

Algebra I Worksheet #10 Unit 8 Selected Solutions

A rectangular water tank is 8 feet long, 5 feet wide, and 6 feet deep. The tank is **full** initially and water is drained out of the tank at a constant rate of 10 cubic feet per minute until the tank is empty. Let t represent the time that water has been draining out of the tank (in **minutes**). Let $f(t)$ represent the **depth of the water** in the tank (in **inches**). Answer each of the following.

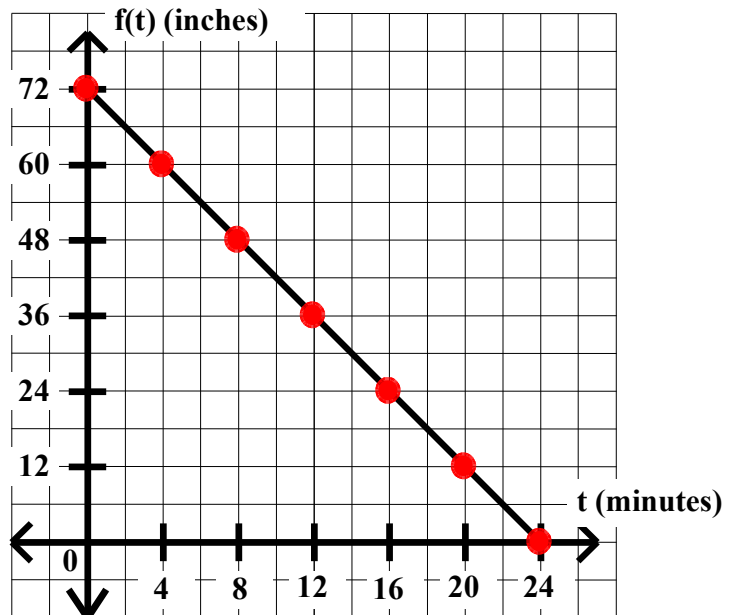
9. How long will it take to empty the tank? **24 minutes**

$V = LWH = (8 \text{ ft.})(5 \text{ ft.})(6 \text{ ft.}) = 240$ cubic feet The tank is full to start with. Water is drained at 10 cubic feet per minute. The time to empty the tank = $(240 \text{ cu.ft.}) / (10 \text{ cu.ft. per minute}) = 24$ minutes

10. Make a table giving t and $f(t)$ every 4 minutes from $t = 0$ until the tank is empty.

t minutes	$f(t)$ inches
0	72
4	60
8	48
12	36
16	24
20	12
24	0

11. Graph function f .



12. Write an equation giving $f(t)$ in terms of t .

$f(t) = -3t + 72$

The depth of the water decreases at a constant rate. Since the depth decreases a total of 72 inches in 24 minutes, it decreases at 3 inches per minute. The slope of the graph is -3 (inches per minute). Since the depth is 72 inches initially, the 'y-intercept' is 72. Using the slope-intercept model, the equation is $f(t) = -3t + 72$.

13. Write an inequality to describe the domain of function f . **$0 \leq t \leq 24$**

14. Write an inequality to describe the range of function f . **$0 \leq f(t) \leq 72$**

15. Evaluate $f(5)$. What does $f(5)$ represent in terms of the problem?

$f(5) = -3(5) + 72 = \mathbf{57 \text{ inches}}$
 $f(5)$ represents the depth of the water in the tank after 5 minutes.

16. If $f(t) = 15$, then find the value of t . Describe what this value of t represents in terms of the problem.

$-3t + 72 = 15$
 $-3t = -57$
 $t = \mathbf{19 \text{ minutes}}$
This value of t represents the time it takes for the water in the tank to be 15 inches deep.