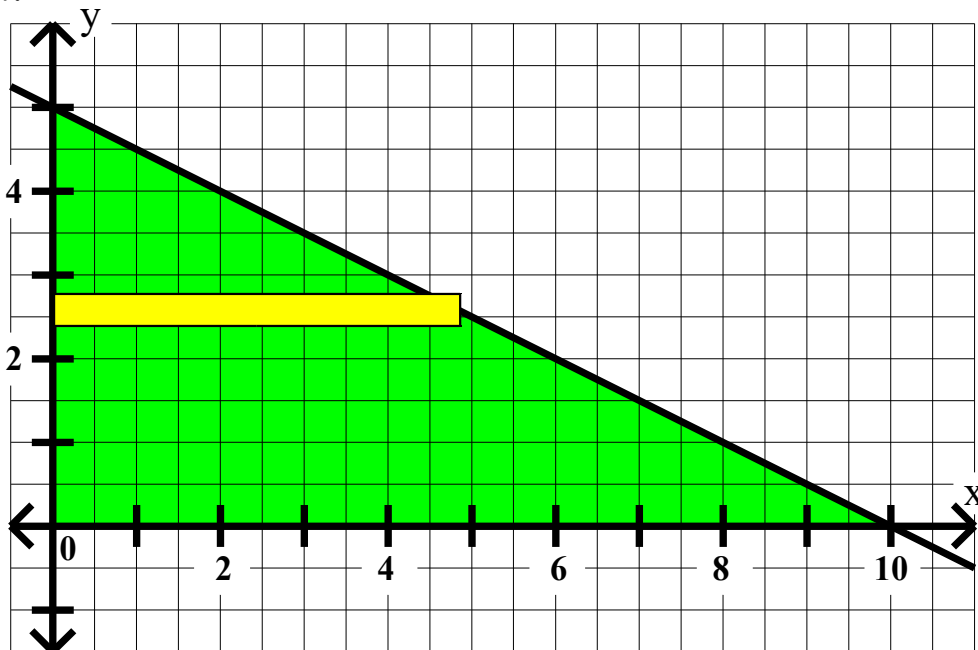
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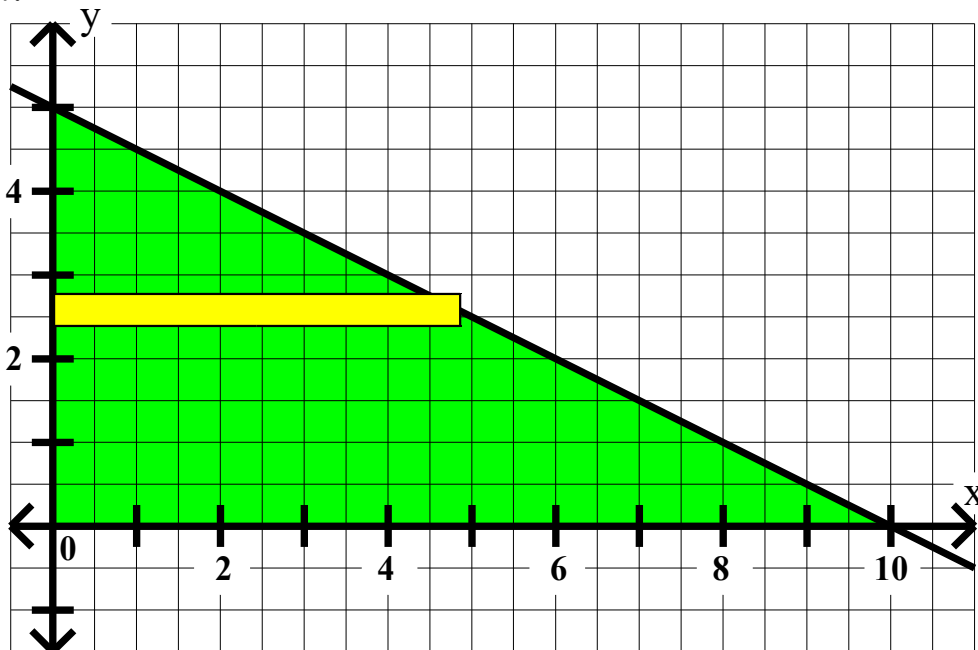
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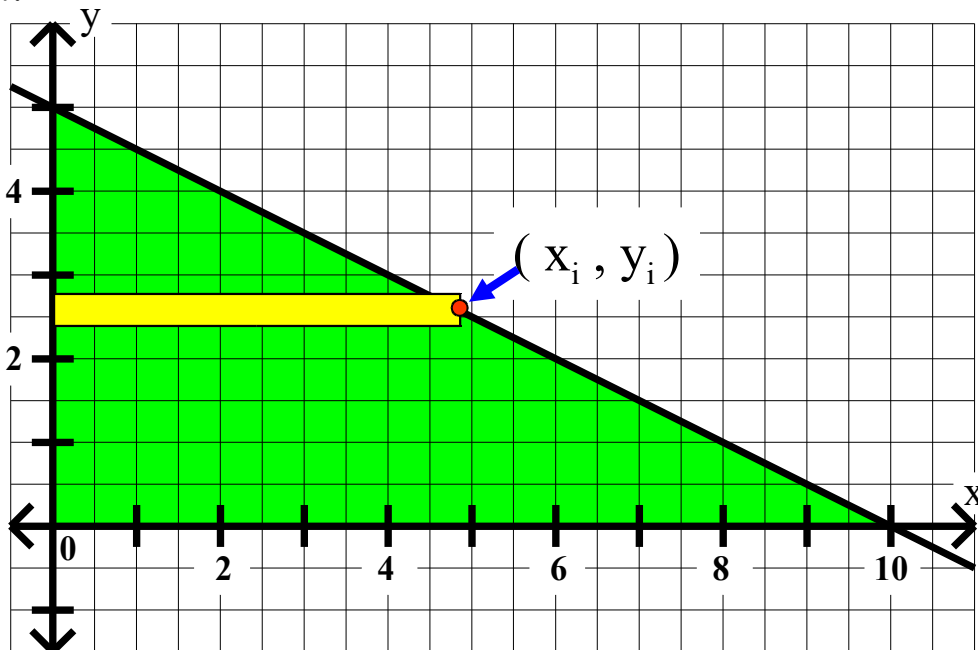
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$h =$

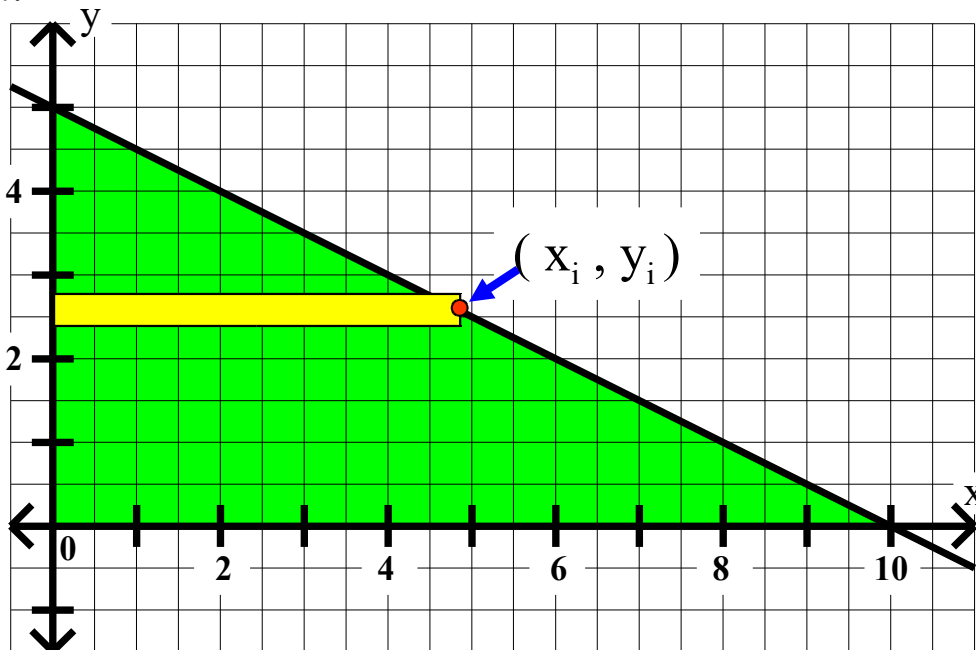
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- sketch the generating region, showing a typical generating rectangle,
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Sample 1b. The region in the first quadrant bounded by $x + 2y = 10$ and the coordinate axes is rotated about the y -axis.

a.



Disks: $V = \pi r^2 h$

$$r = x_i$$

$$h =$$

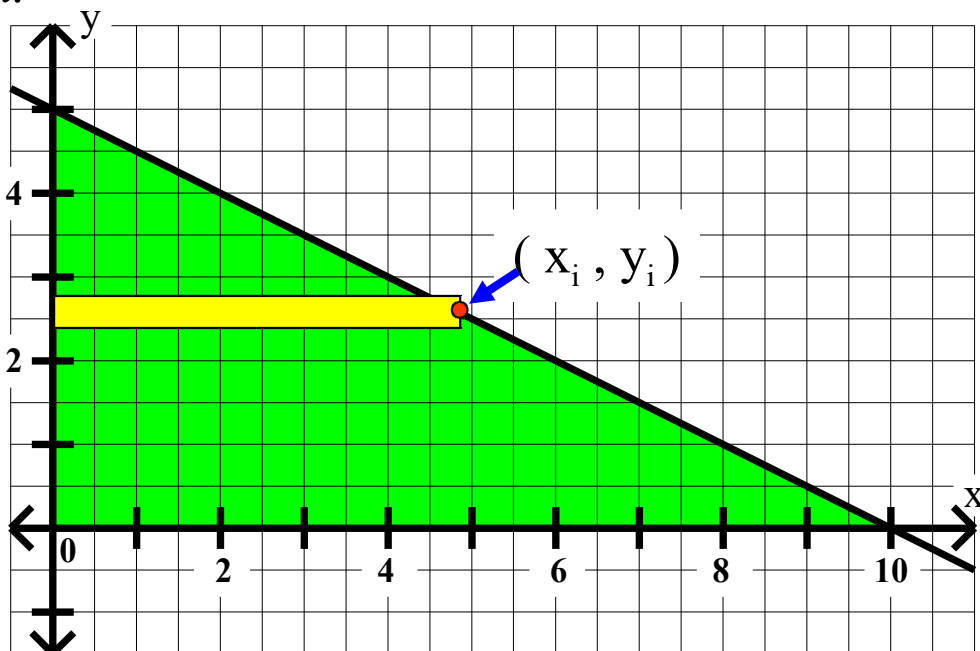
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Disks: $V = \pi r^2 h$

$$r = x_i$$

$$h = \Delta y$$

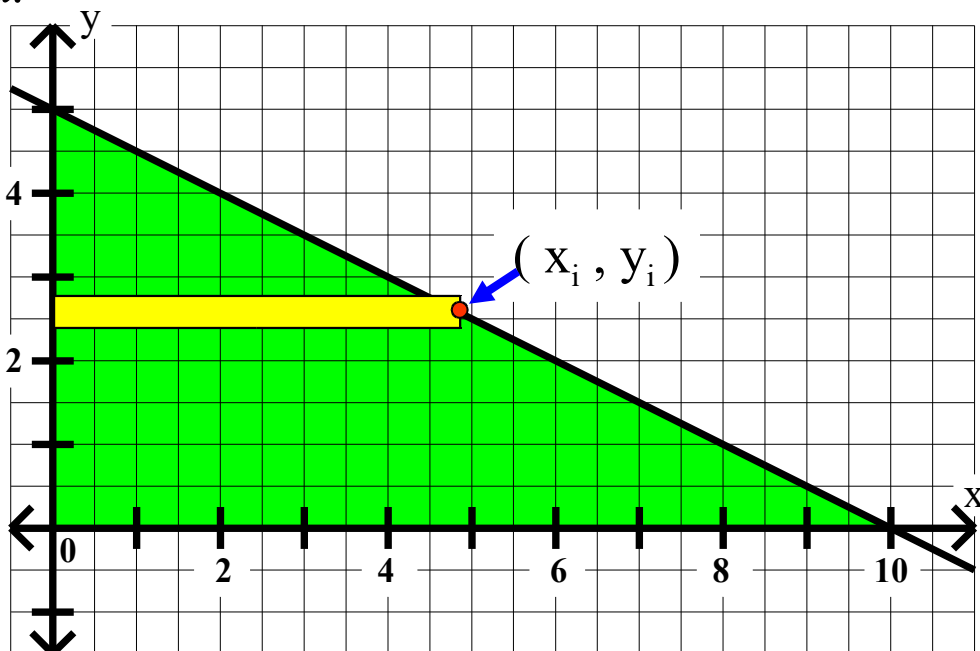
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$$r = x_i = -2y_i + 10$$

$$h = \Delta y$$

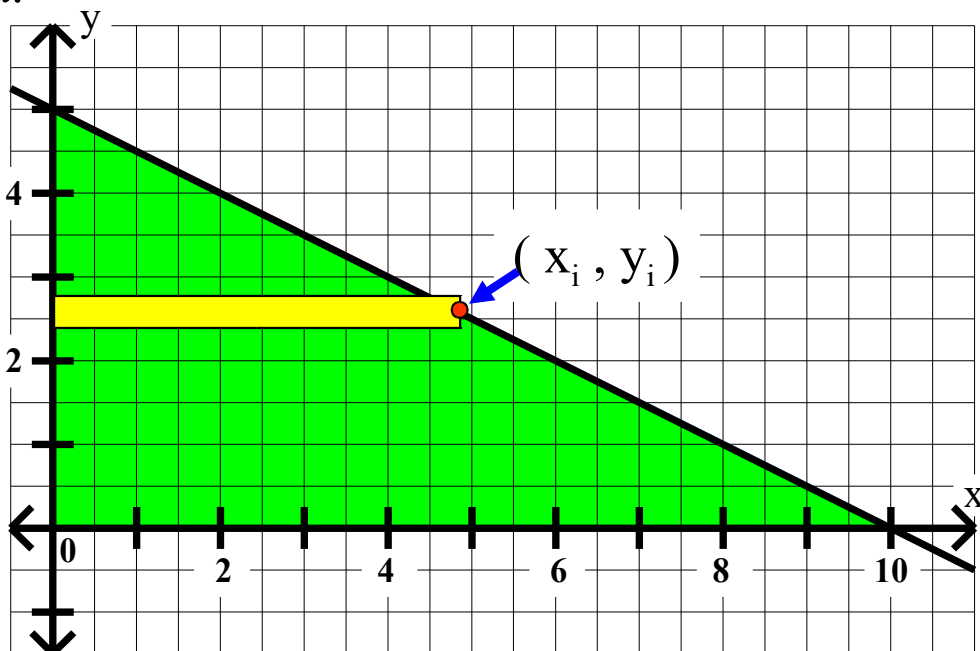
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$$h = \Delta y$$

b. $V_i =$

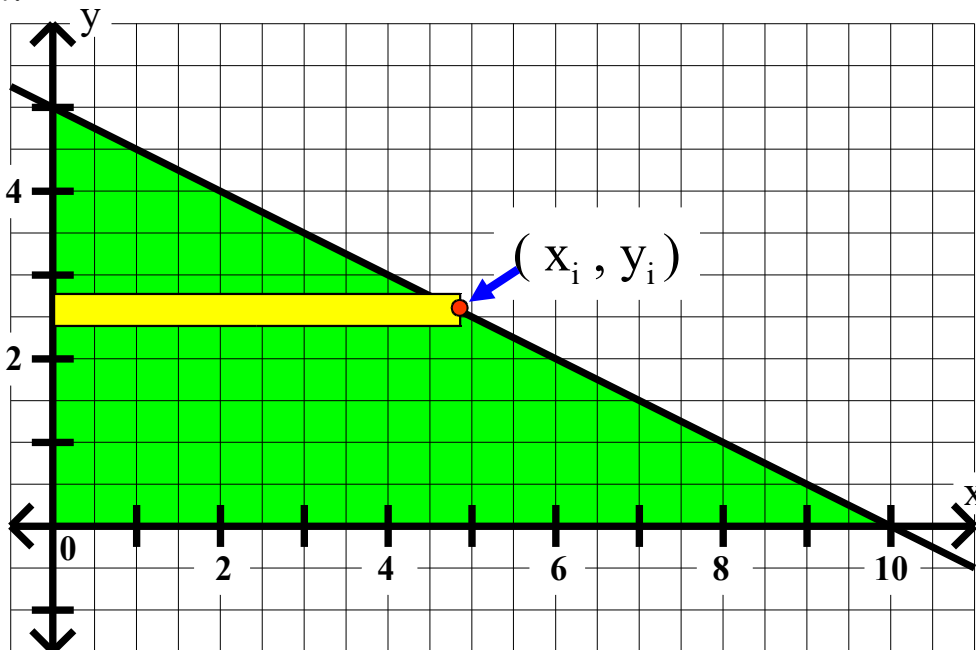
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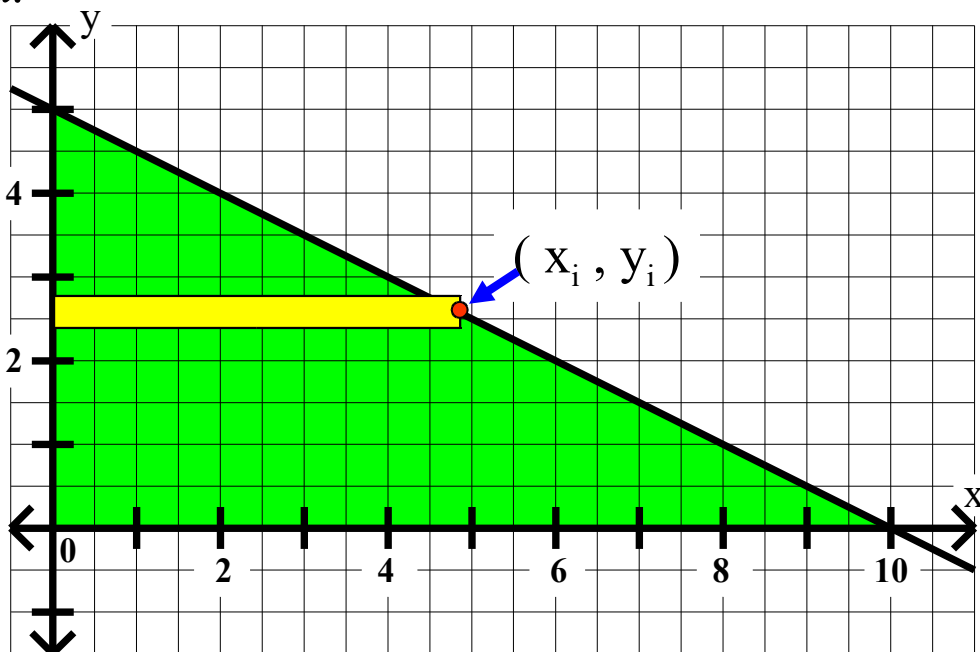
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$$b. V_i = \pi(-2y_i + 10)^2 \Delta y$$

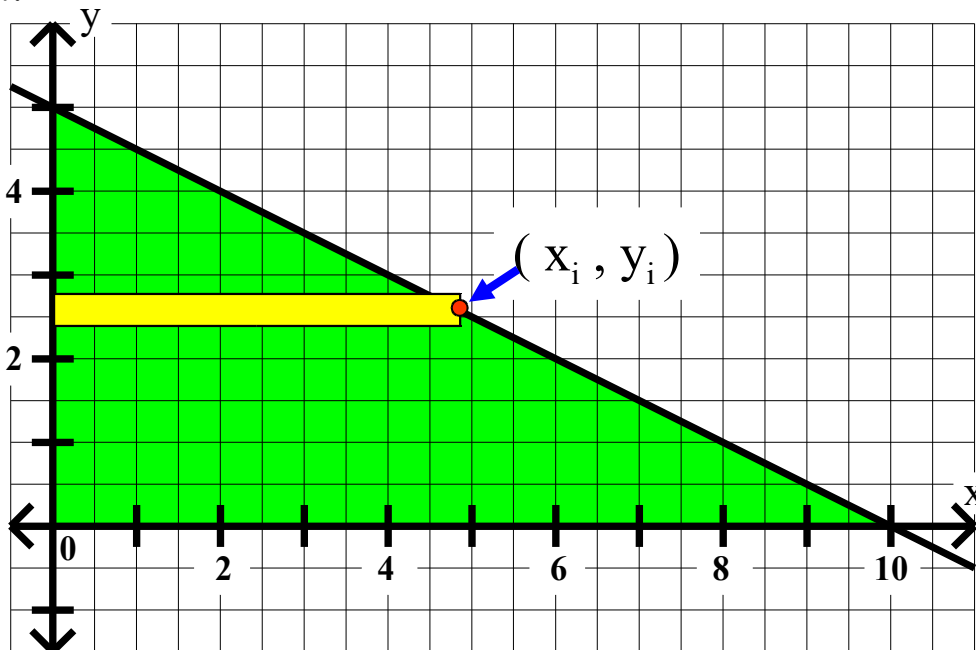
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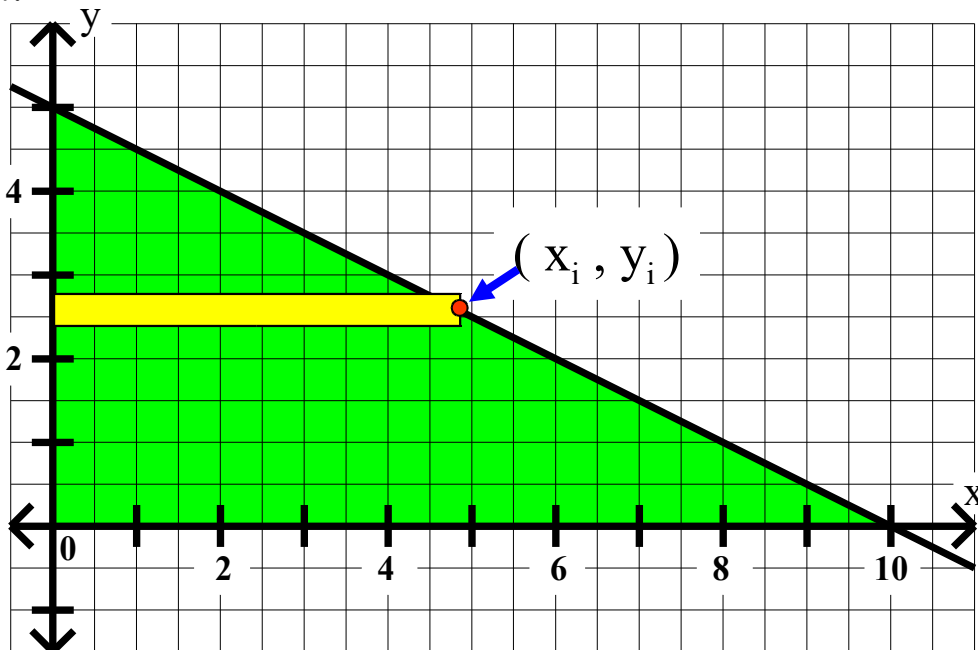
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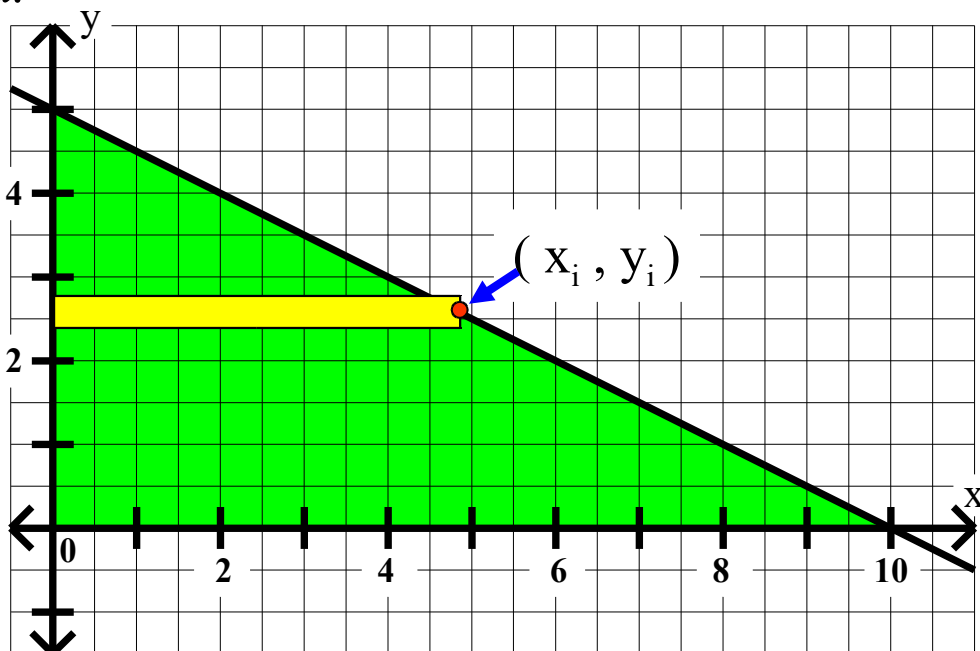
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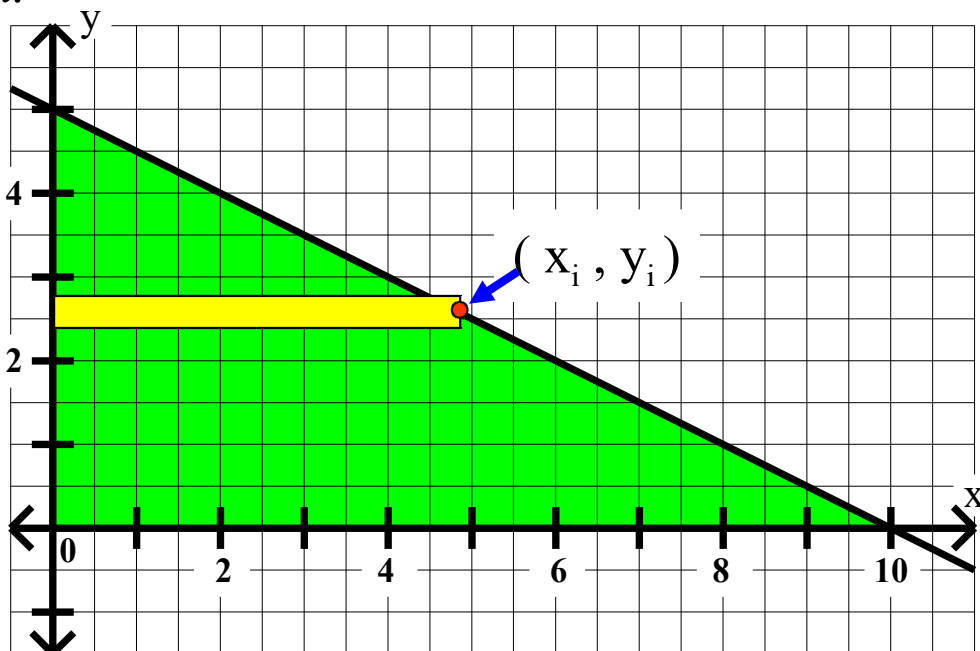
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$$h = \Delta y$$

b. $V_i = \pi(-2y_i + 10)^2 \Delta y$

c. $V =$

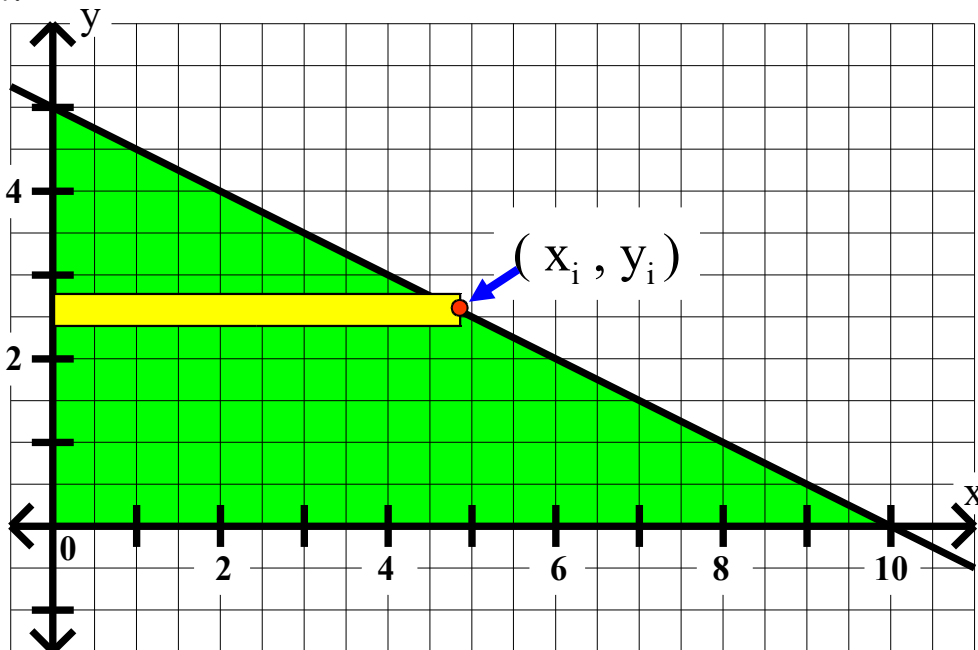
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c. $V = \pi$

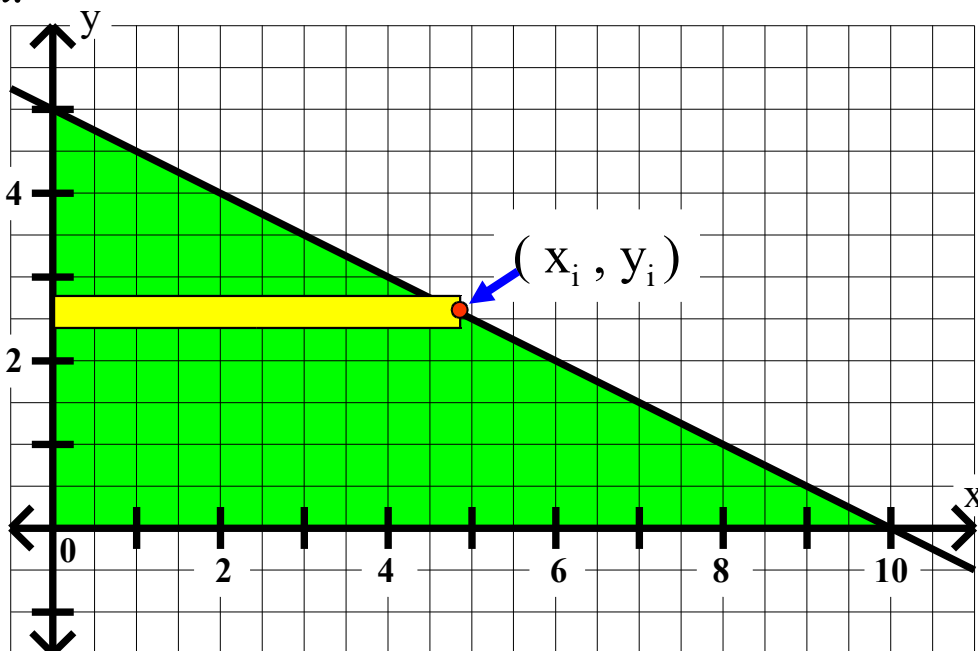
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b. $V_i = \pi(-2y_i + 10)^2 \Delta y$

c. $V = \pi \int$

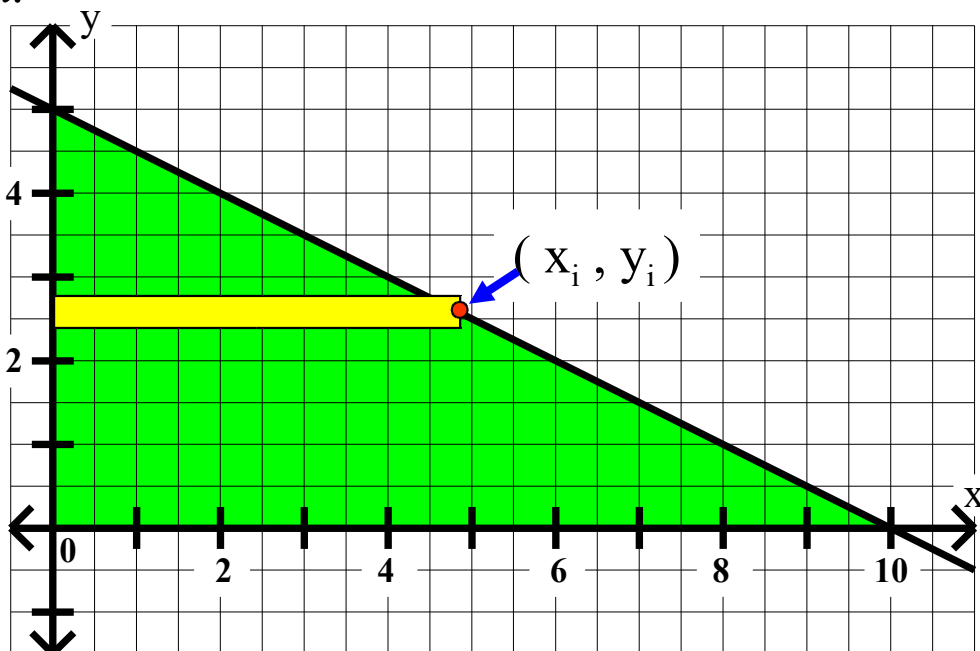
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b. $V_i = \pi(-2y_i + 10)^2 \Delta y$

c. $V = \pi \int (-2y + 10)^2 dy$

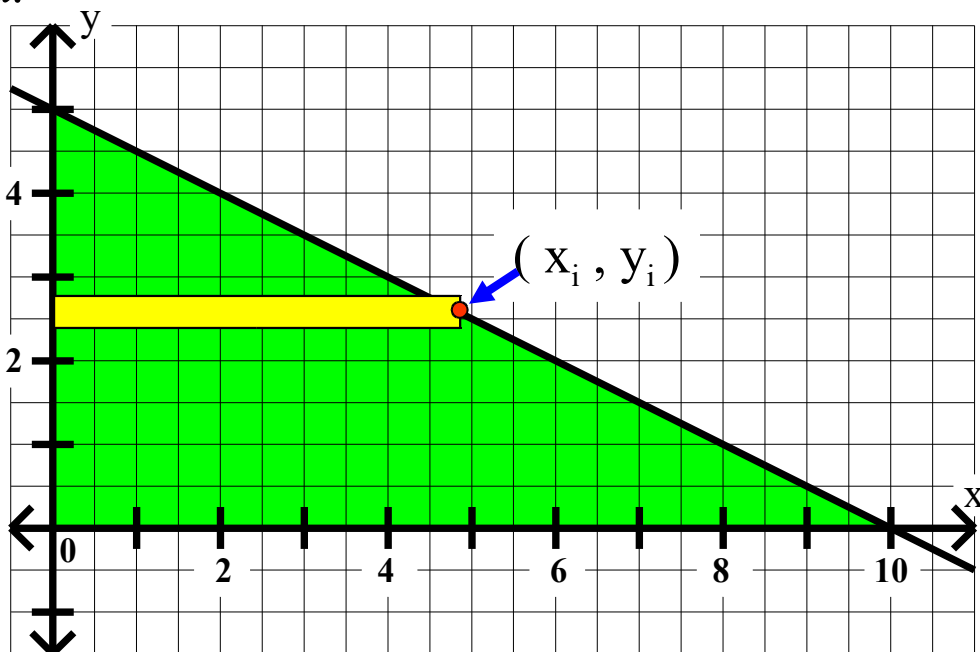
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c. $V = \pi \int_0^5 (-2y + 10)^2 dy$

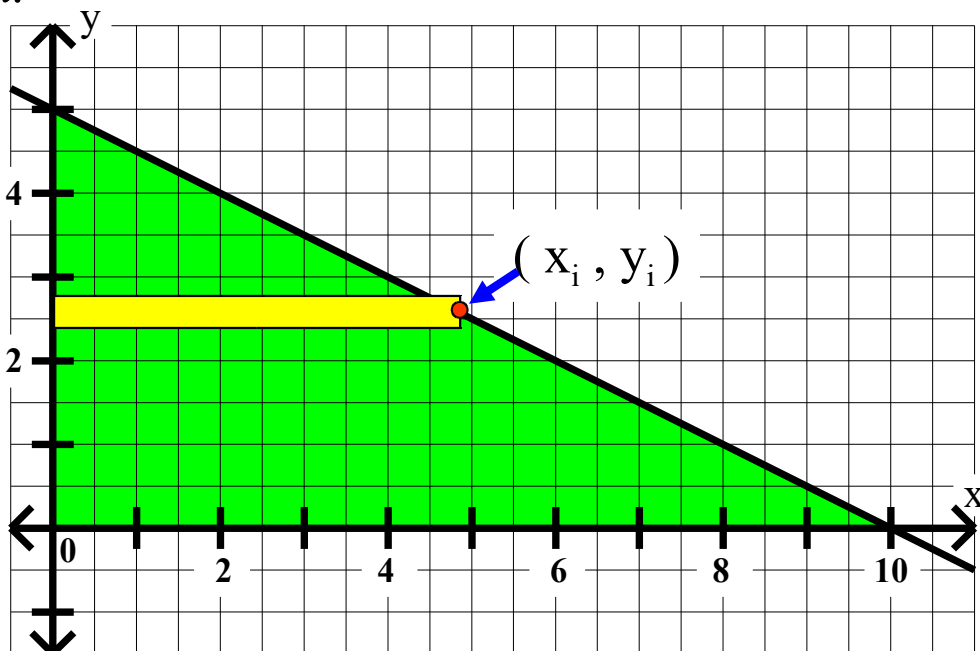
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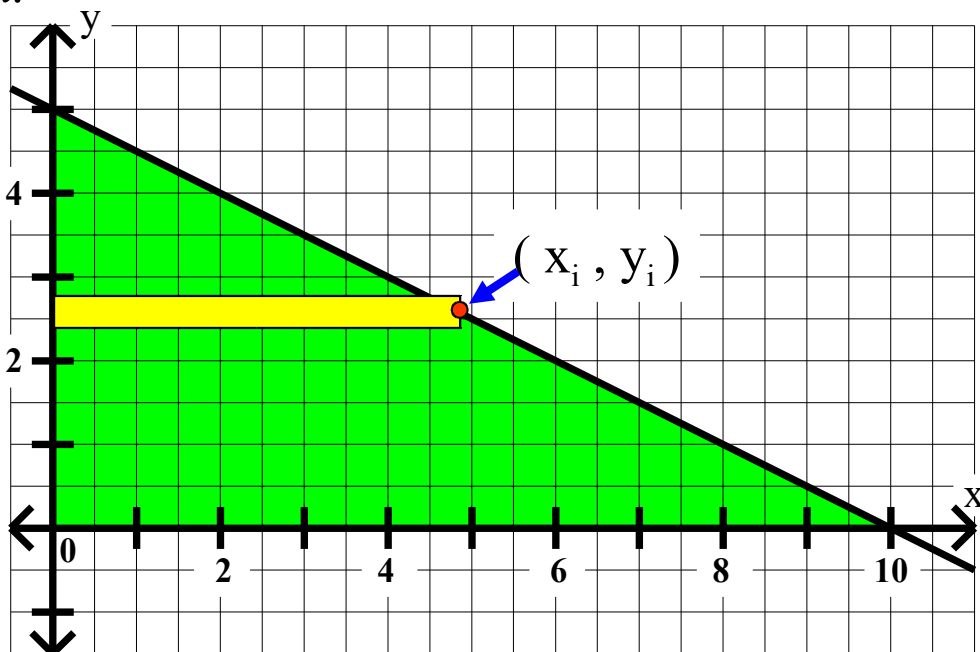
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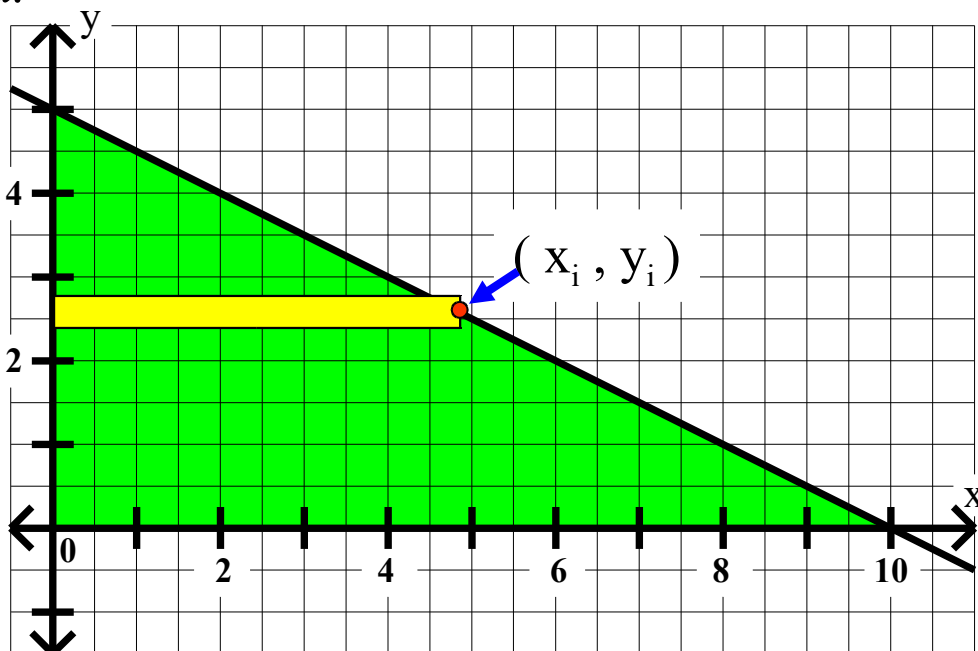
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c. $V = \pi \int_0^5 (-2y + 10)^2 dy$

d. $V \approx$

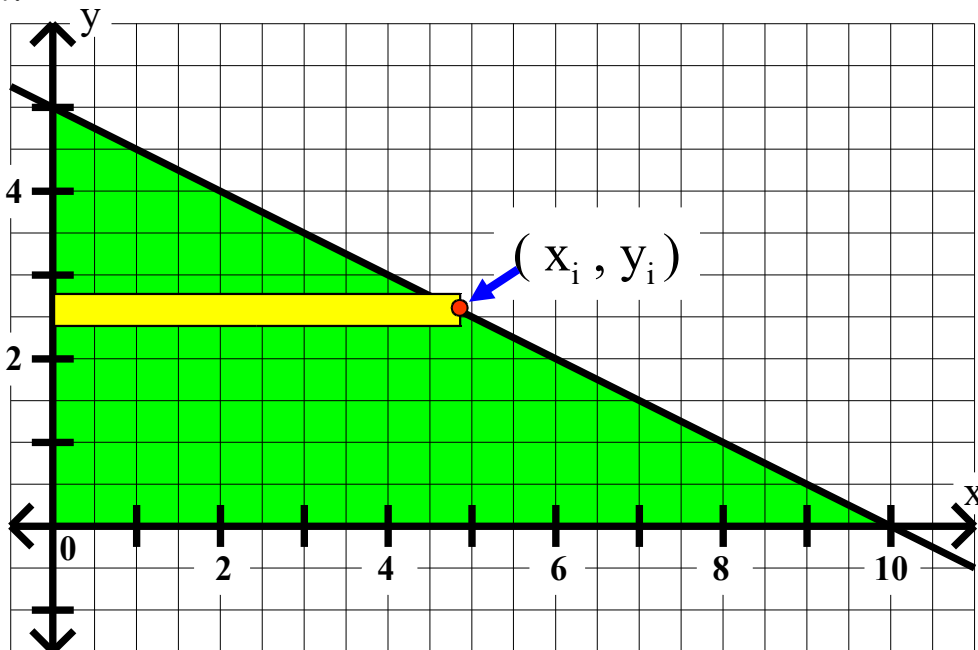
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b. $V_i = \pi(-2y_i + 10)^2 \Delta y$

c. $V = \pi \int_0^5 (-2y + 10)^2 dy$

d. $V \approx 524$ cu. units

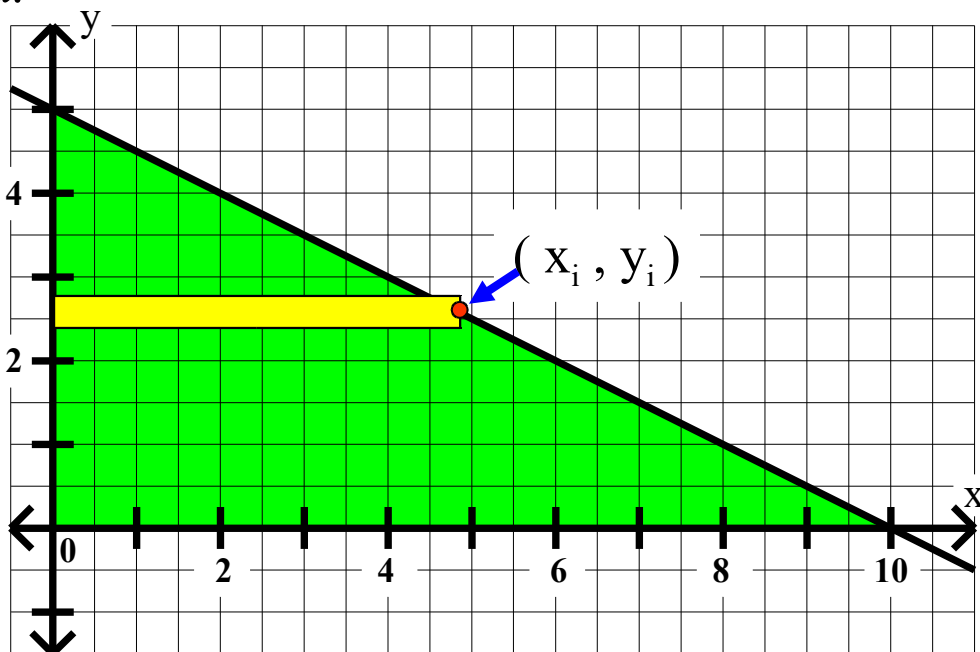
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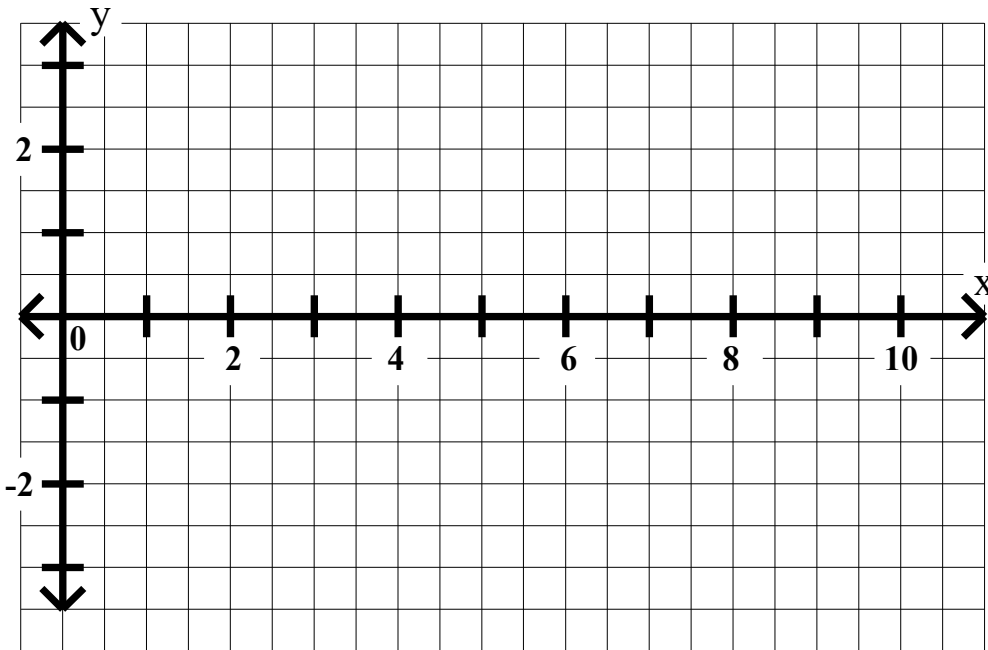
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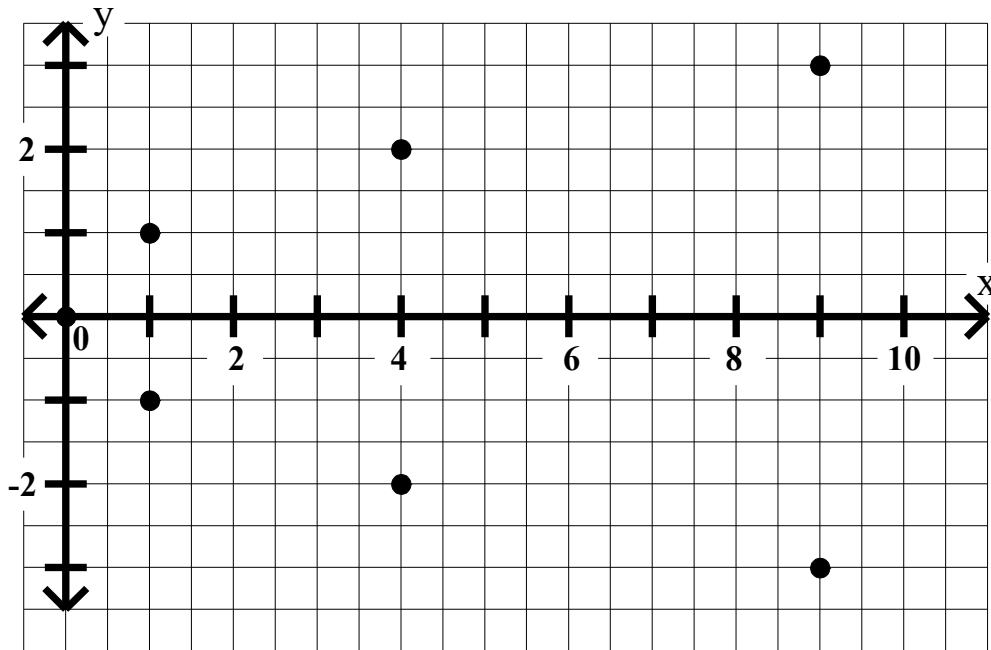
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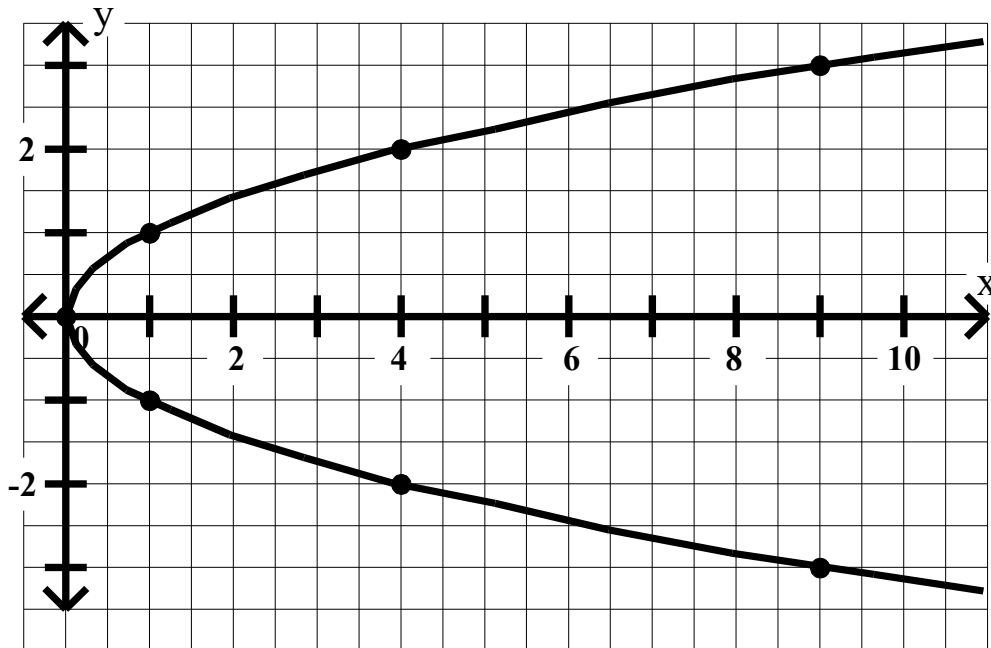
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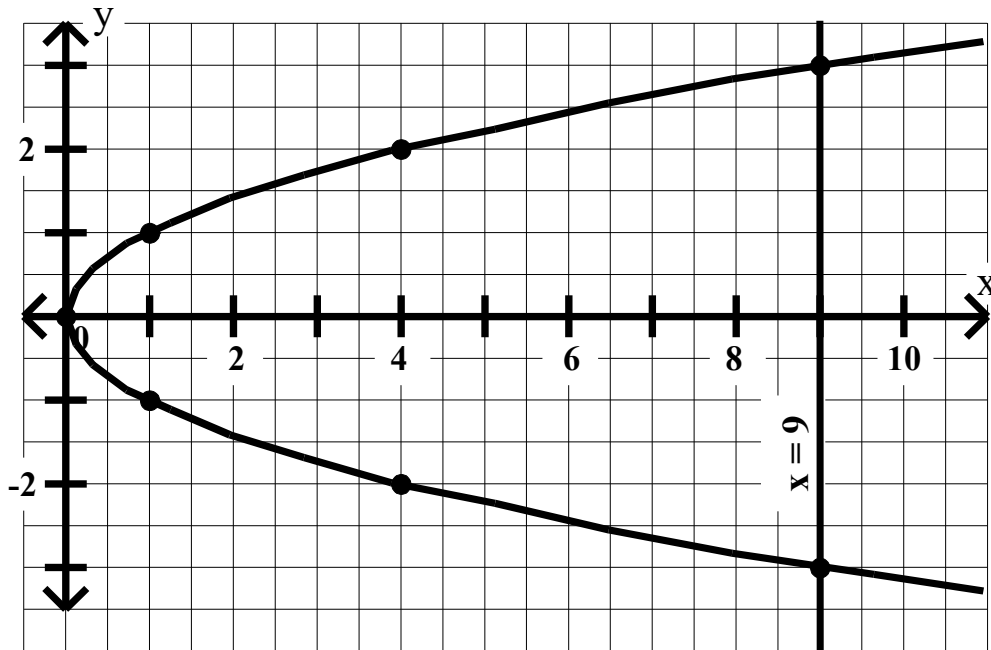
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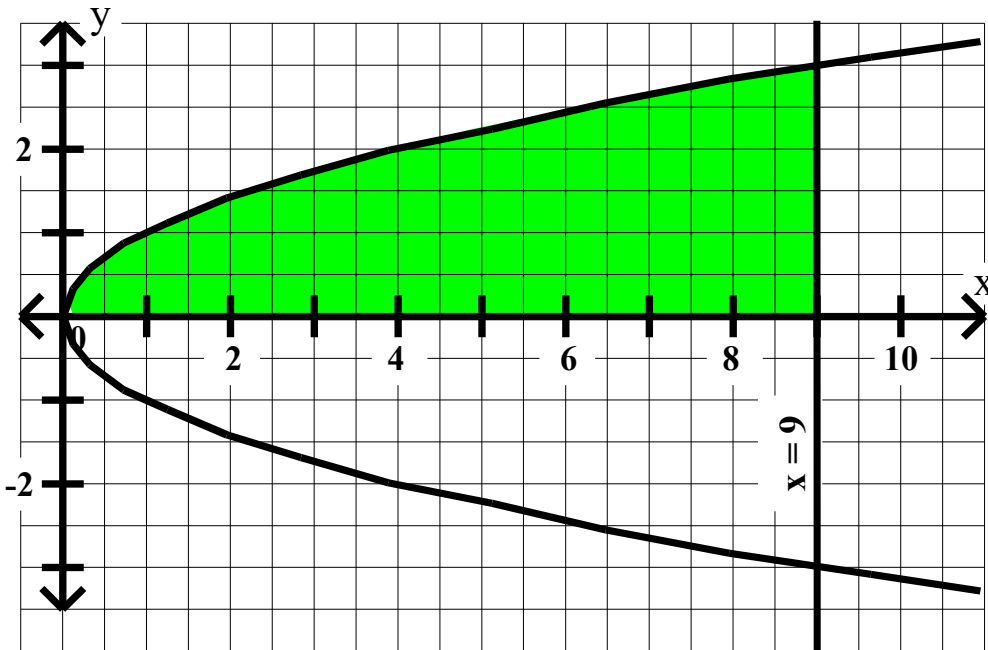
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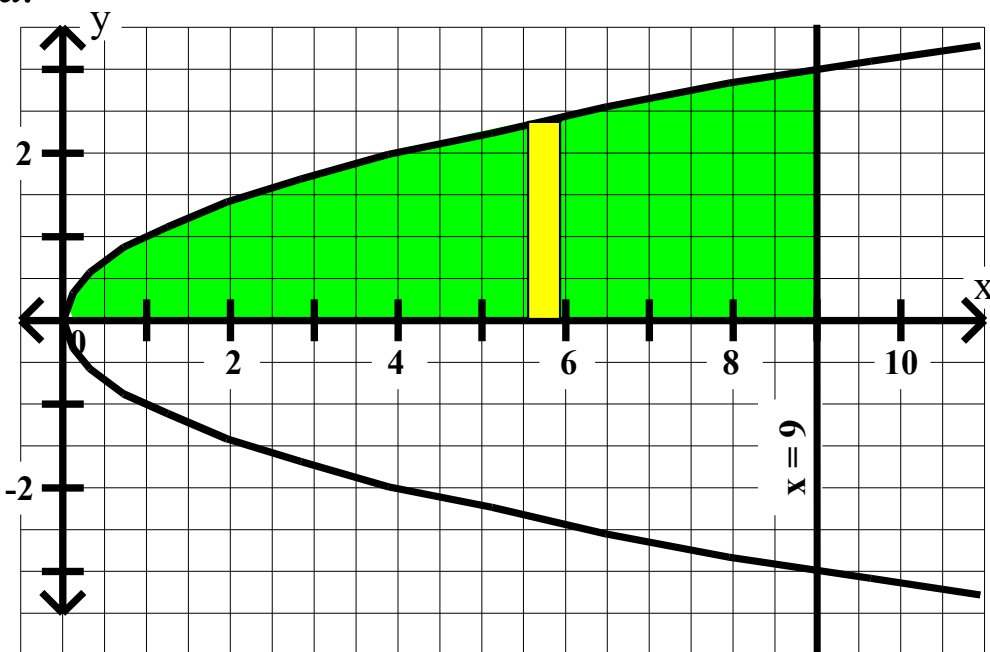
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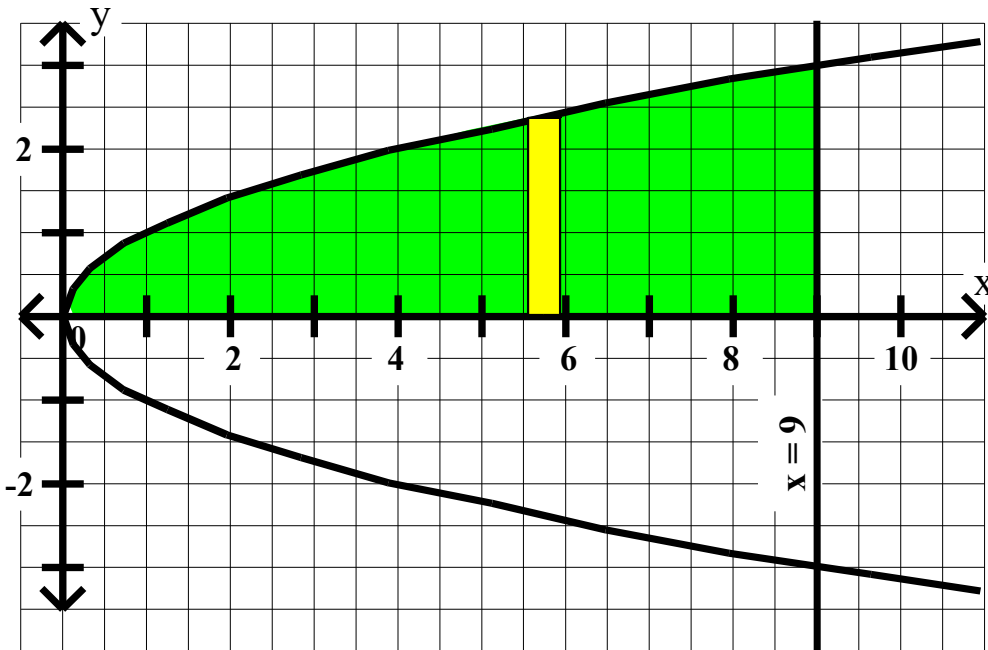
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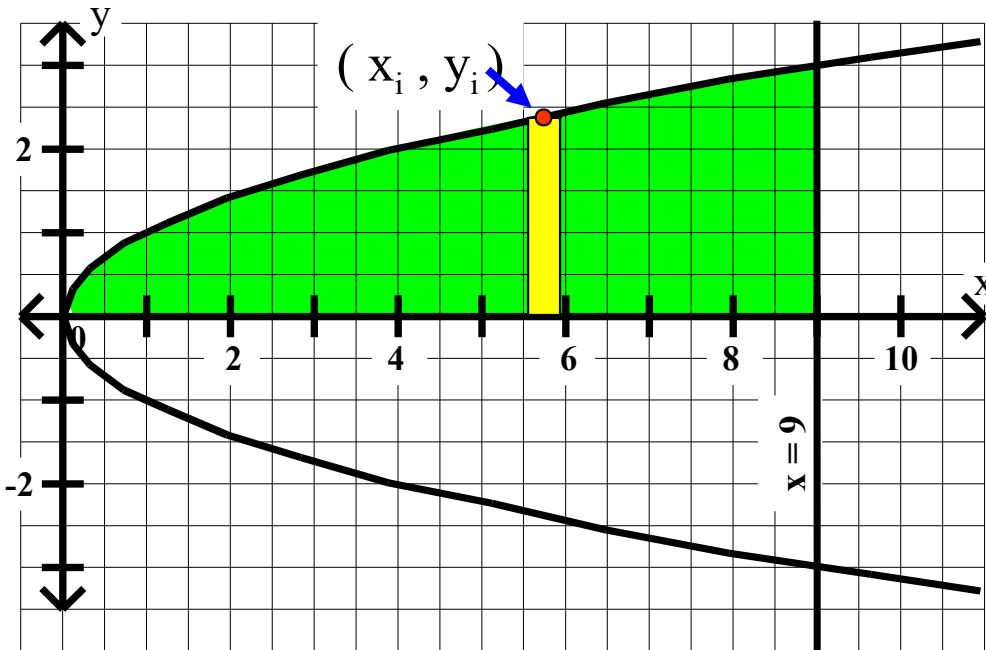
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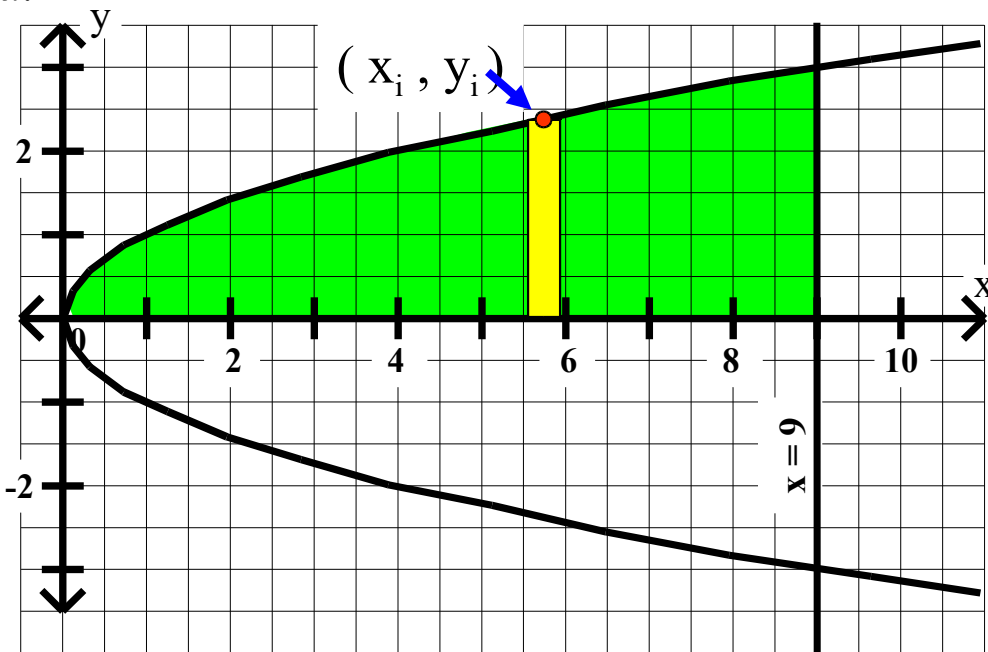
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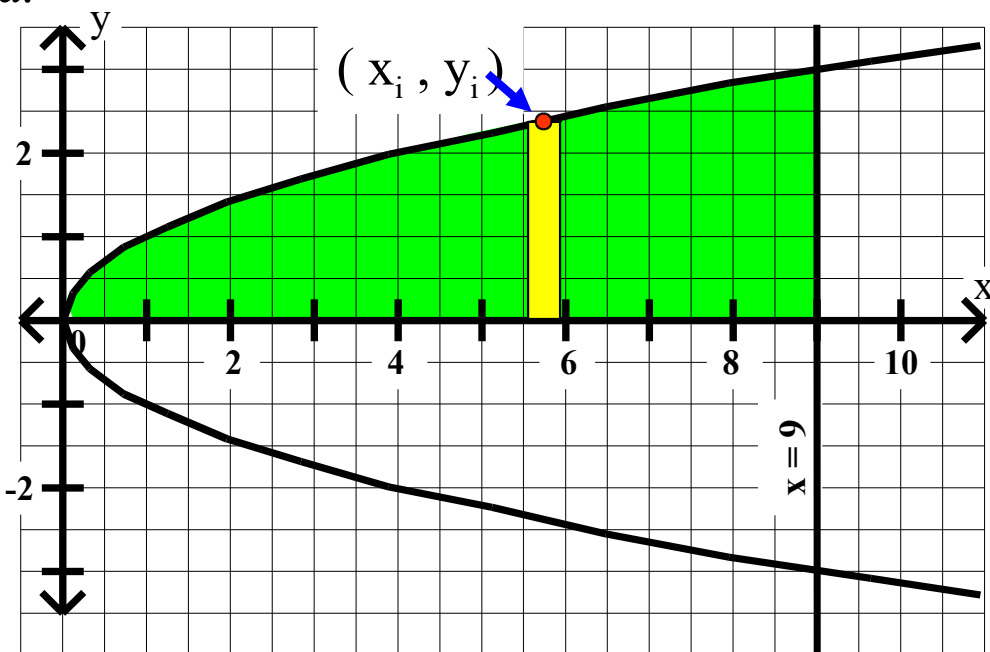
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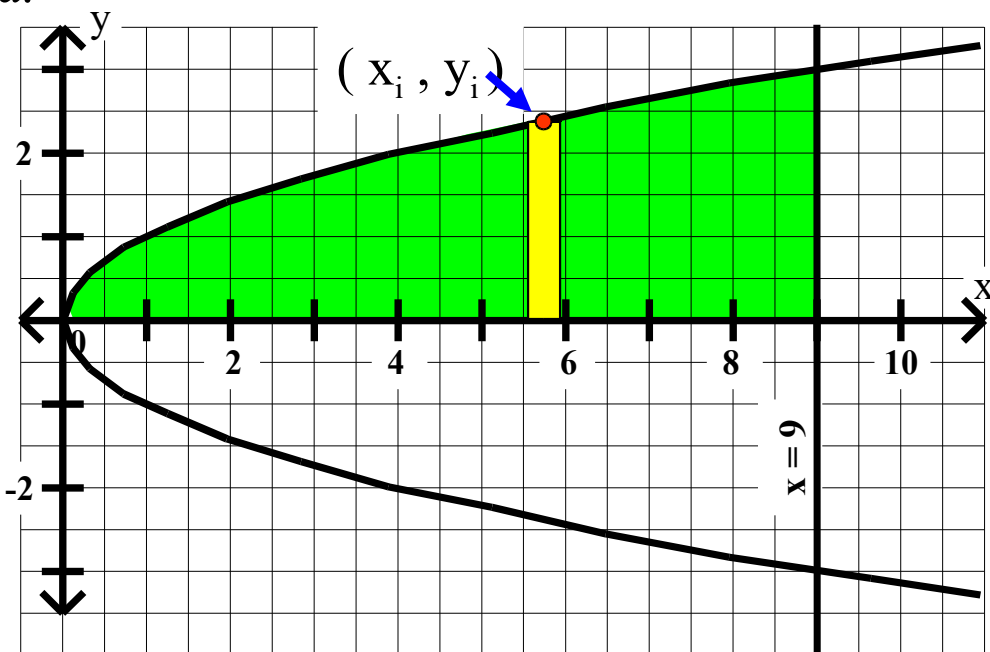
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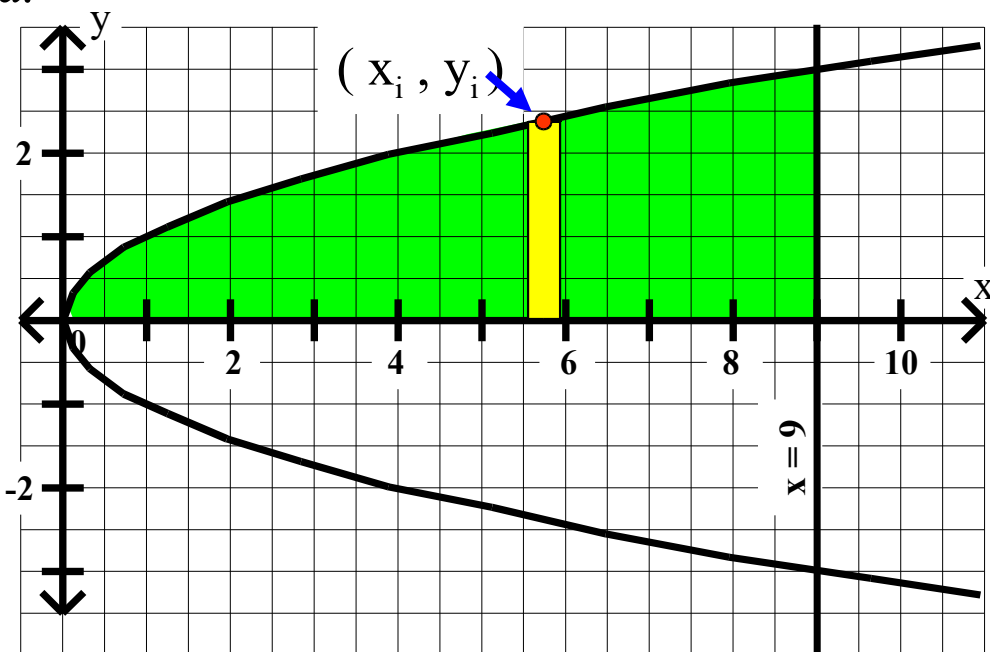
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Sample 2a. The region in the first quadrant bounded by $x = y^2$, the x-axis, and the line $x = 9$ is rotated about the x-axis.

a.



Disks: $V = \pi r^2 h$

$$r = y_i = \sqrt{x_i}$$

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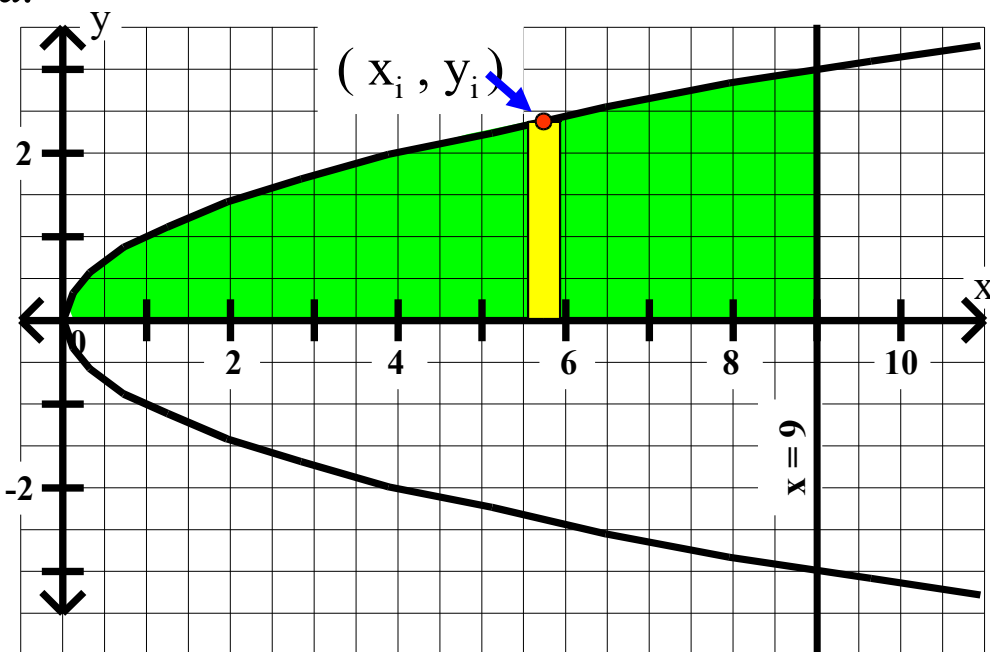
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b. $V_i =$

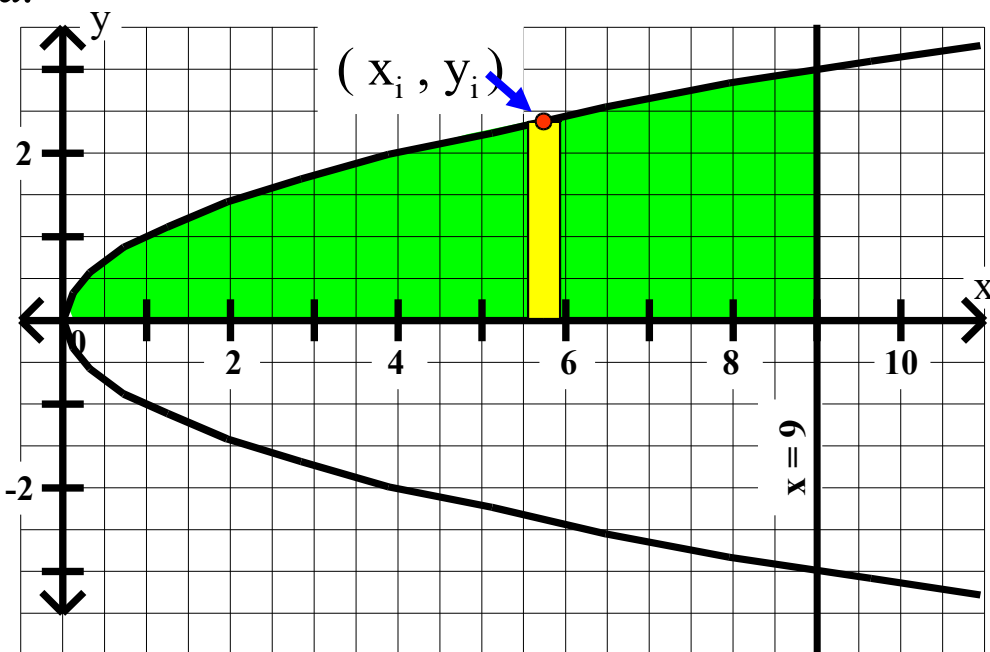
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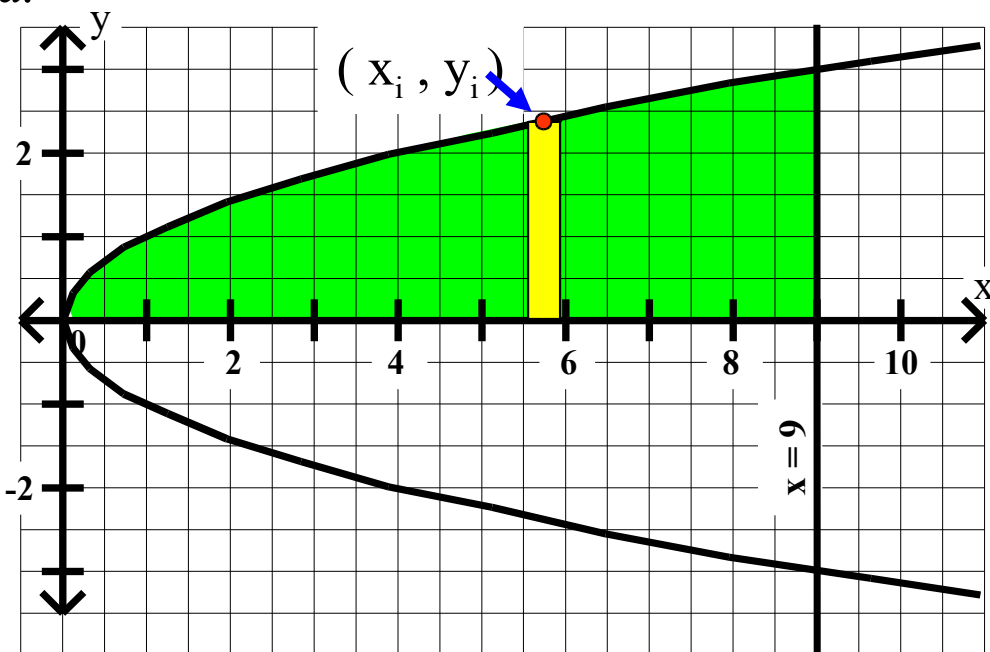
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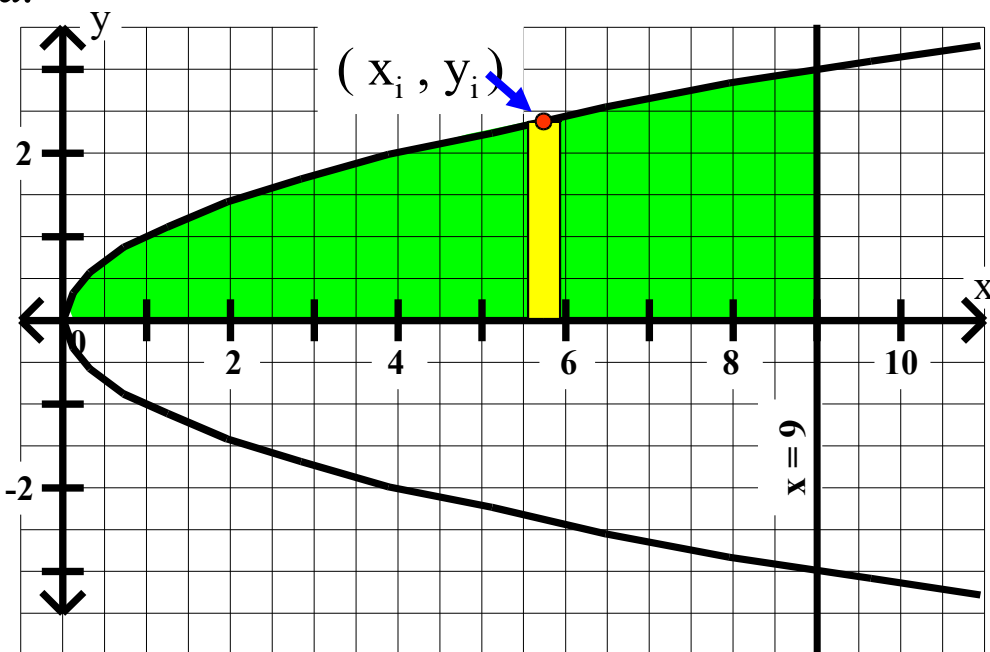
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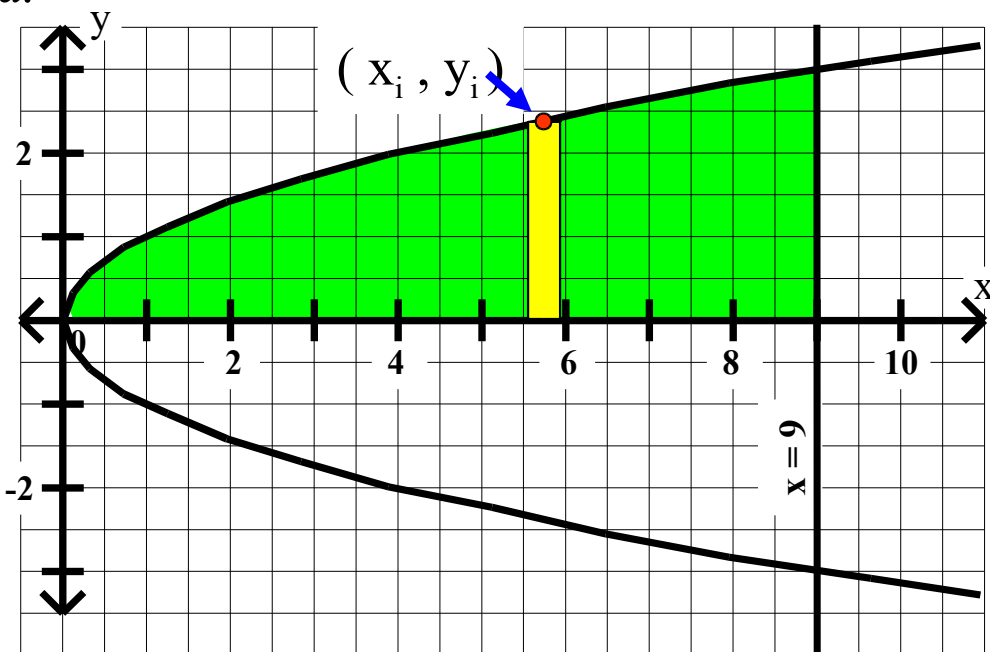
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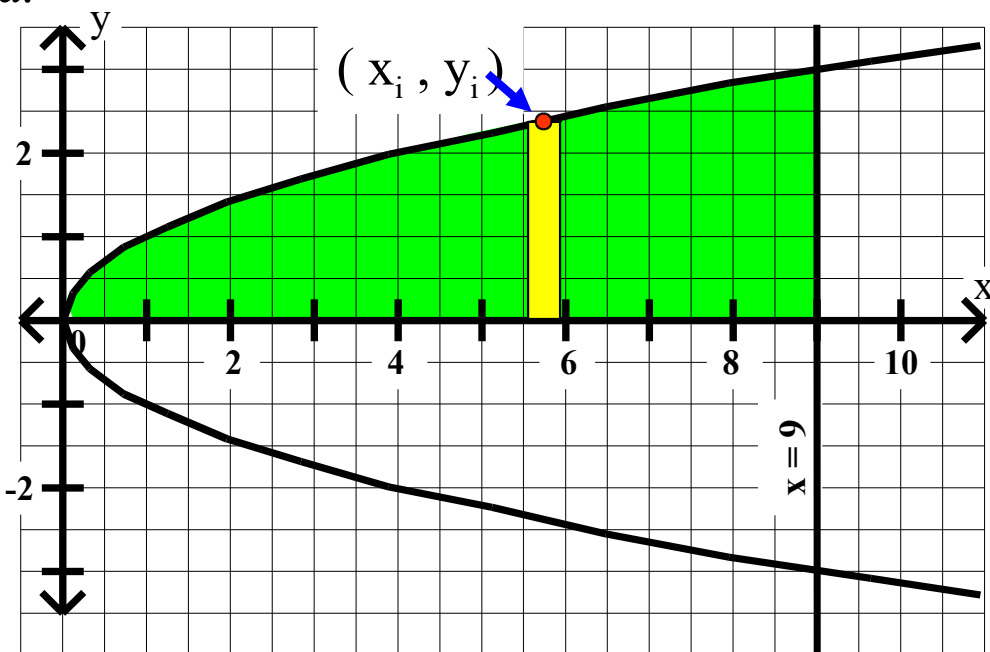
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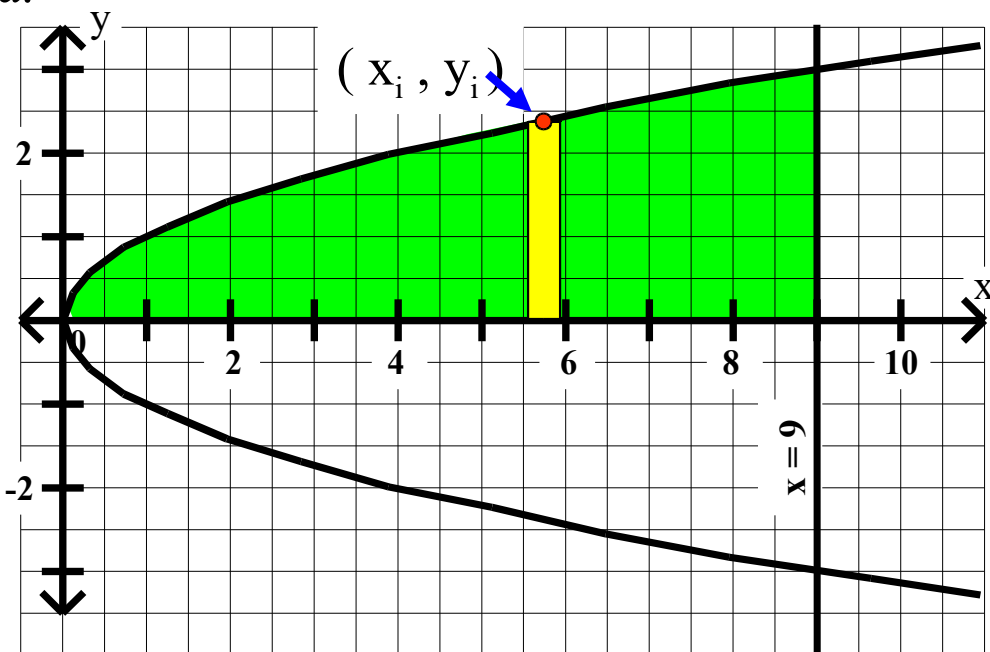
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b. $V_i = \pi(\sqrt{x_i})^2 \Delta x$

c. $V =$

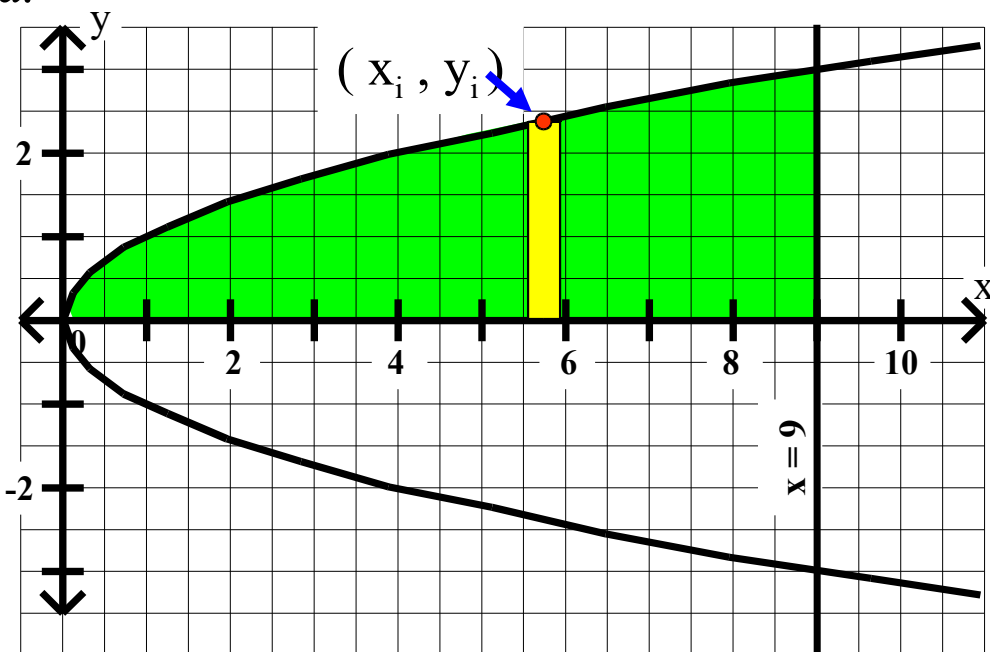
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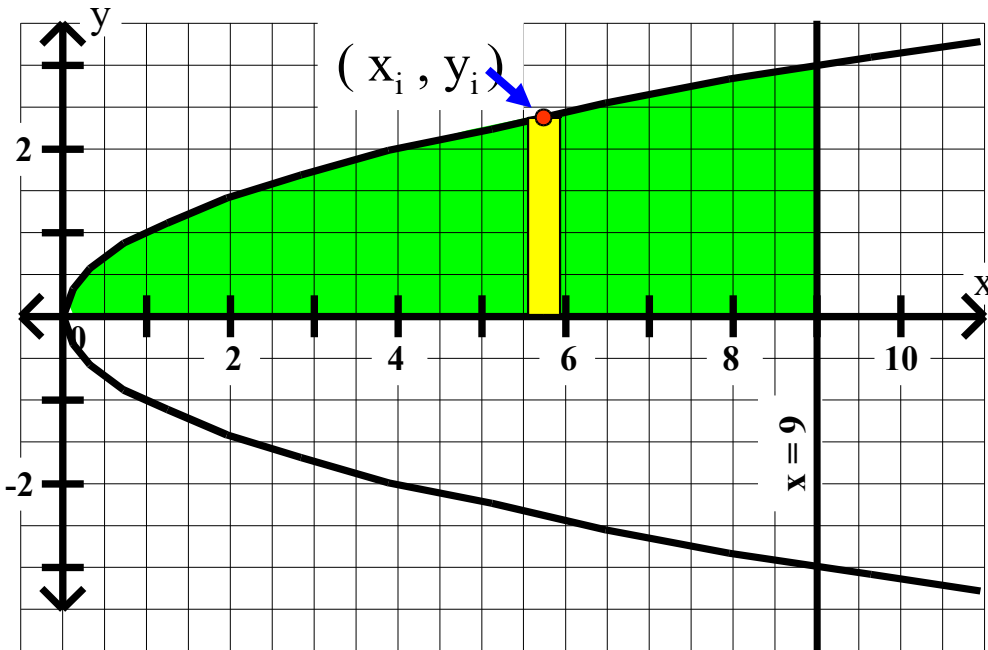
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b. $V_i = \pi(\sqrt{x_i})^2 \Delta x$

c. $V = \pi \int$

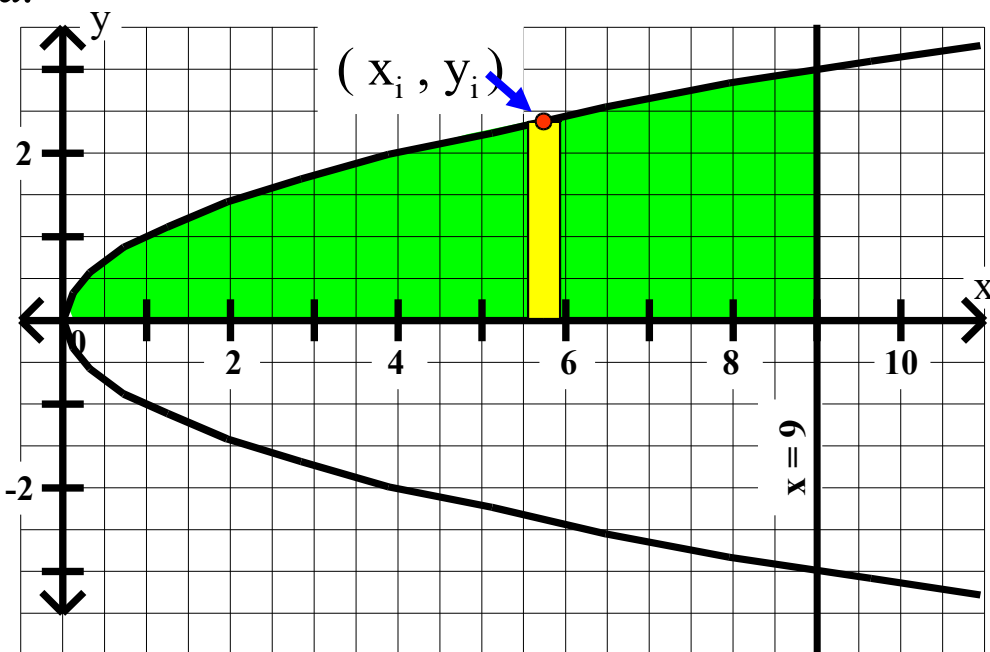
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c. $V = \pi \int x \, dx$

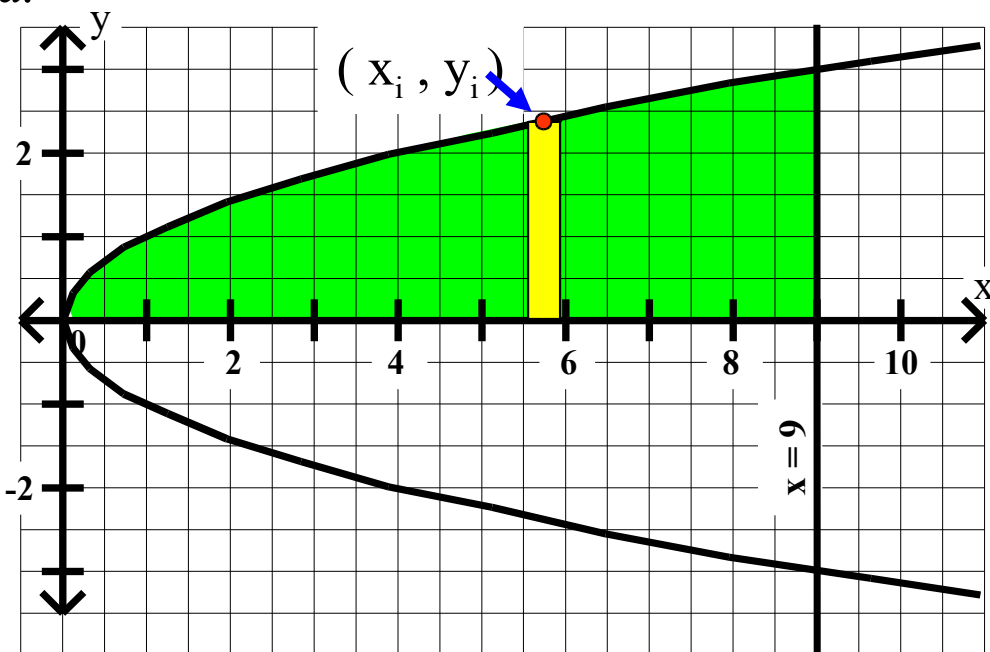
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c. $V = \pi \int_0^9 x \, dx$

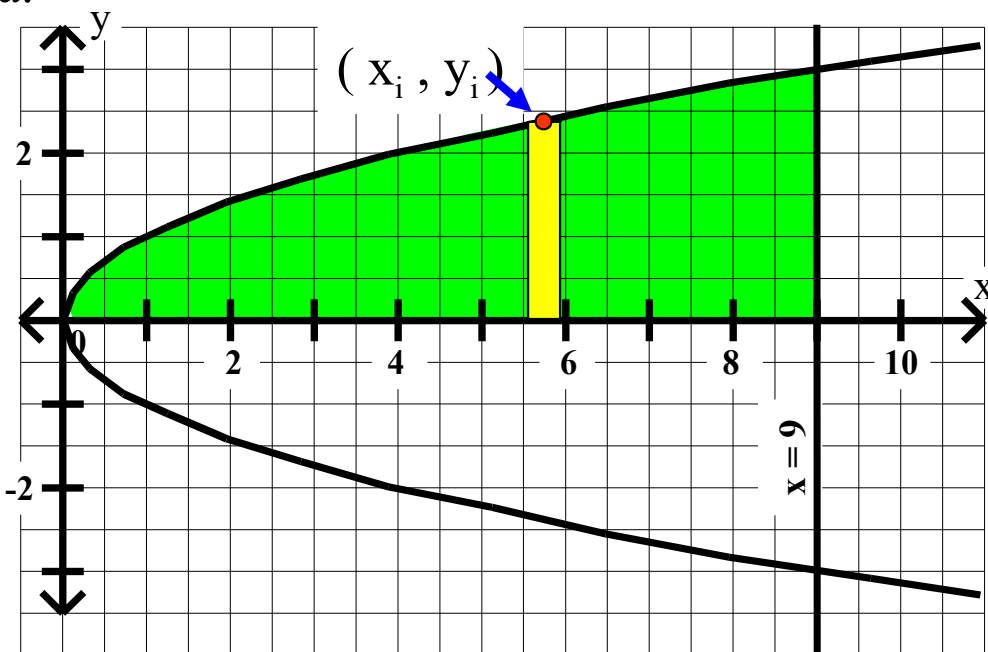
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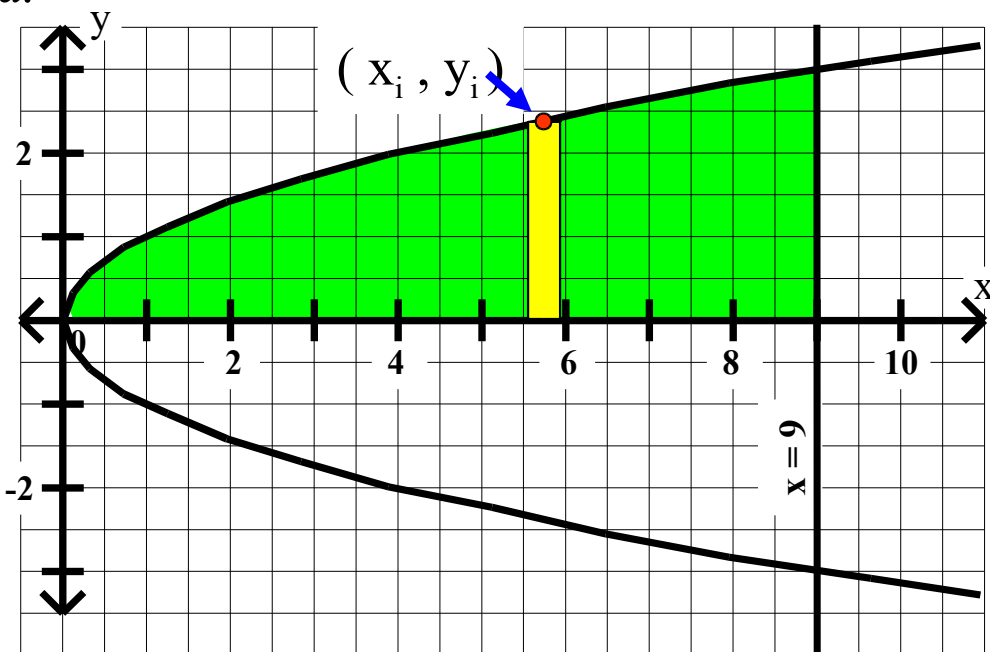
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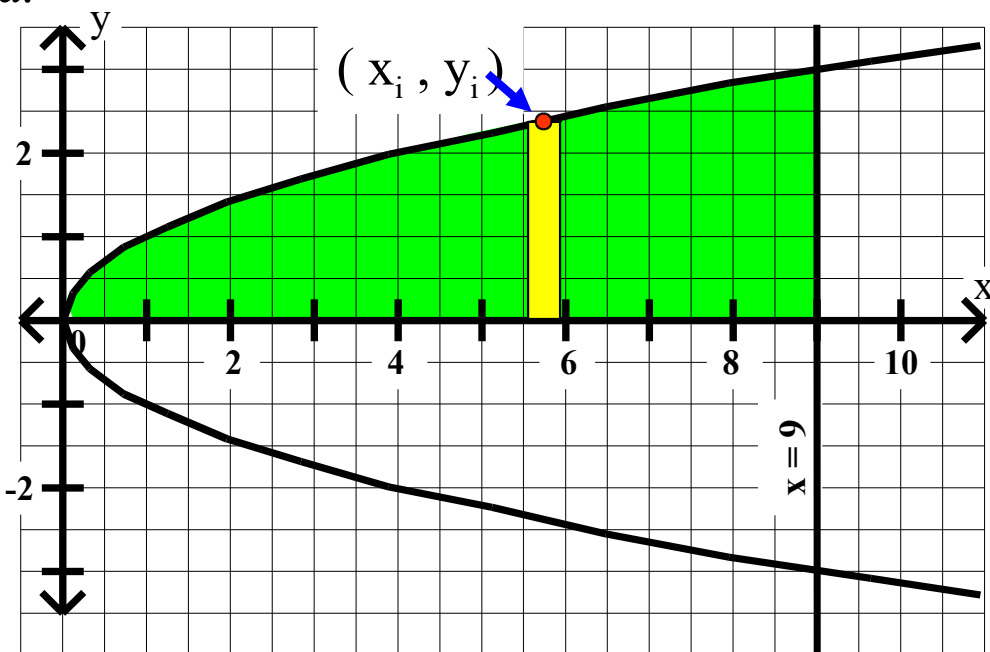
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b. $V_i = \pi(\sqrt{x_i})^2 \Delta x$

c. $V = \pi \int_0^9 x \, dx$

d. $V \approx$

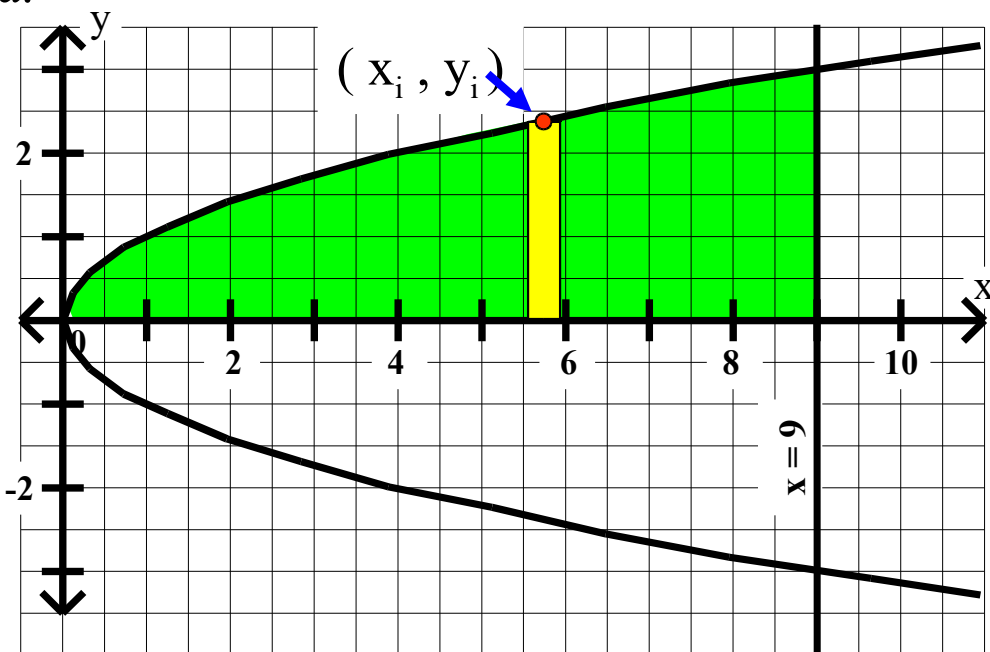
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b. $V_i = \pi(\sqrt{x_i})^2 \Delta x$

c. $V = \pi \int_0^9 x \, dx$

d. $V \approx 127$ cu. units

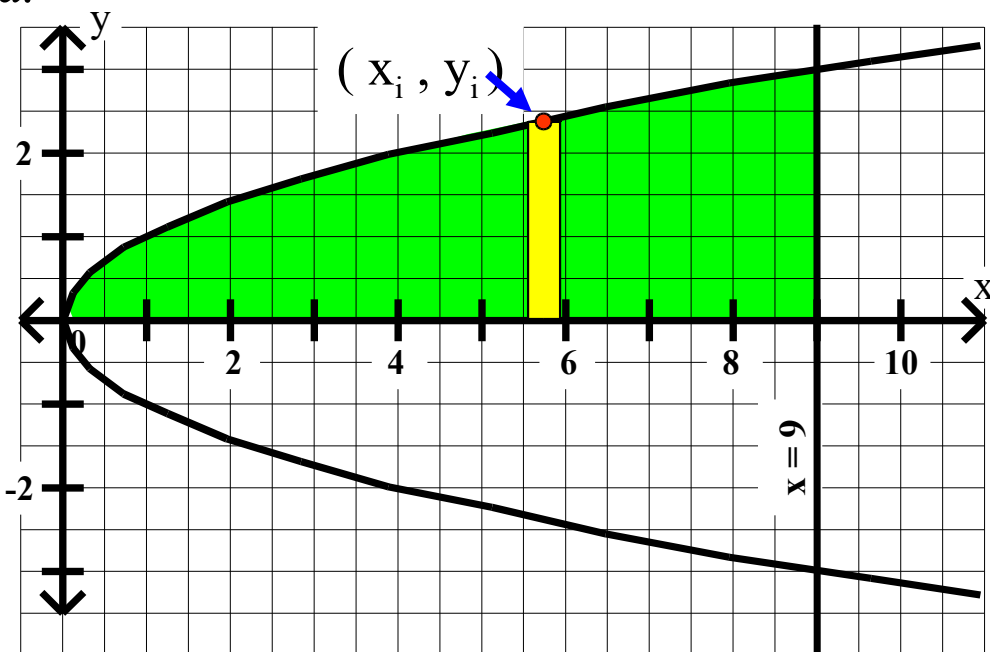
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Sample 2b. The region in the first quadrant bounded by $x = y^2$, the x-axis, and the line $x = 9$ is rotated about the line $x = 9$.

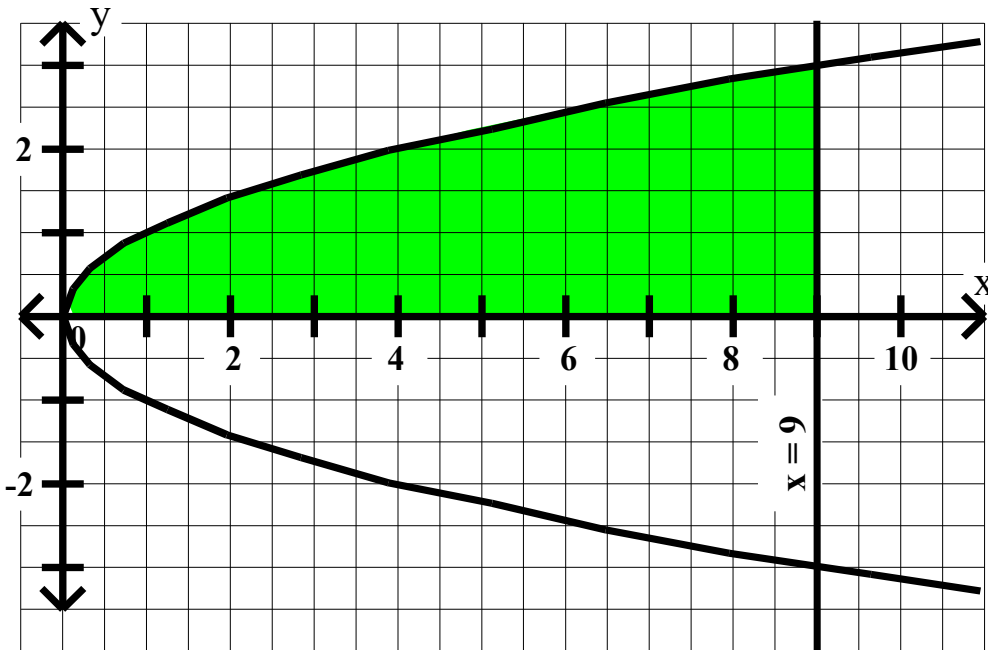
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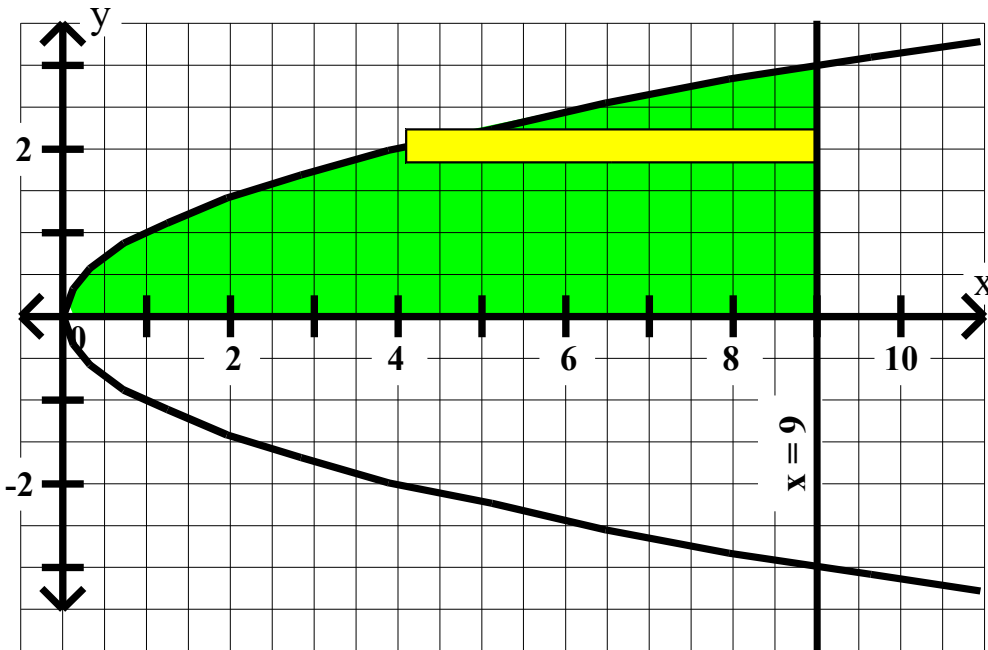
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a.



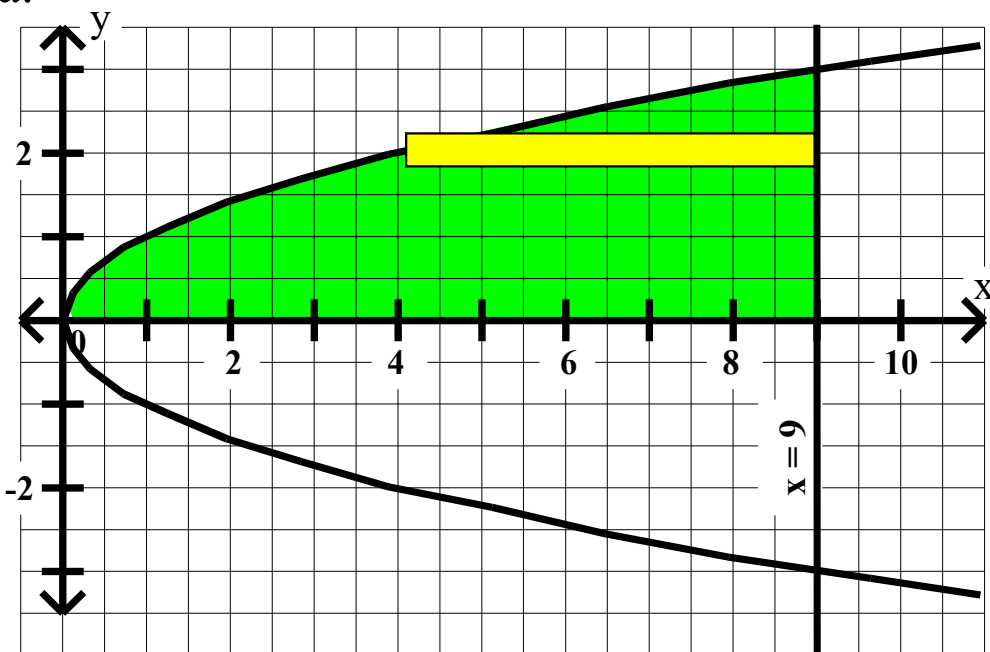
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a.



Disks: $V = \pi r^2 h$

$r =$

$h =$

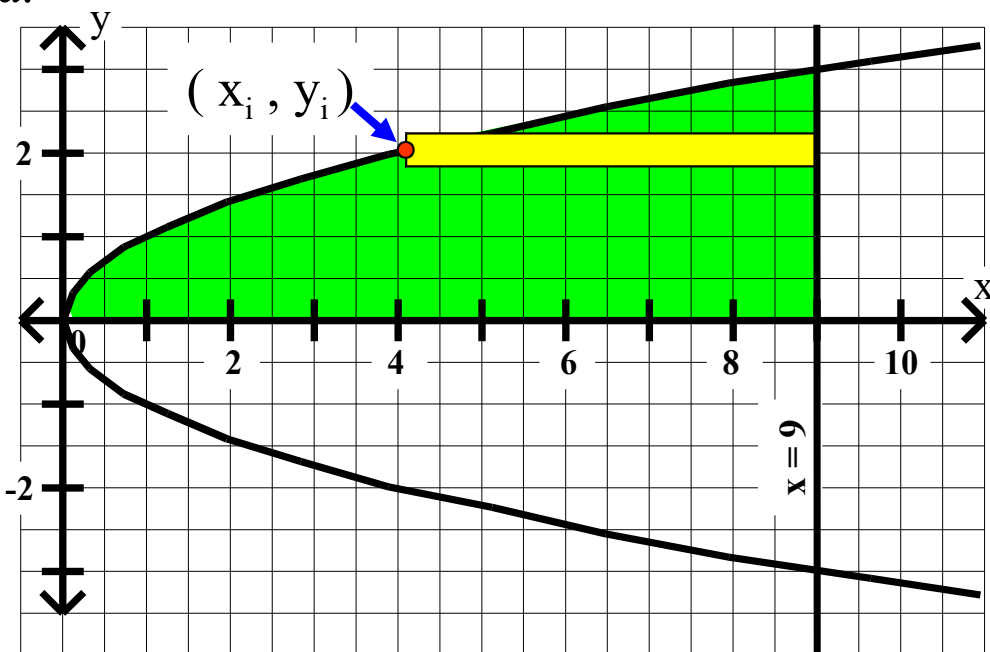
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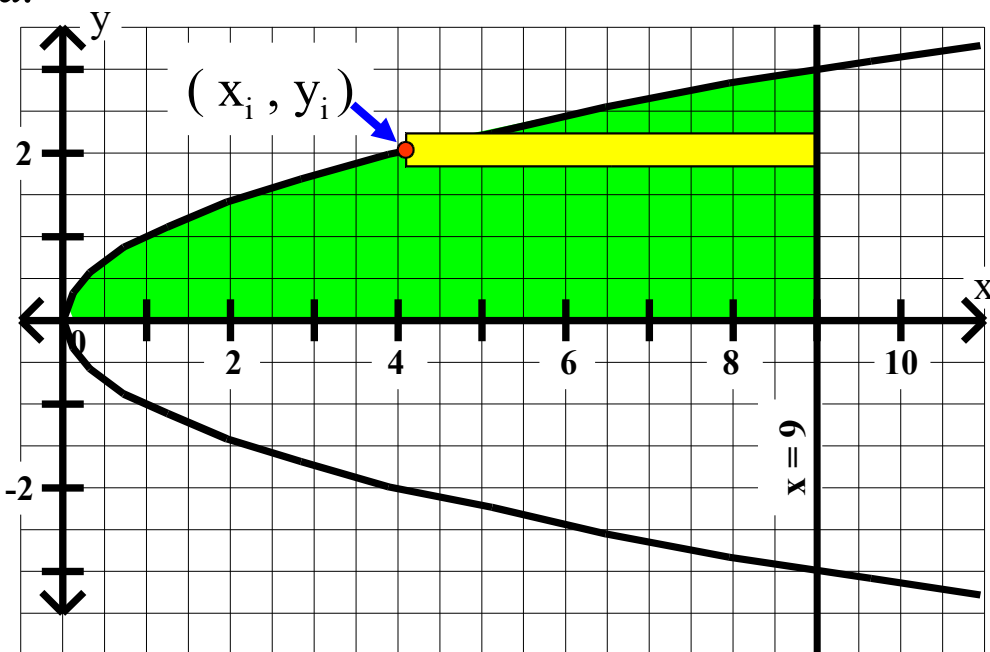
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a.



Disks: $V = \pi r^2 h$

$$r = 9 - x_i$$

$$h =$$

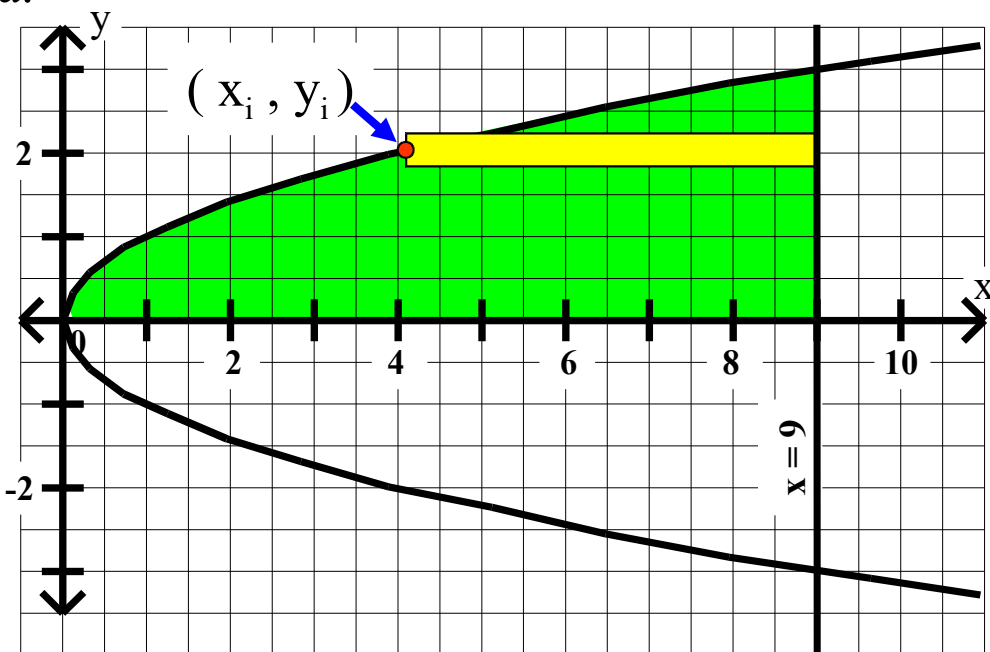
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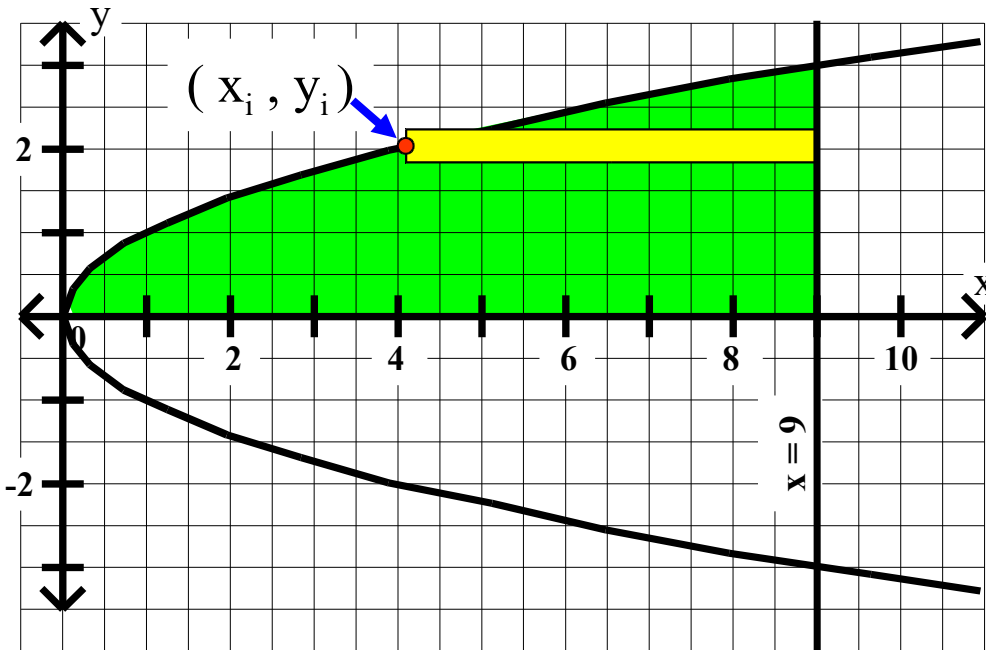
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$$\text{Disks: } V = \pi r^2 h$$

$$r = 9 - x_i = 9 -$$

$$h = \Delta y$$

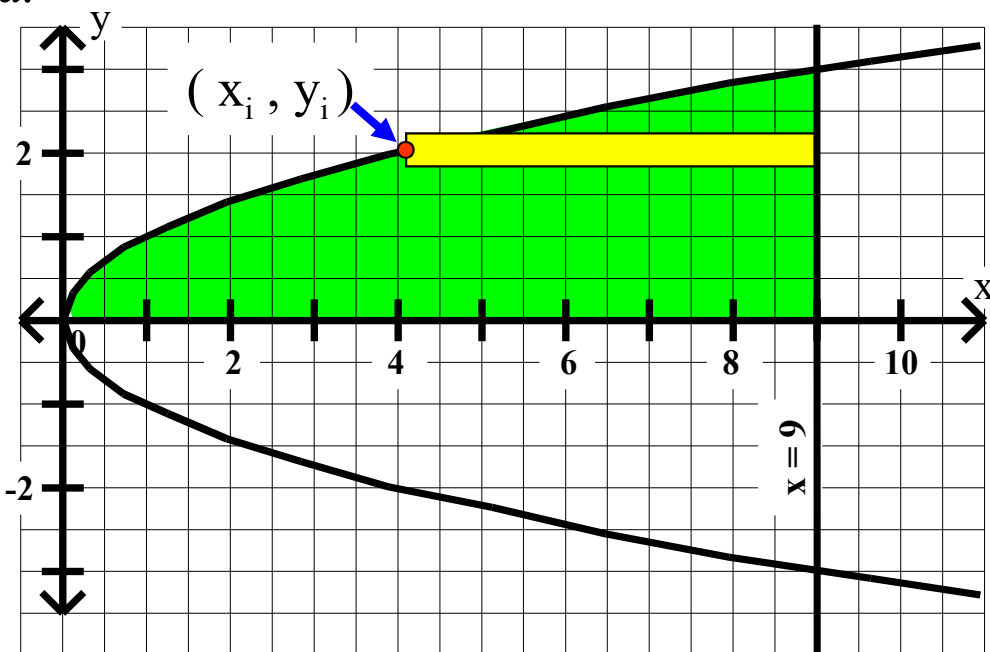
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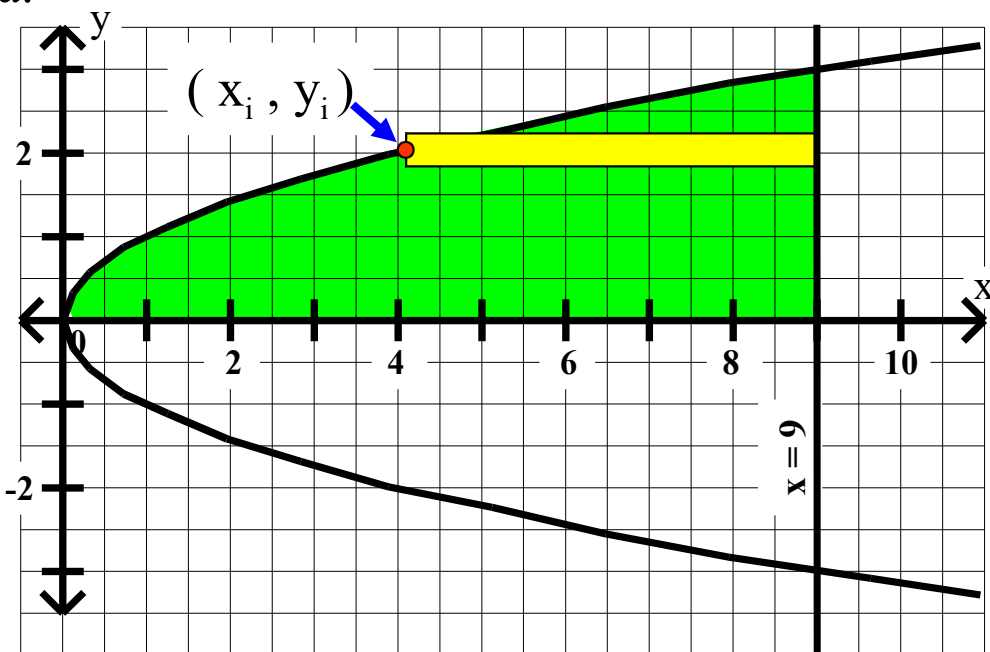
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$$r = 9 - x_i = 9 - y_i^2$$

$$h = \Delta y$$

b. $V_i =$

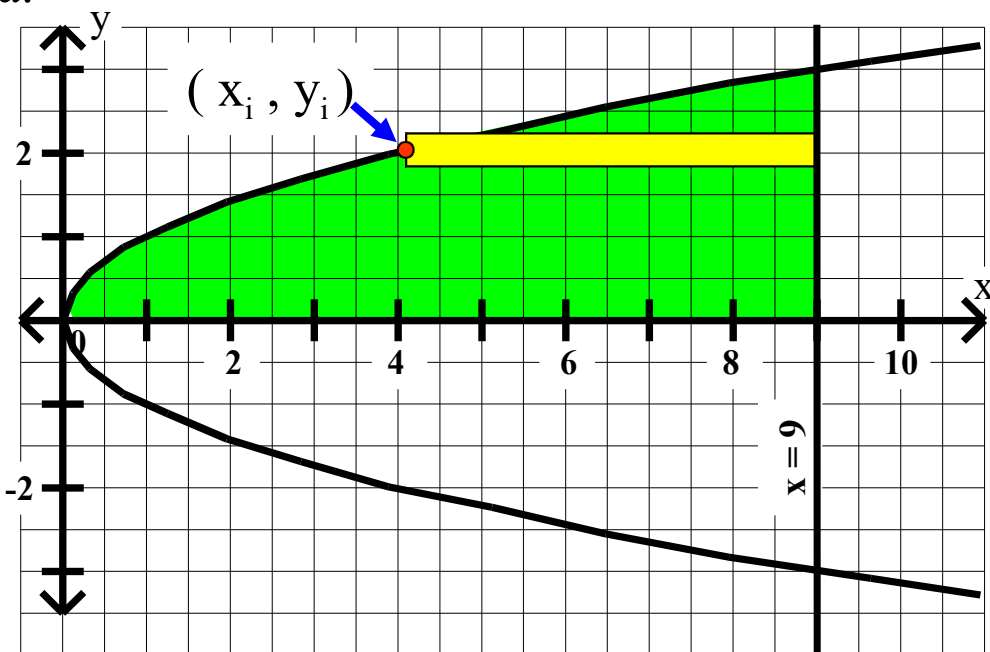
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$$h = \Delta y$$

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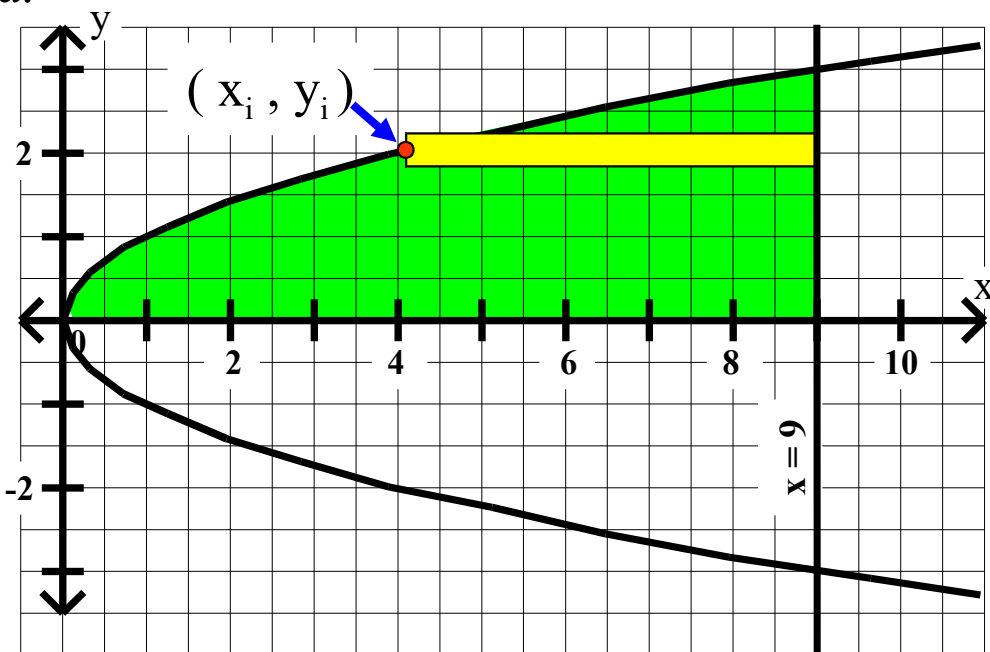
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a.



Disks: $V = \pi r^2 h$

$$r = 9 - x_i = 9 - y_i^2$$

$$h = \Delta y$$

$$b. \quad V_i = \pi(9 - y_i^2)$$

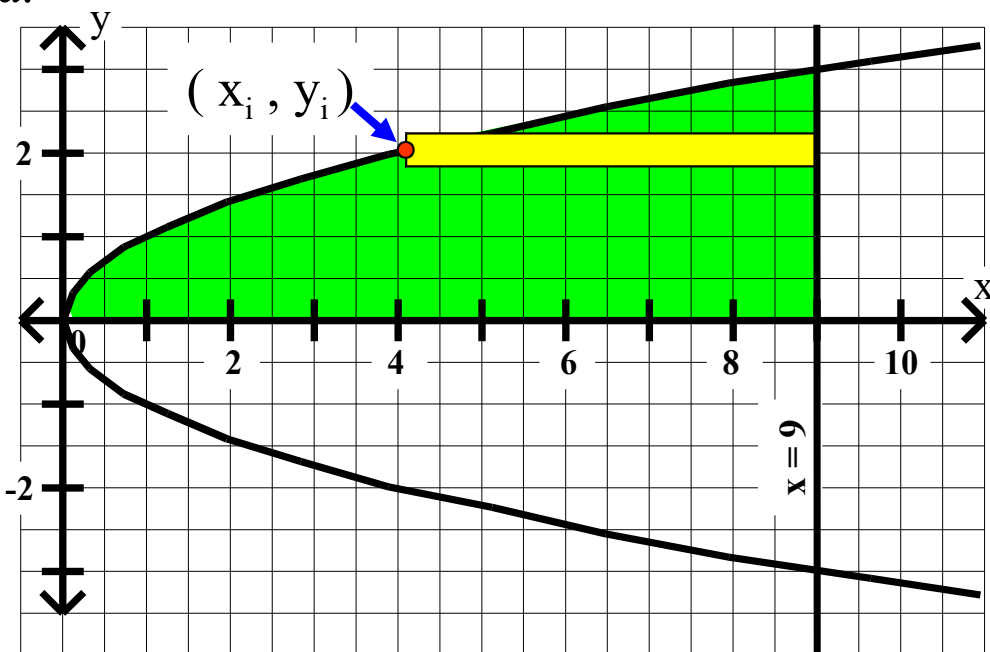
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$$r = 9 - x_i = 9 - y_i^2$$

$$h = \Delta y$$

$$b. \quad V_i = \pi(9 - y_i^2)^2$$

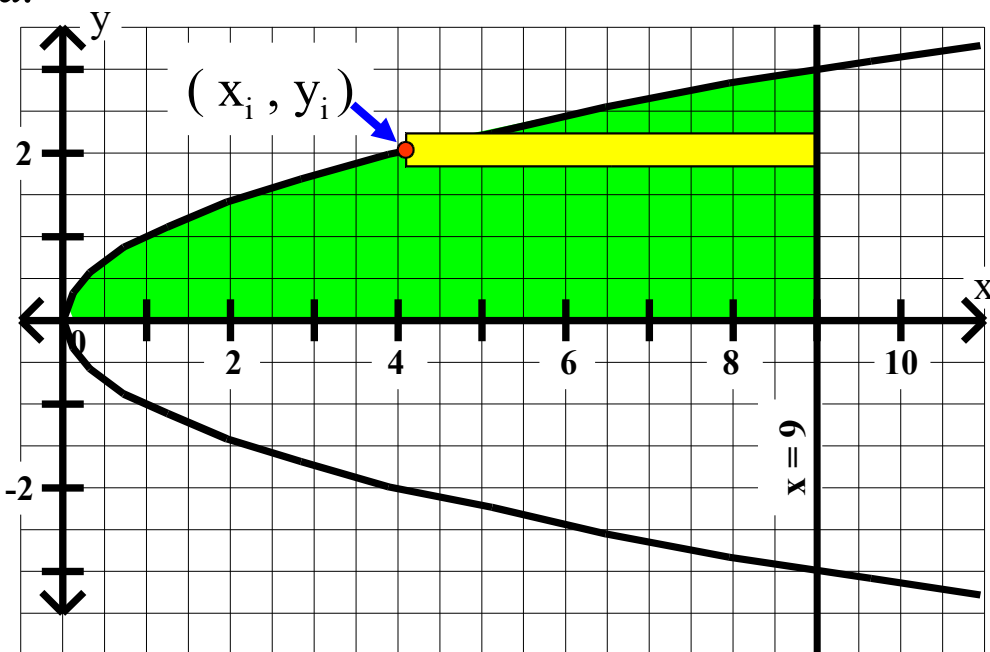
Calculus Class Worksheet #1 Unit 11 Solutions

Use “disks” to find the volume generated by rotating the given region about the given line. For each problem, you must

- sketch the generating region, showing a typical generating rectangle,
- write an expression for the volume generated by this rectangle,
- express the exact volume of the solid as a definite integral, and
- evaluate the integral.

Sample 2b. The region in the first quadrant bounded by $x = y^2$, the x-axis, and the line $x = 9$ is rotated about the line $x = 9$.

a.



Disks: $V = \pi r^2 h$

$$r = 9 - x_i = 9 - y_i^2$$

$$h = \Delta y$$

$$b. V_i = \pi(9 - y_i^2)^2 \Delta y$$

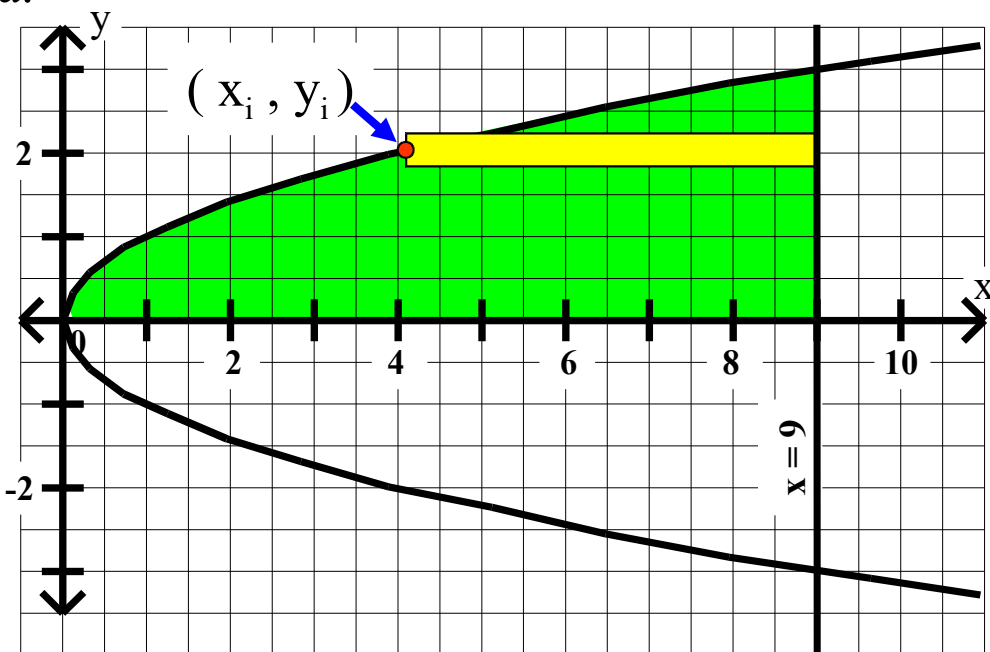
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a.



Disks: $V = \pi r^2 h$

$$r = 9 - x_i = 9 - y_i^2$$

$$h = \Delta y$$

b. $V_i = \pi(9 - y_i^2)^2 \Delta y$

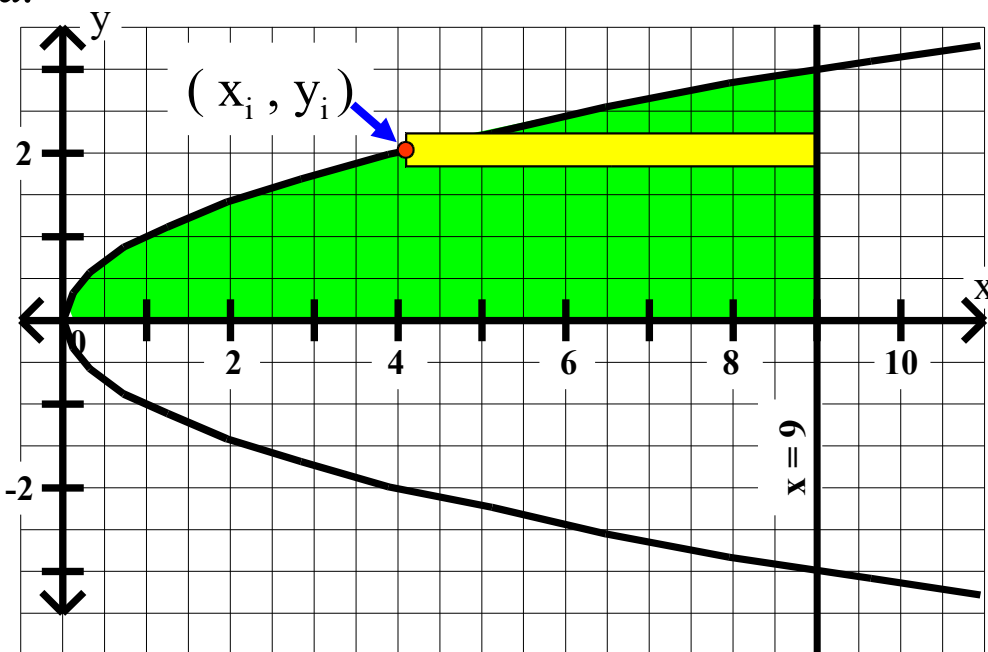
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a.



Disks: $V = \pi r^2 h$

$$r = 9 - x_i = 9 - y_i^2$$

$$h = \Delta y$$

b. $V_i = \pi(9 - y_i^2)^2 \Delta y$

c. $V =$

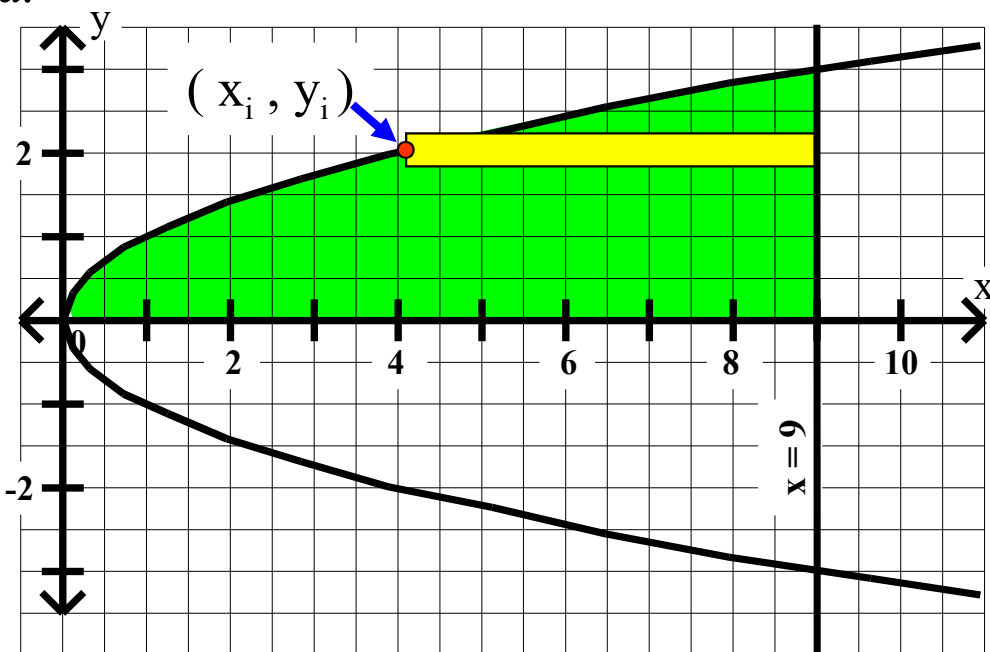
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a.



Disks: $V = \pi r^2 h$

$$r = 9 - x_i = 9 - y_i^2$$

$$h = \Delta y$$

b. $V_i = \pi(9 - y_i^2)^2 \Delta y$

c. $V = \pi$

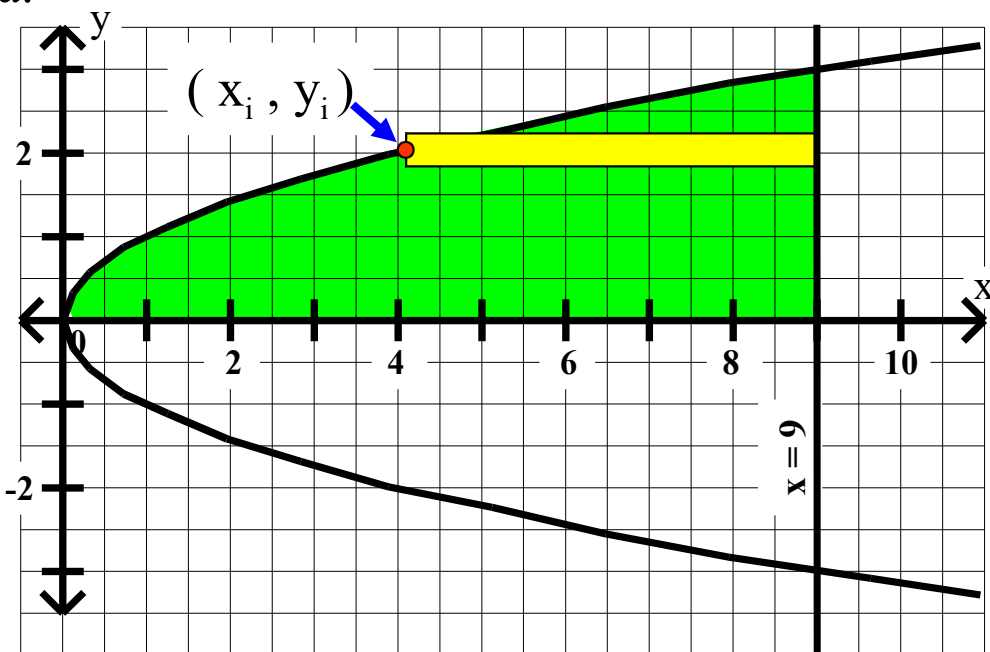
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Disks: $V = \pi r^2 h$

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$$h = \Delta y$$

b. $V_i = \pi(9 - y_i^2)^2 \Delta y$

c. $V = \pi \int$

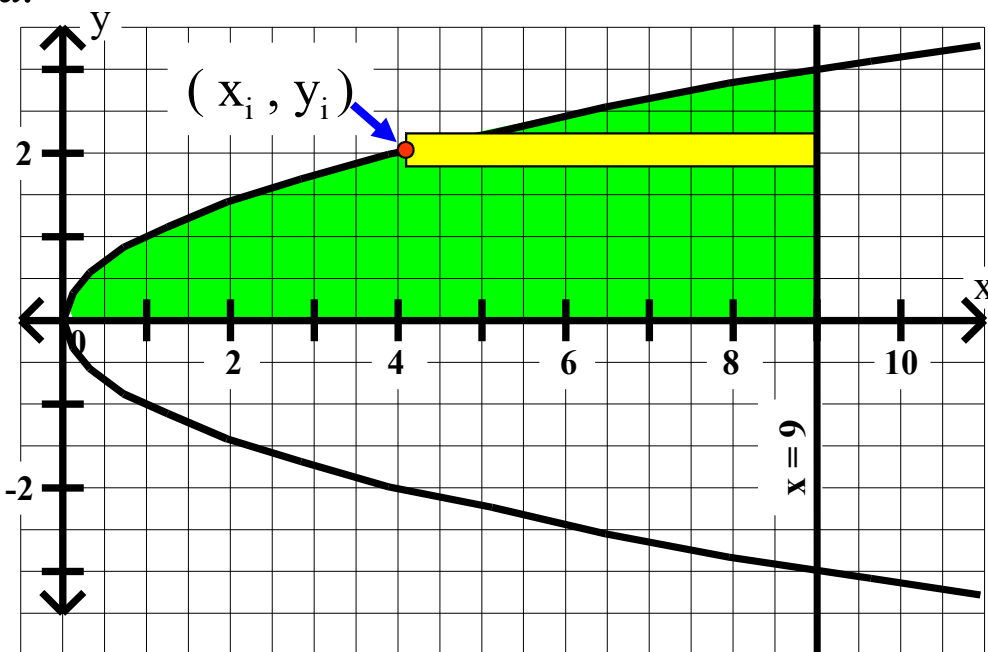
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$$h = \Delta y$$

b. $V_i = \pi(9 - y_i^2)^2 \Delta y$

c. $V = \pi \int (9 - y^2)^2 dy$

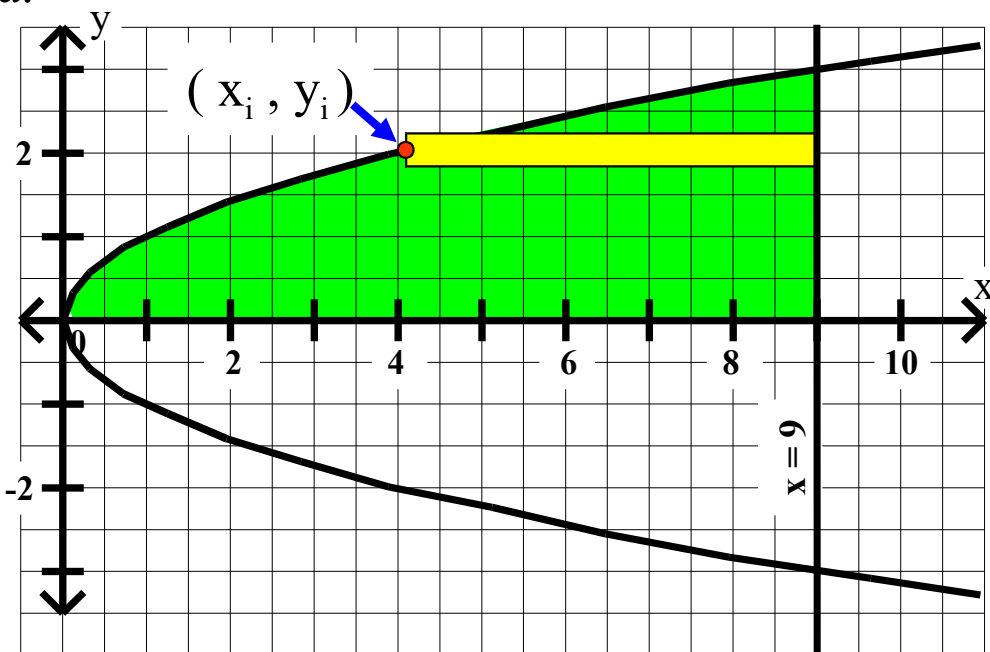
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b. $V_i = \pi(9 - y_i^2)^2 \Delta y$

c. $V = \pi \int_0^3 (9 - y^2)^2 dy$

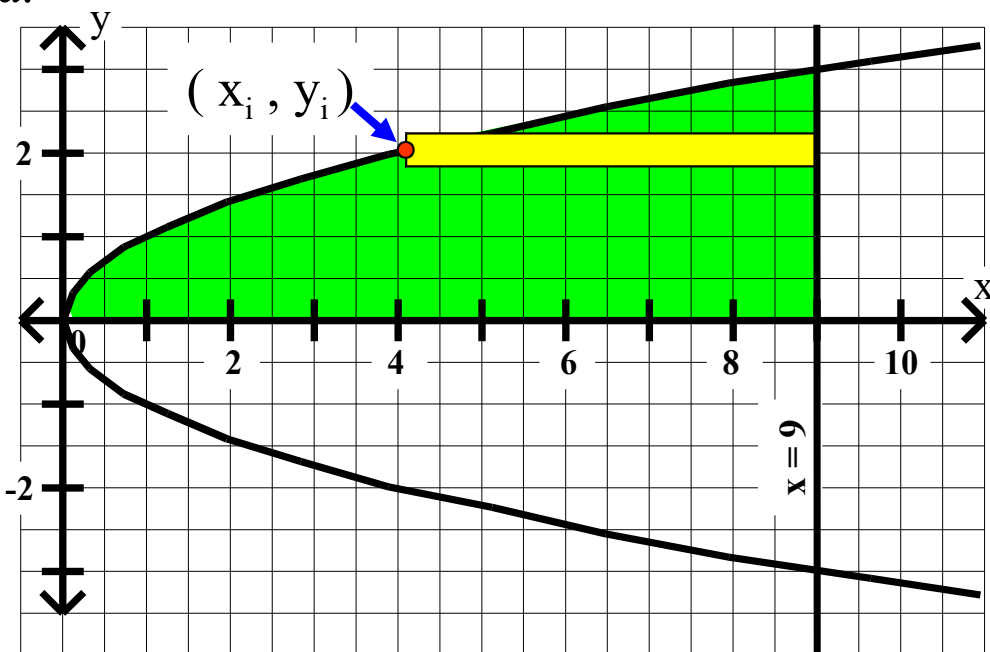
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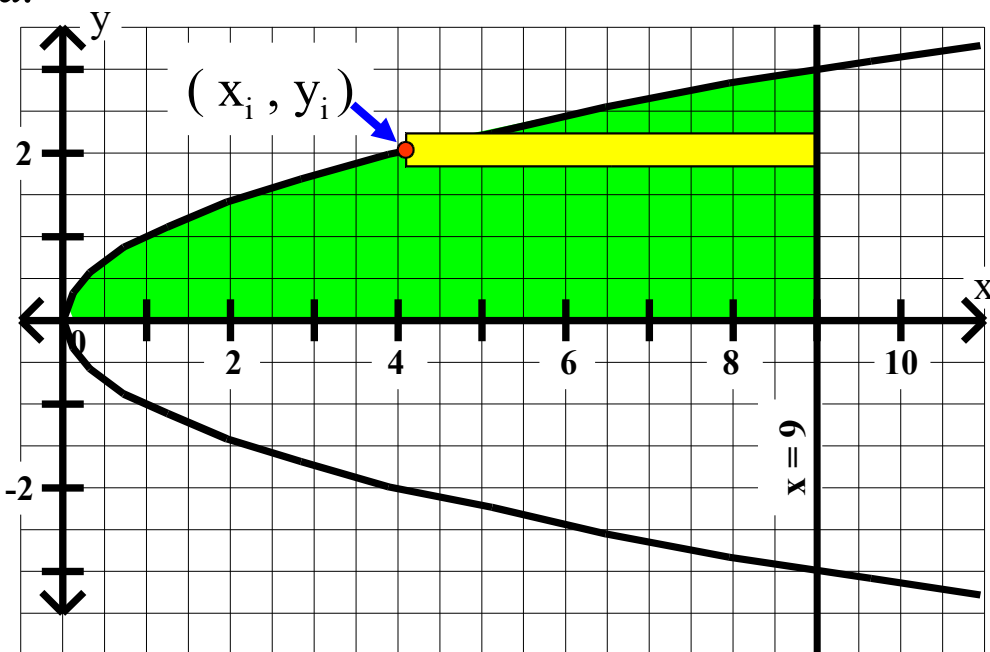
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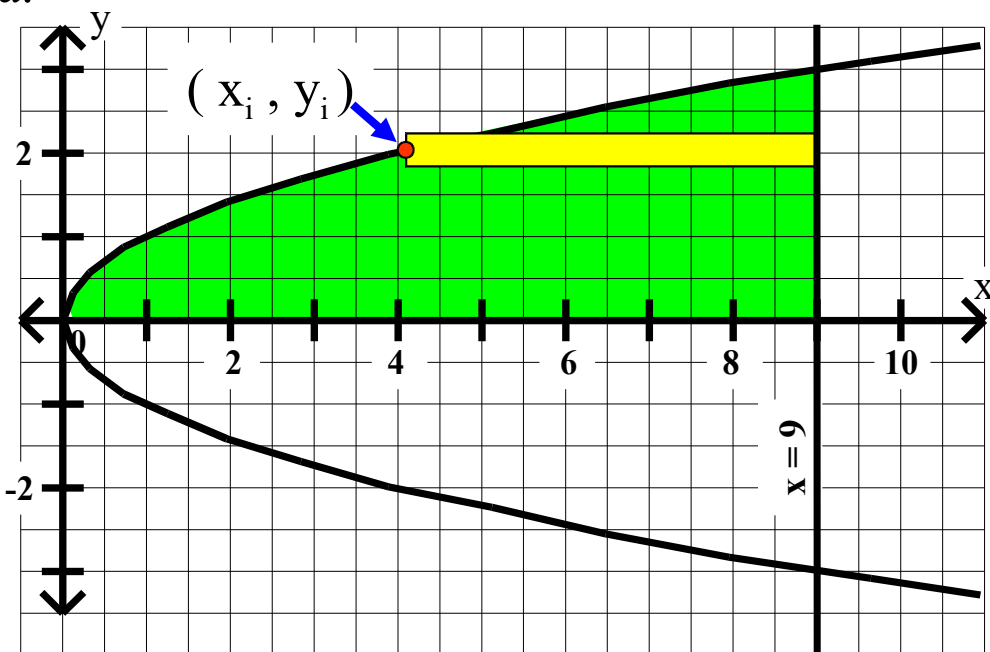
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c. $V = \pi \int_0^3 (9 - y^2)^2 dy$

d. $V \approx$

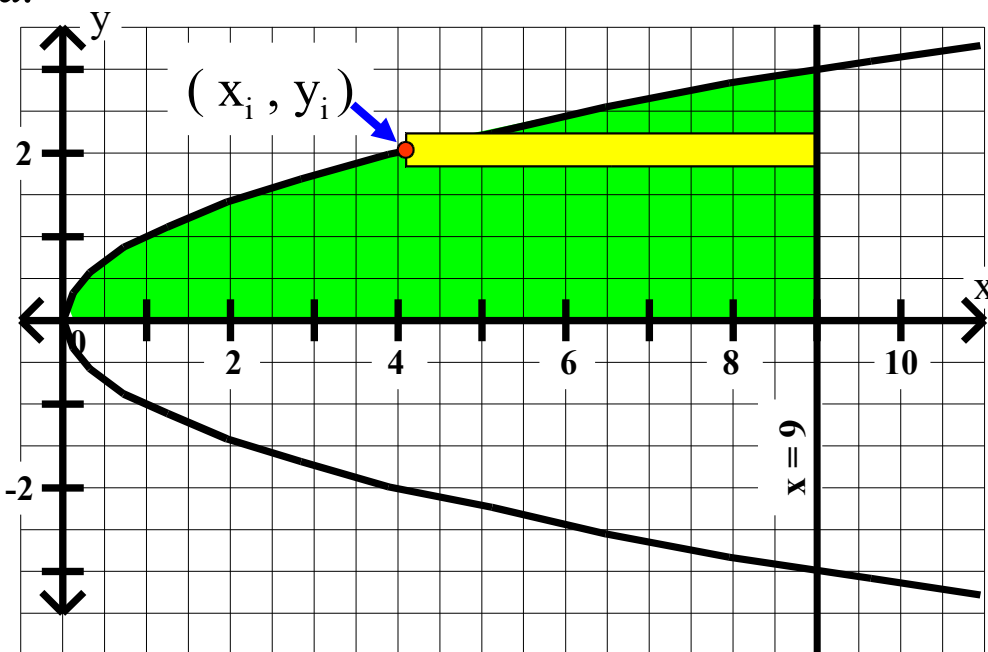
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c. $V = \pi \int_0^3 (9 - y^2)^2 dy$

d. $V \approx 407$ cu. units

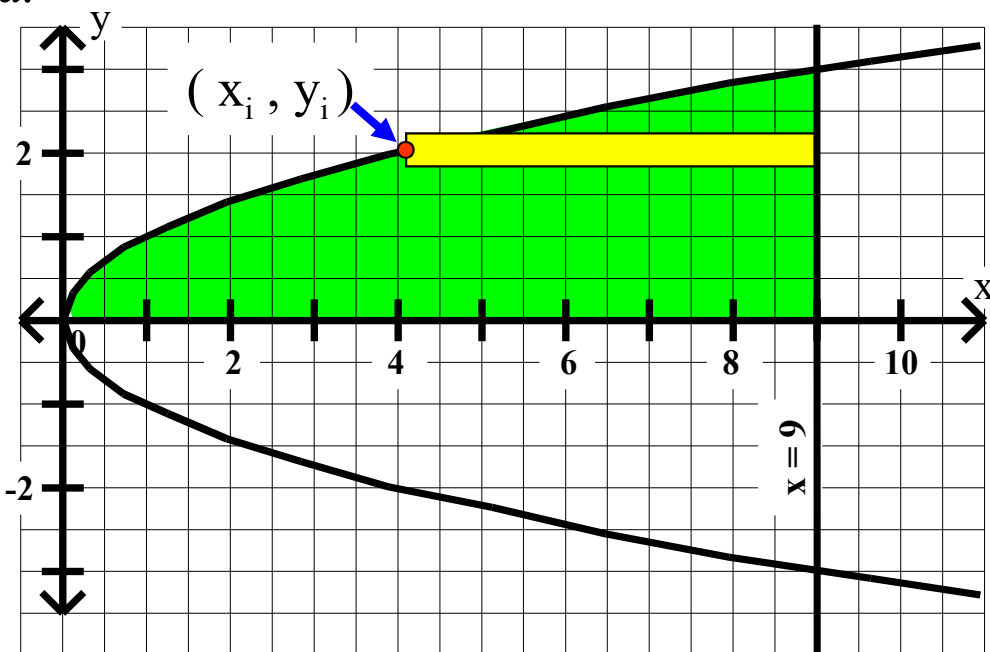
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c. $V = \pi \int_0^3 (9 - y^2)^2 dy$

d. $V \approx 407$ cu. units

