

Algebra I Worksheet #6 Unit 9 selected solutions

2. The sum of two numbers is 100. The first number is two less than five times the second. What are the numbers?

$$\begin{array}{l} \text{first number : } x \\ \text{second number : } y \end{array} \quad \begin{array}{l} x + y = 100 \\ x = 5y - 2 \end{array} \quad \begin{array}{l} (5y - 2) + y = 100 \\ 6y - 2 = 100 \\ 6y = 102 \\ y = 17 \\ x = 83 \end{array}$$

The first number is 83, and the second is 17.

4. Coffee worth 80¢ per pound is mixed with coffee worth 50¢ per pound to produce a twenty pound blend worth 68¢ per pound. How many pounds of each type of coffee is used?

$$\begin{array}{l} \text{Am't of coffee @ 80¢ per pound: } x \\ \text{Am't of coffee @ 50¢ per pound: } y \end{array} \quad \begin{array}{l} x + y = 20 \text{ (pounds)} \\ 80x + 50y = 1360 \text{ (cents)} \end{array} \quad \begin{array}{l} -5x - 5y = -100 \\ 8x + 5y = 136 \\ 3x = 36 \\ x = 12 \text{ and } y = 8 \end{array}$$

Note: 20 pounds @ 68¢ per pound has a total value of 1360¢.
Use 12 pounds @ 80¢ per pound and 8 pounds @ 50¢ per pound.

8. A collection of ordinary dimes and nickels is worth \$6.65. The number of nickels is seven less than two times the number of dimes. How many coins of each type are in the collection?

$$\begin{array}{l} \text{Number of dimes: } d \\ \text{Number of nickels: } n \\ \text{Value of the dimes: } 10d \text{ (cents)} \\ \text{Value of the nickels } 5n \text{ (cents)} \end{array} \quad \begin{array}{l} n = 2d - 7 \\ 10d + 5n = 665 \end{array} \quad \begin{array}{l} 10d + 5(2d - 7) = 665 \\ 10d + 10d - 35 = 635 \\ 20d - 35 = 635 \\ 20d = 700 \\ d = 35 \text{ and } n = 63 \end{array}$$

There are 35 dimes and 63 nickels.

10. \$5000 is to be divided between two people so that one receives \$500 more than twice what the other receives. How much will each person receive?

$$\begin{array}{l} \text{Am't received by one person: } x \\ \text{Am't received by other person: } y \end{array} \quad \begin{array}{l} x + y = 5000 \\ y = 2x + 500 \end{array} \quad \begin{array}{l} x + (2x + 500) = 5000 \\ 3x + 500 = 5000 \\ 3x = 4500 \\ x = 1500 \\ y = 3500 \end{array}$$

One receives \$1500, and the other receives \$3500.