## Advanced Challenge Level 2 Problem \#14 page 1

For this problem of the week, you are given three velocity-time graphs. Assume that $\mathbf{v}>0$ implies movement to the right and $\mathbf{v}<0$ implies movement to the left. Any reference to starting point refers to the position of the particle when $t=0$. Good luck.
A particle moves on a straight line in such a way that its velocity (in feet per second), as a function of time (in seconds) is shown by function $f$ below.


Answer the following questions.

1. Fill out the following table.

|  | $\mathbf{0} \leq \mathbf{t} \leq \mathbf{3}$ | $\mathbf{3} \leq \mathbf{t} \leq \mathbf{6}$ | $\mathbf{6} \leq \mathbf{t} \leq \mathbf{9}$ | $\mathbf{9} \leq \mathbf{t} \leq \mathbf{1 2}$ | $\mathbf{0} \leq \mathbf{t} \leq \mathbf{1 2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| a. average acceleration |  |  |  |  |  |
| b. distance moved <br> c. average velocity |  |  |  |  |  |
| d. average speed |  |  |  |  |  |
| e. final distance from <br> starting point |  |  |  |  |  |

2. Evaluate each of the following: $f(2)=$ $\qquad$ $f(5)=$ $\qquad$ $\mathrm{f}(8)=$ $\qquad$ $\mathrm{f}(11)=$ $\qquad$
3. Evaluate each of the following: $\qquad$ $f^{\prime}(5)=$ $\qquad$ $f^{\prime}(8)=$ $\qquad$ $f^{\prime}(11)=$ $\qquad$
4. Evaluate each of the following.

$$
\int_{0}^{3} f(x) d x=\_\int_{3}^{6} f(x) d x=\_\int_{6}^{9} f(x) d x=\_\int_{9}^{12} f(x) d x=\_\int_{0}^{12} f(x) d x=
$$

## Advanced Challenge Problem \#45 page 2

A particle moves on a horizontal line in such a way that its velocity (in feet per second), as a function of time (in seconds) is shown by function $g$ below.


Answer the following questions.
5. Fill out the following table.

|  | $0 \leq \mathbf{t} \leq \mathbf{3}$ | $\mathbf{3} \leq \mathbf{t} \leq \mathbf{6}$ | $\mathbf{6 \leq t \leq 9} \leq 9 \leq \mathrm{t} \leq \mathbf{1 2}$ | $0 \leq \mathbf{t} \leq \mathbf{1 2}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| a. average acceleration |  |  |  |  |  |
| b. distance moved |  |  |  |  |  |
| c. average velocity |  |  |  |  |  |
| d. average speed <br> e. final distance from <br> starting point |  |  |  |  |  |

6. Evaluate each of the following: $g(2)=$ $\qquad$ $g(5)=$ $\qquad$ $g(8)=$ $\qquad$ $\mathrm{g}(11)=$ $\qquad$
7. Evaluate each of the following: $\qquad$ $g^{\prime}(5)=$ $\qquad$ $g^{\prime}(8)=$ $\qquad$ $g^{\prime}(11)=$
8. Evaluate each of the following.
$\int_{0}^{3} g(x) d x=\_\int_{3}^{6} g(x) d x=\_\int_{6}^{9} g(x) d x=\quad \int_{9}^{12} g(x) d x=\_\int_{0}^{12} g(x) d x=$

## Advanced Challenge Problem \#45 page 3

A particle moves on a horizontal line in such a way that its velocity (in feet per second), as a function of time (in seconds) is shown by function $h$ below.


Answer the following questions.
9. Fill out the following table.

|  | $\mathbf{0} \leq \mathbf{t} \leq \mathbf{3}$ | $\mathbf{3} \leq \mathbf{t} \leq \mathbf{6}$ | $\mathbf{6} \leq \mathbf{t} \leq \mathbf{9}$ | $\mathbf{9} \leq \mathbf{t} \leq \mathbf{1 2}$ | $\mathbf{0} \leq \mathbf{t} \leq \mathbf{1 2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| a. average acceleration |  |  |  |  |  |
| b. distance moved |  |  |  |  |  |
| c. average velocity |  |  |  |  |  |
| d. average speed <br> e. final distance from <br> starting point |  |  |  |  |  |

10. Evaluate each of the following: $h(2)=$ $\qquad$ $h(5)=$ $\qquad$ $\mathbf{h}(8)=$ $\qquad$ $h(11)=$ $\qquad$
11. Evaluate each of the following: $h^{\prime}(2)=$ $\qquad$ $h^{\prime}(5)=$ $\qquad$ $h^{\prime}(8)=$ $\qquad$ $h^{\prime}(11)=$ $\qquad$
12. Evaluate each of the following.
$\int_{0}^{3} h(x) d x=\_\int_{3}^{6} h(x) d x=\_\int_{6}^{9} h(x) d x=\quad \int_{9}^{12} h(x) d x=\_\int_{0}^{12} h(x) d x=$
