## Advanced Challenge Level 2 Problem \#12

The diagram below shows a horizontal line with a fixed point $P$. Another point (not shown) moves on this line for ten seconds. The function $s=f(t)=0.5 t^{2}-4 t+6$ represents the distance, $s$, in inches, that the moving point is from point $P$. $t$ represents the time in seconds that the point has been moving where $0 \leq t \leq 10$. It is understood that if $\mathrm{s}>\mathbf{0}$, then the moving point is to the right of point $P$, and if $s<0$, then the moving point is to the left of point $P$.


1. Write a function for the velocity of the moving point. $v=$ $\qquad$
2. What is the position and the velocity of the moving point when $t=0$ seconds?
3. What is the position and the velocity of the moving point when $t=4$ seconds?
4. What is the position and the velocity of the moving point when $t=10$ seconds?
5. What is the average velocity of the moving point from $t=0$ seconds to $t=4$ seconds?
6. Find a value of $t$ between 0 and 4 when the velocity of the moving point is equal to the average velocity you found in question \# 5 .
7. What is the average velocity of the moving point from $t=4$ seconds to $t=10$ seconds?
8. Find a value of $t$ between 4 and 10 when the velocity of the moving point is equal to the average velocity you found in question \# 7 .
9. What is the average velocity of the moving point from $t=0$ seconds to $t=10$ seconds?
10. Find a value of $t$ between 0 and 10 when the velocity of the moving point is equal to the average velocity you found in question $\# 9$.
11. Write an algebraic expression for the average velocity of the moving point from $t=a$ seconds to $t=b$ seconds where $0 \leq a<b \leq 10$.
12. Represent, in terms of $a$ and $b$, a value of $t$ between $a$ and $b$ when the velocity of the moving point is equal to the average velocity you found in question \# 11.
