Advanced Challenge Level 2 Problem #12

The diagram below shows a horizontal line with a fixed point P. Another point (not shown) moves on this line for ten seconds. The function $s = f(t) = 0.5t^2 - 4t + 6$ represents the distance, s, in inches, that the moving point is from point P. t represents the time in seconds that the point has been moving where $0 \le t \le 10$. It is understood that if s > 0, then the moving point is to the right of point P, and if s < 0, then the moving point is to the left of point P.



1. Write a function for the velocity of the moving point. v =_____

2. What is the position and the velocity of the moving point when t = 0 seconds?

3. What is the position and the velocity of the moving point when t = 4 seconds?

4. What is the position and the velocity of the moving point when t = 10 seconds?

5. What is the average velocity of the moving point from t = 0 seconds to t = 4 seconds?

6. Find a value of t between 0 and 4 when the velocity of the moving point is equal to the average velocity you found in question # 5.

7. What is the average velocity of the moving point from t = 4 seconds to t = 10 seconds?

8. Find a value of t between 4 and 10 when the velocity of the moving point is equal to the average velocity you found in question # 7.

9. What is the average velocity of the moving point from t = 0 seconds to t = 10 seconds?

10. Find a value of t between 0 and 10 when the velocity of the moving point is equal to the average velocity you found in question # 9.

11. Write an algebraic expression for the average velocity of the moving point from t = a seconds to t = b seconds where $0 \le a \le b \le 10$.

12. Represent, in terms of a and b, a value of t between a and b when the velocity of the moving point is equal to the average velocity you found in question # 11.