## Calculus Worksheet \#4 Unit 10 Selected Solutions

Sketch the region described in each problem and find its area ( 3 significant digits). 1. The region is bounded by the $x$-axis, the lines $x=1$ and $x=5$, and the graph of the function $f(x)=e^{0.5 x}$.


| $y=e^{0.5 x}$ |  |
| :---: | :---: |
| $\mathbf{x}$ | $y$ |
| 0 | 1 |
| 1 | 1.65 |
| 2 | 2.72 |
| 3 | 4.48 |
| 4 | 7.39 |
| 5 | 12.2 |
| 6 | 20.1 |

$$
\begin{aligned}
A & =\int_{1}^{5} \mathrm{e}^{0.5 \mathrm{x}} \mathrm{dx}=\left.2 \mathrm{e}^{0.5 \mathrm{x}}\right|_{1} ^{5} \\
& =2\left[\mathrm{e}^{2.5}-\mathrm{e}^{0.5}\right] \approx 21.1 \text { sq. units }
\end{aligned}
$$

4. The region is bounded by the $x$-axis, the lines $x=0.5$ and $x=2.5$, and the graph of the function $f(x)=2 / x$.


| $y=\frac{1}{y}$ |  |
| :--- | :--- |
|  |  |
| $x$ | $y$ |
| 1 | 2 |
| 2 | 1 |
| 3 | .667 |
| 4 | .5 |
| 5 | .4 |
| 6 | .333 |

$$
\begin{aligned}
A & =\int_{0.5}^{2.5} \frac{2}{x} d x=\left.2[\ln |x|]\right|_{0.5} ^{2.5} \\
& =2[\ln (2.5)-\ln (0.5)] \\
& =2[\ln (5)]=\ln (25) \approx 3.22 \text { sq. units }
\end{aligned}
$$

