Advanced Challenge Level 2 Problem #3

Consider the following definition.

The inclination of a line is defined as follows:

If a line is horizontal, then its inclination is 0°. If a line is not horizontal, then its inclination is the angle measured counter clockwise from the x-axis to the line.

Note that the inclination of a line is never negative and always less than 180°.

The symbol α is used to represent the inclination of a line. The inclination is usually expressed in degrees, but may also be expressed in radians.

Let α_1 , α_2 , and α_3 represent the inclinations of lines L_1 , L_2 , and L_3 , shown below. Since line L_1 is a horizontal line, its inclination $\alpha_1 = 0^\circ$. The inclination of line L_2 is an obtuse angle. $\alpha_2 \approx 153^\circ$.

The inclination of line L_3 is an acute angle. $\alpha_3 = 45^{\circ}$.



You have to do each of the following.

1. Derive a relationship between the slope of a line and its inclination.

2. Use your relationship to find the inclination of the following lines. Where appropriate, round your answers to three significant digits.

(a) y = 2x(b) x = 3(c) y = -5(d) y = -2x(e) 3x + 5y = -10(f) 5x - 2y = -6

Show your complete process, including your reasoning, neatly organized.