

Algebra II Worksheet #1 Unit 8 Selected Solutions

A steel ball is propelled upward from a point that is 224 feet above the ground. Its height, h (in feet), above the ground after t seconds is given by the function $h = -16t^2 + 80t + 224$, where $t \geq 0$. Use this equation to answer the following questions.

1. How high above the ground will the ball be after 3 seconds?

$$\begin{aligned}\text{Find } h \text{ when } t = 3. \quad h &= -16(3)^2 + 80(3) + 224 \\ h &= -16(9) + 240 + 224 \\ h &= -144 + 240 + 224 = 320\end{aligned}$$

The ball will be 320 feet high after 3 seconds.

3. When will the ball be 288 feet above the ground?

$$\begin{aligned}\text{Find } t \text{ when } h = 288. \quad 288 &= -16t^2 + 80t + 224 \\ 16t^2 - 80t + 64 &= 0 \\ t^2 - 5t + 4 &= 0 \\ (t - 1)(t - 4) &= 0 \\ t &= 1 \text{ or } t = 4\end{aligned}$$

The ball will be 288 feet high after 1 second and again after 4 seconds.

7. What is the maximum height that the ball will reach and how long will it take it to reach that height?

Find the vertex of the function $h = -16t^2 + 80t + 224$.

$$\begin{aligned}h - 224 &= -16(t^2 - 5t) \\ h - 224 - 100 &= -16(t^2 - 5t + 6.25) \\ h - 324 &= -16(t - 2.5)^2 \\ \text{Vertex: } &(2.5, 324)\end{aligned}$$

The maximum height is 324 feet. It will take 2.5 seconds to reach that height.