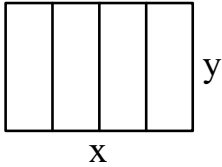


Algebra II Worksheet #6 Unit 8 Selected Homework Solutions

6. Sam wants to fence in a rectangular plot of land **and** to divide it into four equal areas using three lengths of fencing parallel to two opposite sides. If he has a total of 800 feet of fencing to work with, then find the dimensions that will maximize the total area enclosed. What is the maximum area?



Consider the diagram shown. Let x represent the length of the rectangular plot of land. Let y represent its width.

Clearly, the total amount of fencing required is $2x + 5y$.

Once again, to maximize the area, we must represent the area as a function of one variable.

$$\begin{aligned} A &= xy \text{ where } 2x + 5y = 800 \\ 5y &= -2x + 800 \\ y &= -.4x + 160 \end{aligned}$$

Therefore,

$$\begin{aligned} A &= x(-.4x + 160) \\ A &= -.4x^2 + 160x \end{aligned}$$

The maximum area corresponds to the vertex of this function.

$$\begin{aligned} A &= -.4(x^2 - 400x) \\ A - 16,000 &= -.4(x^2 - 400x + 40,000) \\ A - 16,000 &= -.4(x - 200)^2 \\ \text{The vertex is } (200, \underline{16,000}). \\ \text{For maximum area, } x &= 200. \\ y &= -.4(200) + 160 = -80 + 160 = 80. \end{aligned}$$

**The plot with maximum area is 200 feet long and 80 feet wide.
The plot will have a maximum area of 16,000 square feet.**