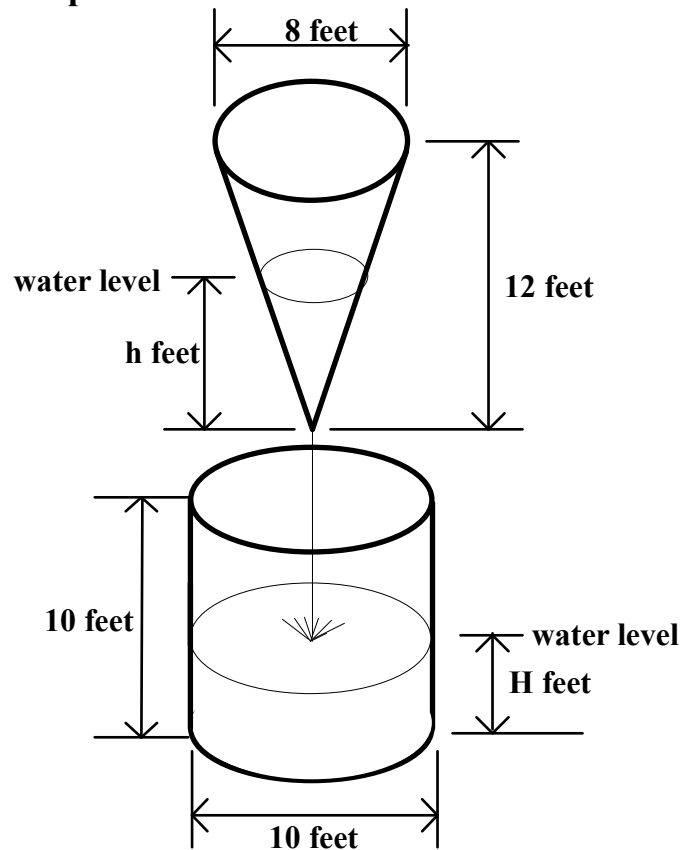


Advanced Challenge Level 2 Problem #21

Water is draining out of a conical tank into a cylindrical tank. (Please refer to the diagram below.) The conical tank is 12 feet deep and has a diameter of 8 feet at the top. The cylindrical tank is 10 feet deep and has a diameter of 10 feet. Show your work carefully organized and explained.



The depth, h (feet), of water in the conical tank is changing at the rate of $(0.5h - 8)$ feet per minute. Answer the following questions.

1. Write an expression for the volume of water in the conical tank as a function of h .
2. At what rate is the depth of the water in the conical tank changing when $h = 5$ feet?
3. At what rate is the volume of the water in the conical tank changing when $h = 5$ feet?
4. At what rate is the volume of the water in the cylindrical tank changing when $h = 5$ feet?
5. Let H be the depth of the water in the cylindrical tank. Write an expression for the volume of water in the cylindrical tank as a function of H .
6. At what rate is H changing when $h = 5$ feet?
7. At what rate is H changing when $h = 12$ feet?
8. At what rate is H changing when $h = 2$ feet?